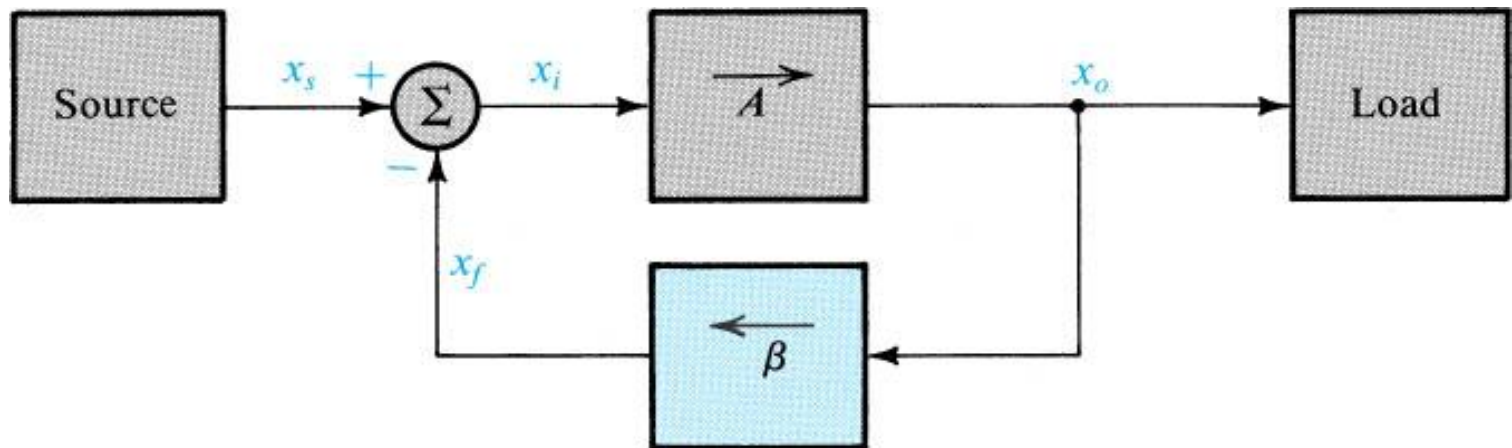


# CHAPTER 10



# Feedback

- Consists of **returning part** of the output of a system to the input
- **Negative Feedback**: a portion of the output signal is returned to the input in opposition to the original input signal
- **Positive Feedback**: the feedback signal aids the original input signal
- Negative Feedback Effects:
  - Reduces gain
  - Stabilizes gain
  - Reduces non linear distortion
  - Reduces certain types of noise
  - Controls input and output impedances
  - Extends bandwidth
- The disadvantage of reducing the gain can be overcome by adding few more stages of amplification

## **Advantages of Negative Feedback**

- 1. Gain Sensitivity** – variations in gain is reduced
- 2. Bandwidth Extension** – larger than that of basic amplifier
- 3. Noise Sensitivity** – may increase S/N ratio
- 4. Reduction of Nonlinear Distortion**
- 5. Control of Impedance Levels** – input and output impedances can be increased or decreased

## **Disadvantages of Negative Feedback**

- 1. Circuit Gain** – reduced compared to that of basic amplifier
- 2. Stability** – possibility that feedback circuit will become unstable and oscillate at high frequencies

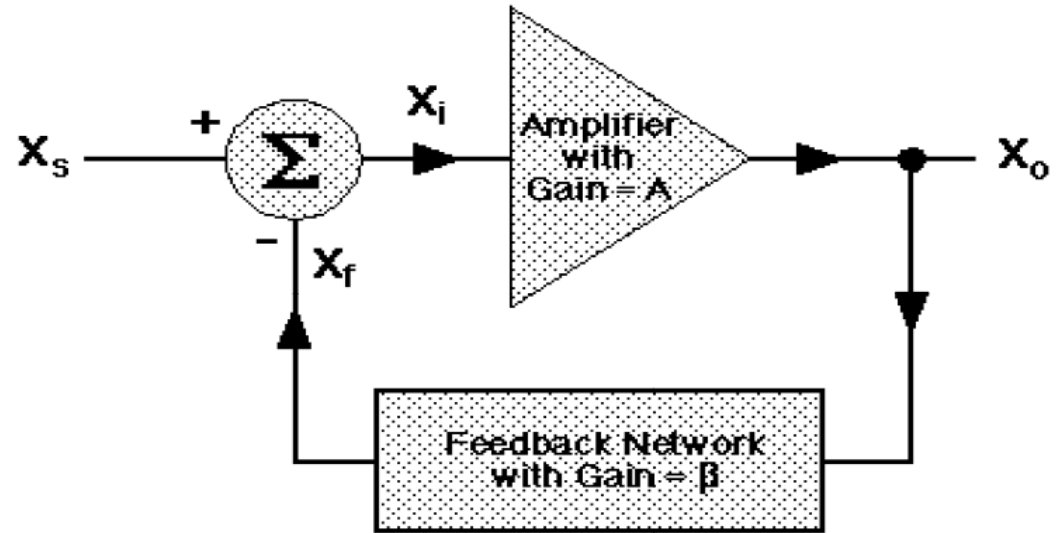
# THE BASIC FEEDBACK CIRCUIT

- Input to the amplifier is:

$$X_i = X_s - X_f$$

- Output of the amplifier is:

$$X_o = AX_i$$



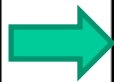
- Output signal in terms of input and feedback gain:

$$X_o = A(X_s - X_f) = A(X_s - \beta X_o)$$

- Rearranging:  $X_o = AX_s - A\beta X_o \rightarrow X_o(1 + A\beta) = AX_s$

- From which we obtain the negative feedback equation by solving for the overall gain:

$$A_{fb} \equiv \frac{X_o}{X_s} = \frac{A}{1 + A\beta}$$



$$A_{fb} \equiv \frac{X_o}{X_s} = \frac{A}{1 + A\beta} \approx \frac{1}{\beta} \quad \text{for large } A$$

## Example

How good is the  $1/\beta$  approximation?

Assume open-loop gain is  $A = 1 \times 10^5$ , and the closed-loop gain is  $A_f = 50$ . Then

$$A_f = \frac{A}{1 + \beta A}$$

$$\beta = 0.01999$$

$$50 = \frac{1 \times 10^5}{1 + \beta \times 10^5}$$

$$A_f \cong 1/\beta = 50.025$$

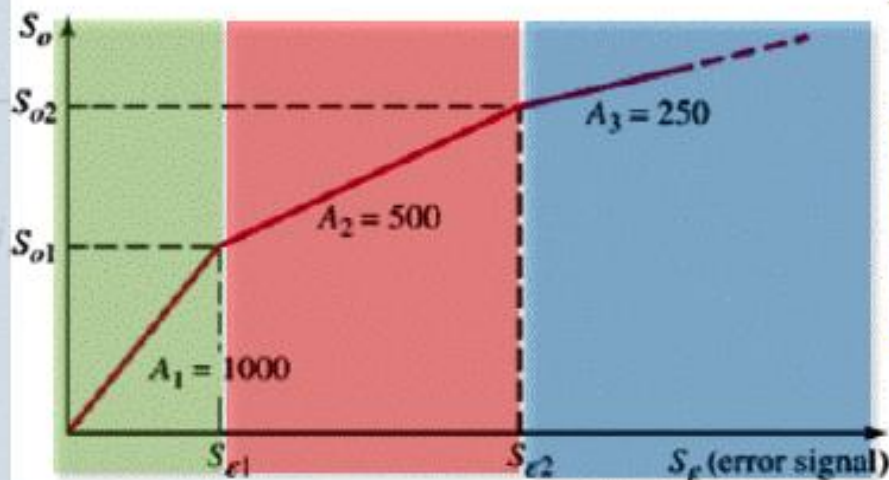
Assume open-loop gain is  $A = 10^6$ , with the same  $\beta$

$$A_f = \frac{A}{1 + \beta A} = \frac{1 \times 10^6}{1 + \beta 10^6} = 50.025$$

Practically the same closed-loop gain

# Reduction of Nonlinear Distortion

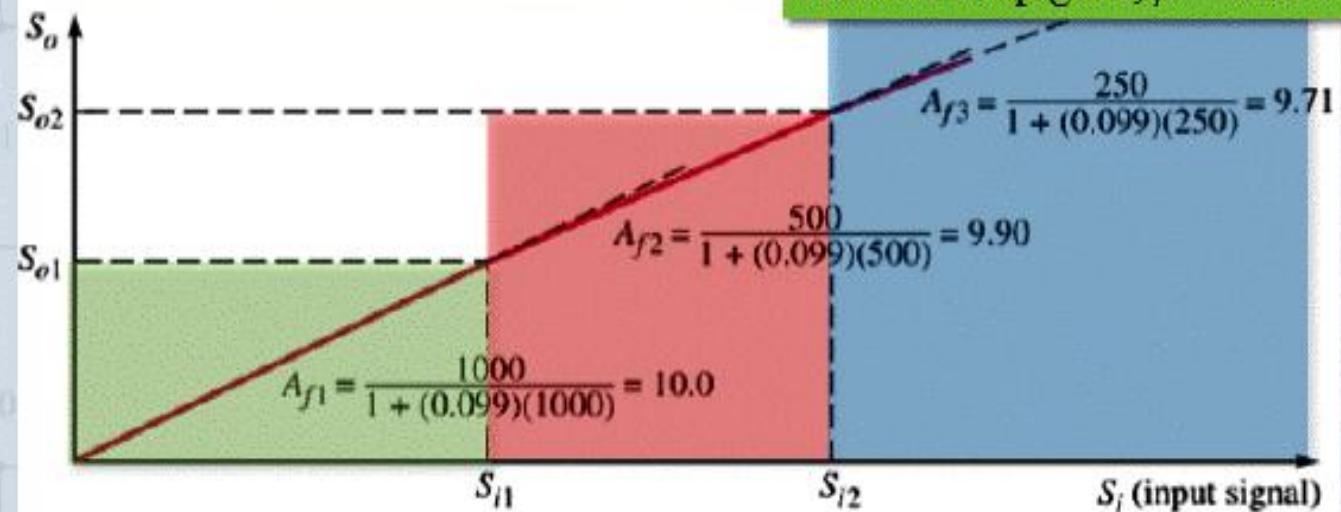
Open-Loop Gain



Non-linear because the gain depends on the signal

$$A_f = \frac{A}{1 + \beta A} \equiv \frac{1}{\beta}$$

Closed-loop gain,  $\beta = 0.099$



# Gain Sensitivity

$$A_f = \frac{A}{1 + \beta A}$$

$$\frac{dA_f}{dA} = \frac{1}{1 + \beta A} - \frac{A}{(1 + \beta A)^2} \beta = \frac{1}{(1 + \beta A)^2}$$

$$dA_f = \frac{dA}{(1 + \beta A)^2}$$

Dividing both sides with closed-loop gain yields

$$\frac{dA_f}{A_f} = \frac{\frac{dA}{(1 + \beta A)^2}}{\frac{A}{1 + \beta A}} = \frac{1}{1 + \beta A} \frac{dA}{A}$$

$$\left( \frac{dA_f}{A_f} \right) \left( \frac{dA}{A} \right) = \frac{1}{1 + \beta A}$$

This shows that the % change in closed-loop gain is smaller, by a factor  $1 + \beta A$ , than the % change in open-loop gain.

# Gain Sensitivity

An engineer designed a feedback amplifier  $\beta = 0.01999$ , and  $A = 1 \times 10^5$ . By how much does the closed-loop gain change when the same feedback network is used, but an amplifier with open-loop gain  $A = 1 \times 10^6$  is used?

$$\begin{aligned}\frac{dA_f}{A_f} &= \frac{1}{1 + \beta A} \frac{dA}{A} = \frac{1}{1 + (0.01999) \times 10^5} \frac{10^6 - 10^5}{10^5} \\ &= 4.5 \times 10^{-3} \\ &= 0.45\%\end{aligned}$$

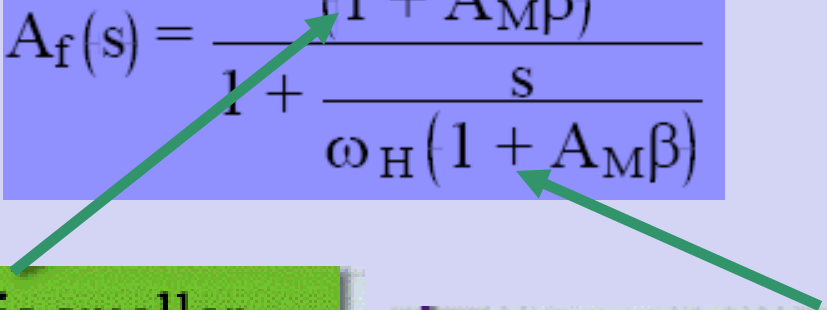
In other words, the open-loop gain changed by a factor 10, while the closed loop gain changed about 0.5%.

# Gain Versus Frequency

Assume we can characterize the frequency response of an amplifier with a single pole

$$A(s) = \frac{A_M}{1 + \frac{s}{\omega_H}}$$

$$A_f(s) = \frac{A(s)}{1 + \beta A(s)}$$

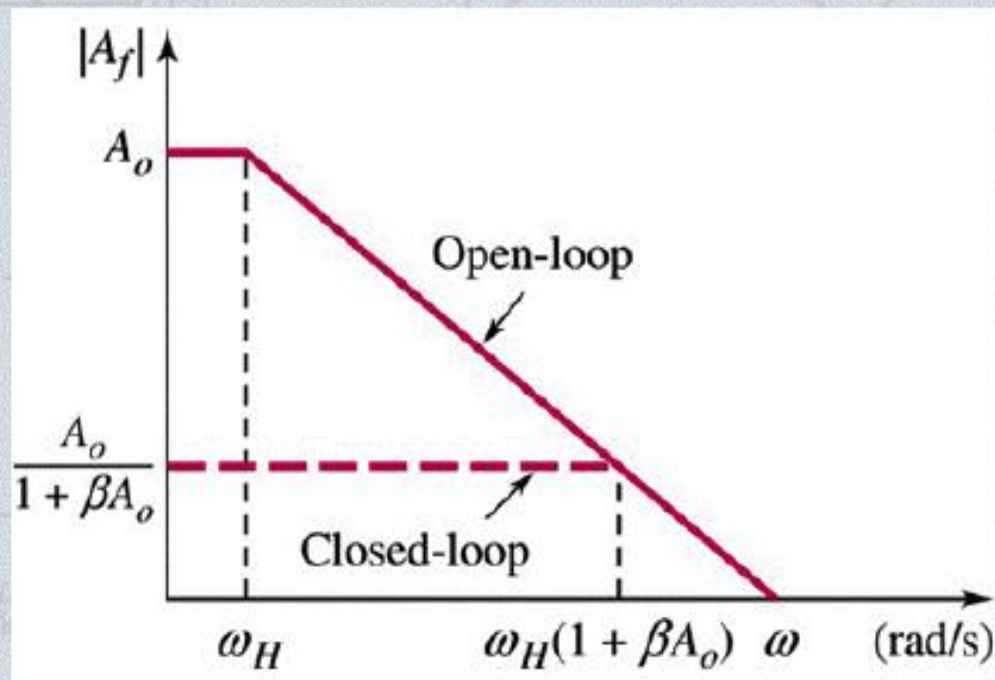
$$A_f(s) = \frac{\frac{A_M}{(1 + A_M\beta)}}{1 + \frac{s}{\omega_H(1 + A_M\beta)}}$$


The closed-loop gain is smaller than the open-loop gain by a factor  $(1 + \beta A)$

The 3 dB bandwidth is larger by a factor  $(1 + \beta A)$

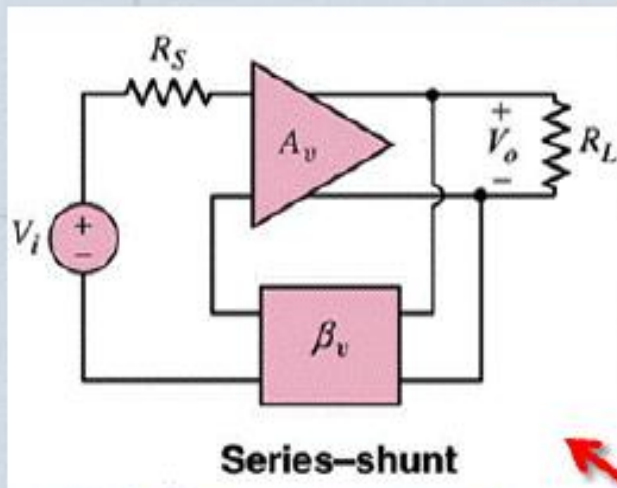
# Gain-Bandwidth Product

Gain-bandwidth product of a feedback amplifier is constant

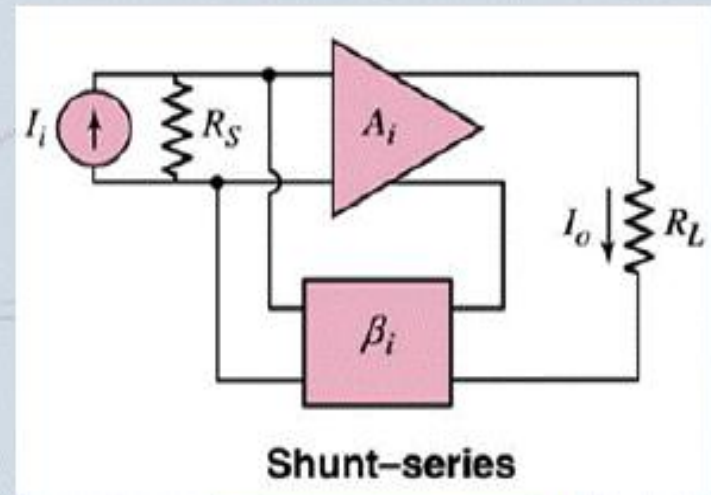


We can increase bandwidth at the expense of gain

# Ideal Basic Feedback Configurations

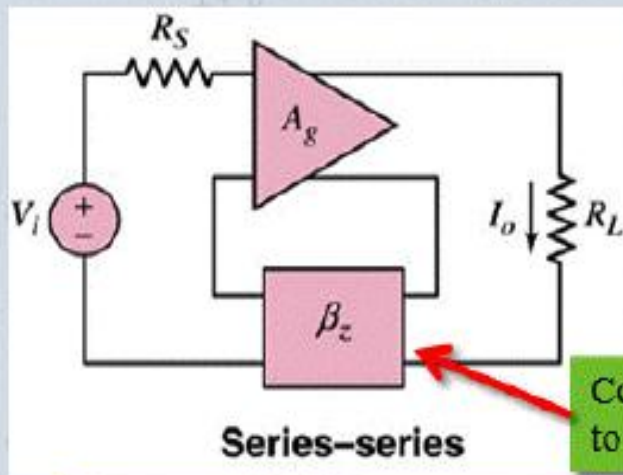


Voltage Amplifier

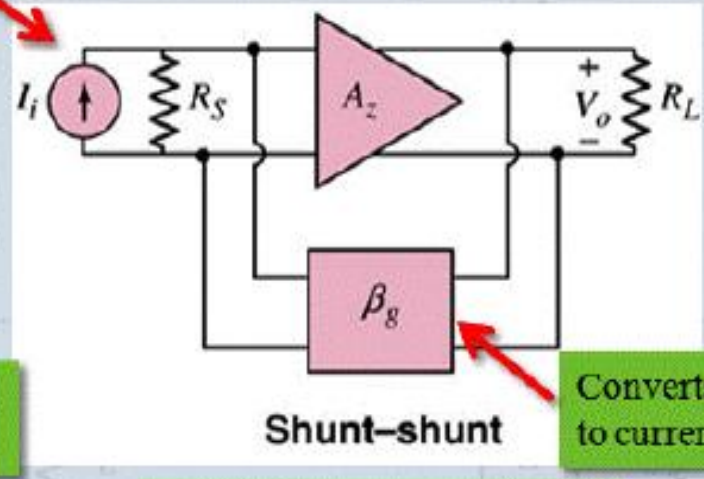


Current Amplifier

Very Common



Transconductance Amplifier  
(voltage in-current out)

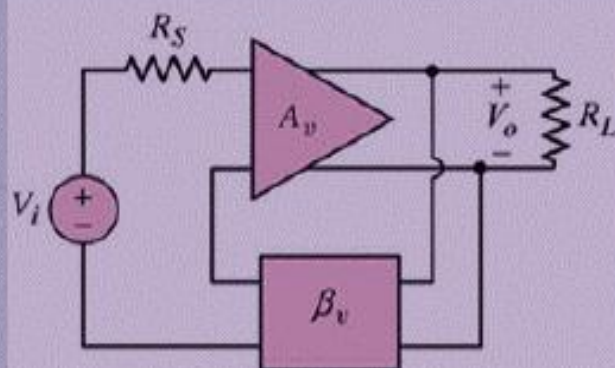


Transresistance Amplifier  
(current in-voltage out)

Converts voltage  
to current

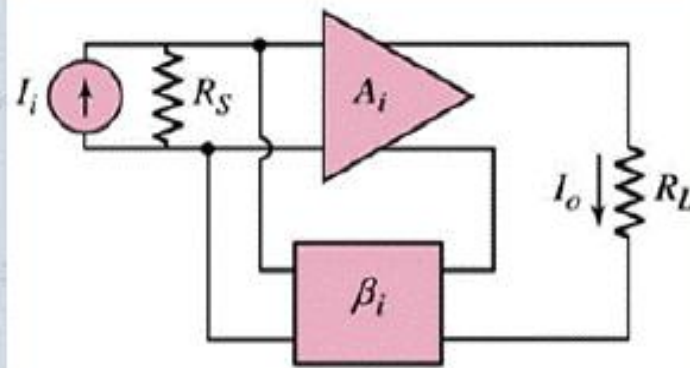
Converts current  
to voltage

# Recap-Ideal Basic Feedback Configurations



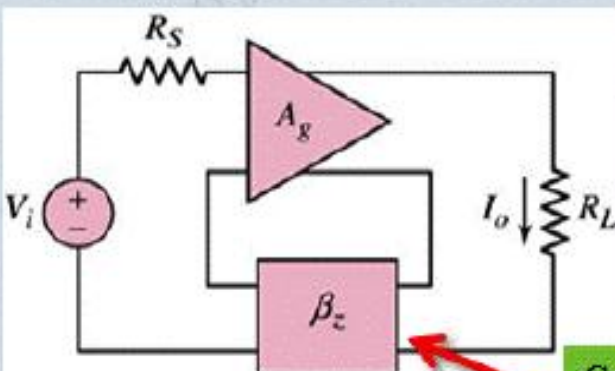
**Series-shunt**

Voltage Amplifier



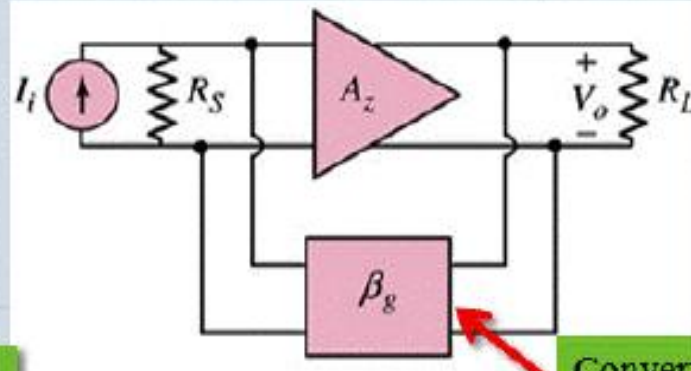
**Shunt-series**

Current Amplifier



**Series-series**

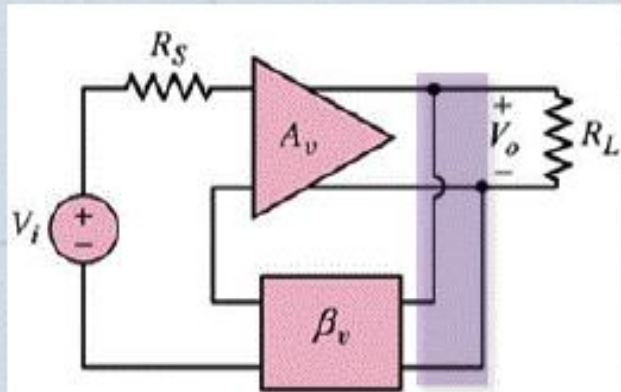
Transconductance Amplifier  
(voltage in-current out)



**Shunt-shunt**

Transresistance Amplifier  
(current in-voltage out)

# Ideal Series-Shunt Feedback



Series-shunt

Voltage Amplifier

$$A_{vf} = \frac{A_v}{1 + \beta_v A_v}$$

Sample output voltage and feed it back to input

Ideal: assume feedback network does not load output/input

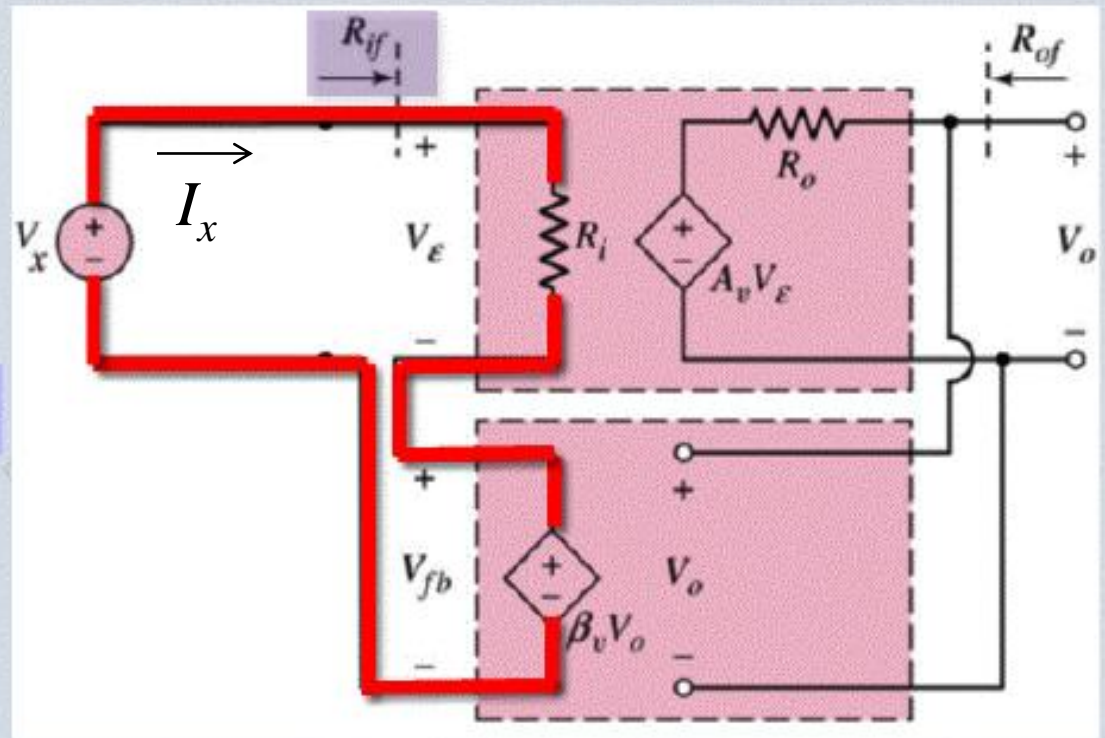
$$V_x = I_x R_i + \beta_v V_o$$

$$= I_x R_i + \beta_v A_v V_\epsilon$$

$$= I_x R_i + \beta_v A_v I_x R_i$$

$$= I_x R_i (1 + \beta_v A_v)$$

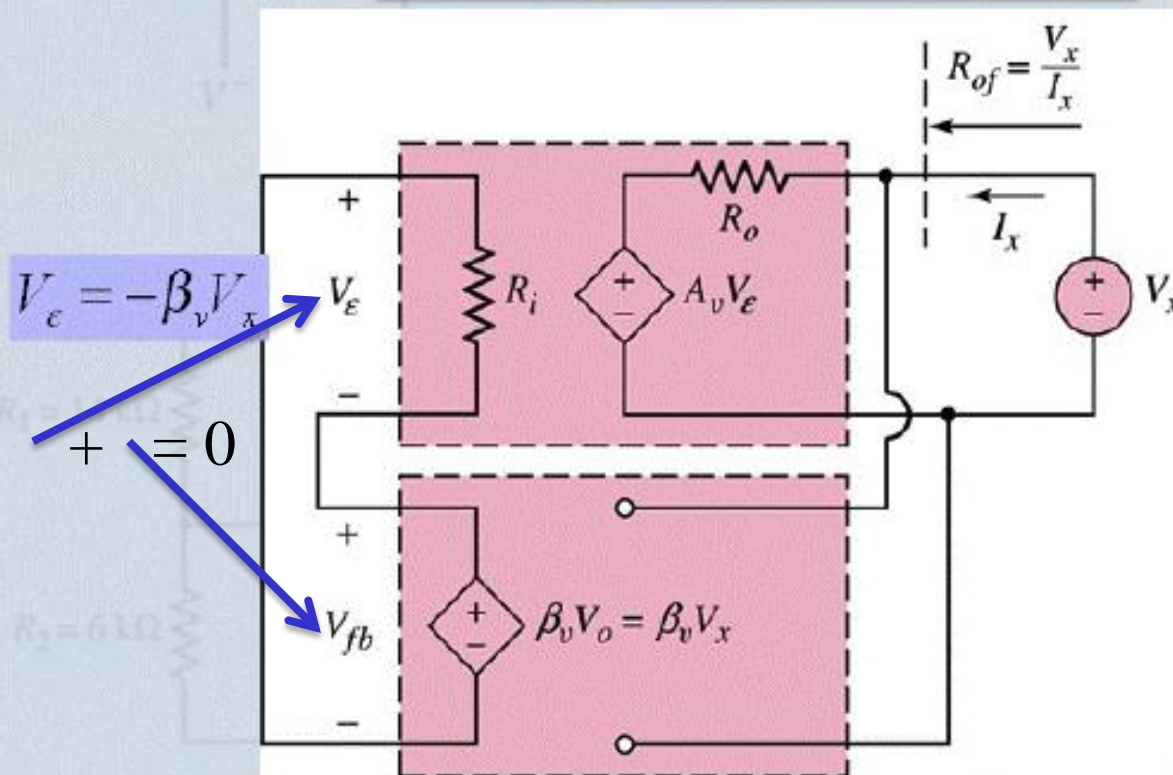
$$R_{if} = \frac{V_x}{I_x} = R_i (1 + \beta_v A_v)$$



# Series-Shunt Feedback Output Resistance

How do we determine output resistance?

1. Turn off independent sources
2. Add test voltage  $V_x$
3. See what test current  $I_x$  flows
4. Determine  $V_x/I_x$



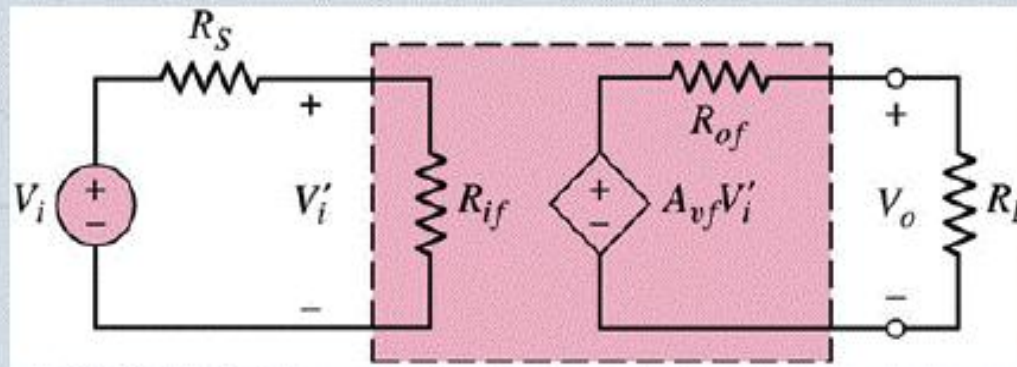
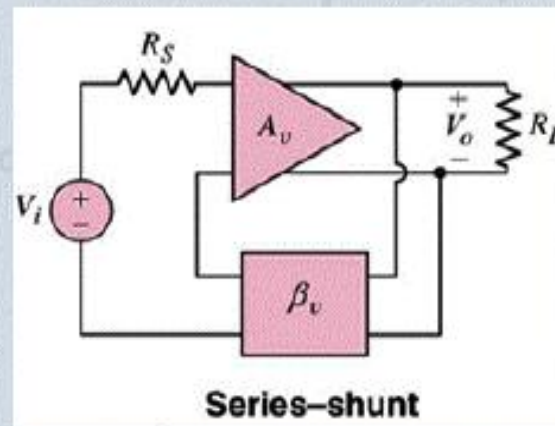
$$I_x = \frac{V_x - A_v V_e}{R_o}$$

$$= \frac{V_x - A_v (-\beta_v V_x)}{R_o}$$

$$= \frac{V_x (1 + \beta_v A_v)}{R_o}$$

$$R_{of} = \frac{V_x}{I_x} = \frac{R_o}{(1 + \beta_v A_v)}$$

# Equivalent Circuit: Series-Shunt Feedback Circuit



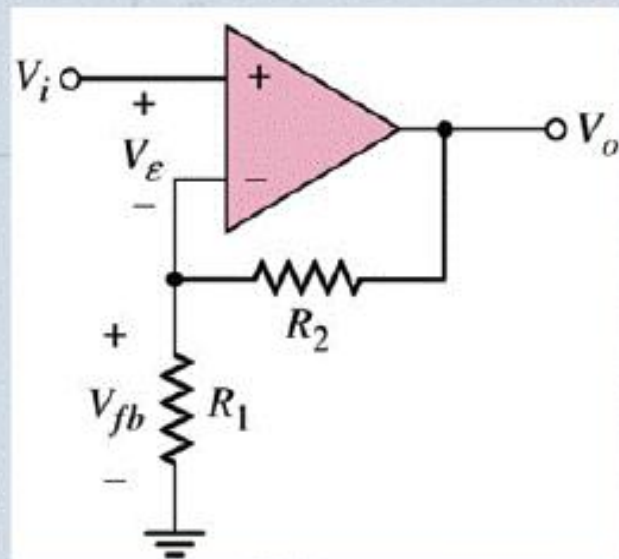
$$R_{if} = R_i (1 + \beta_v A_v)$$

$$A_{vf} = \frac{A_v}{1 + \beta_v A_v}$$

$$R_{of} = \frac{R_o}{(1 + \beta_v A_v)}$$

$$BW_f = (1 + \beta_v A_v) BW$$

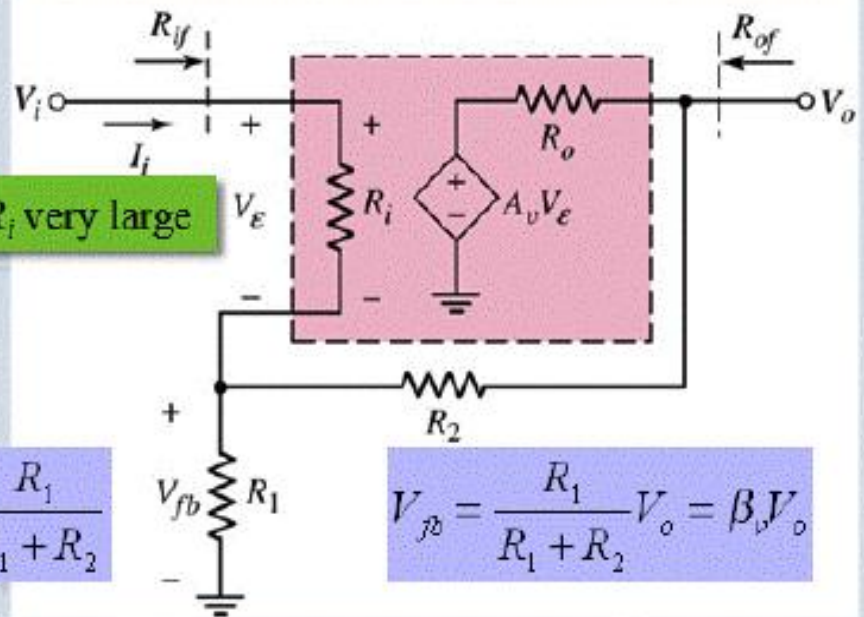
# Op-Amp Series-Shunt Feedback Circuit



Assume  $R_i$  very large

$$\beta_v = \frac{R_1}{R_1 + R_2}$$

$$V_{fb} = \frac{R_1}{R_1 + R_2} V_o = \beta_v V_o$$



## Series-shunt feedback

- Take some of the output voltage
- Feed it back in series with input

## Series-shunt feedback

- Input impedance will increase
- Output impedance will decrease
- Bandwidth will increase

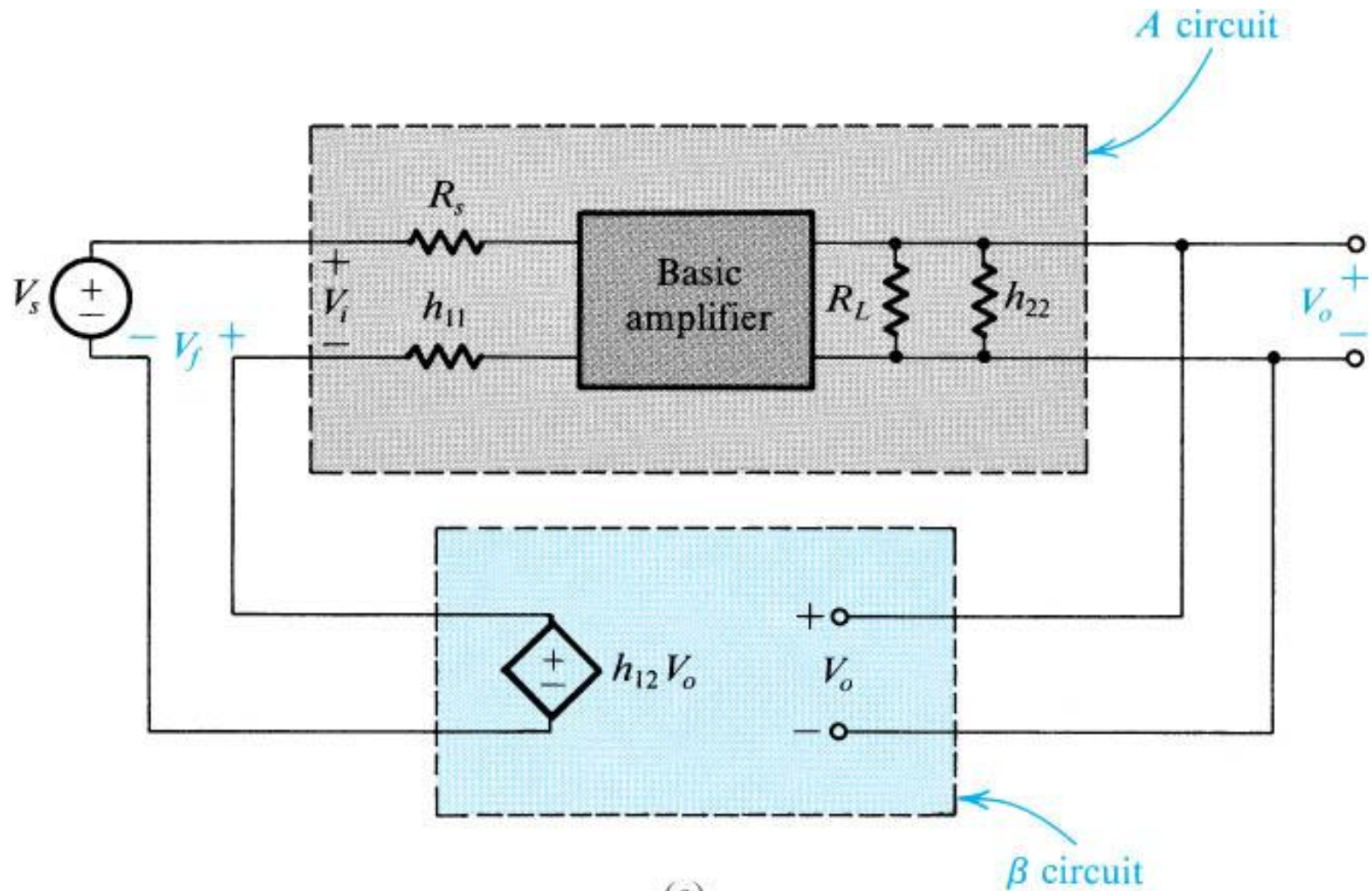
$$A_{vf} \cong \frac{1}{\beta_v}$$

$$\begin{aligned} R_{if} &= R_i (1 + \beta_v A_v) \\ &= R_i \left( 1 + A_v \frac{R_1}{R_1 + R_2} \right) \end{aligned}$$

$$\begin{aligned} A_{vf} &\cong \frac{R_1 + R_2}{R_1} \\ &= 1 + \frac{R_2}{R_1} \end{aligned}$$

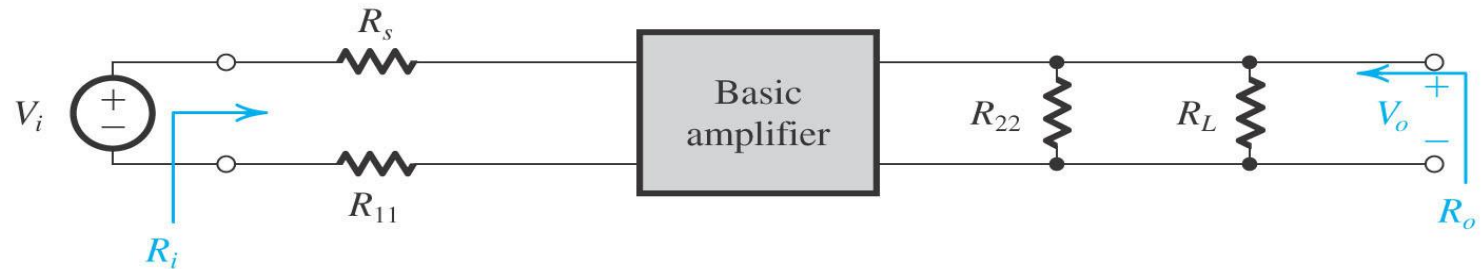
$$\begin{aligned} R_{of} &= R_o / (1 + \beta_v A_v) \\ &= R_o / \left( 1 + A_v \frac{R_1}{R_1 + R_2} \right) \end{aligned}$$

# Actual Series-Shunt Feedback

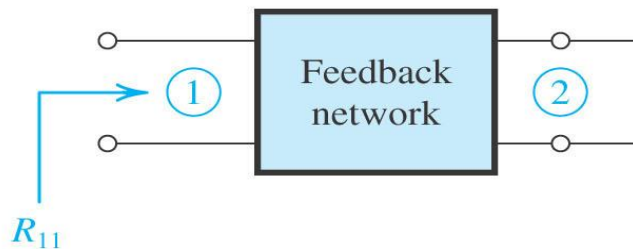


# Analysis Procedure – Rules to Determine Parameters

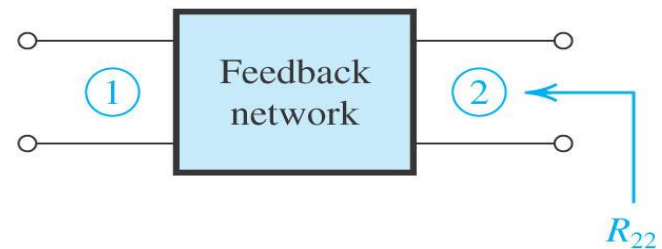
(a) The A circuit is



where  $R_{11}$  is obtained from



and  $R_{22}$  is obtained from



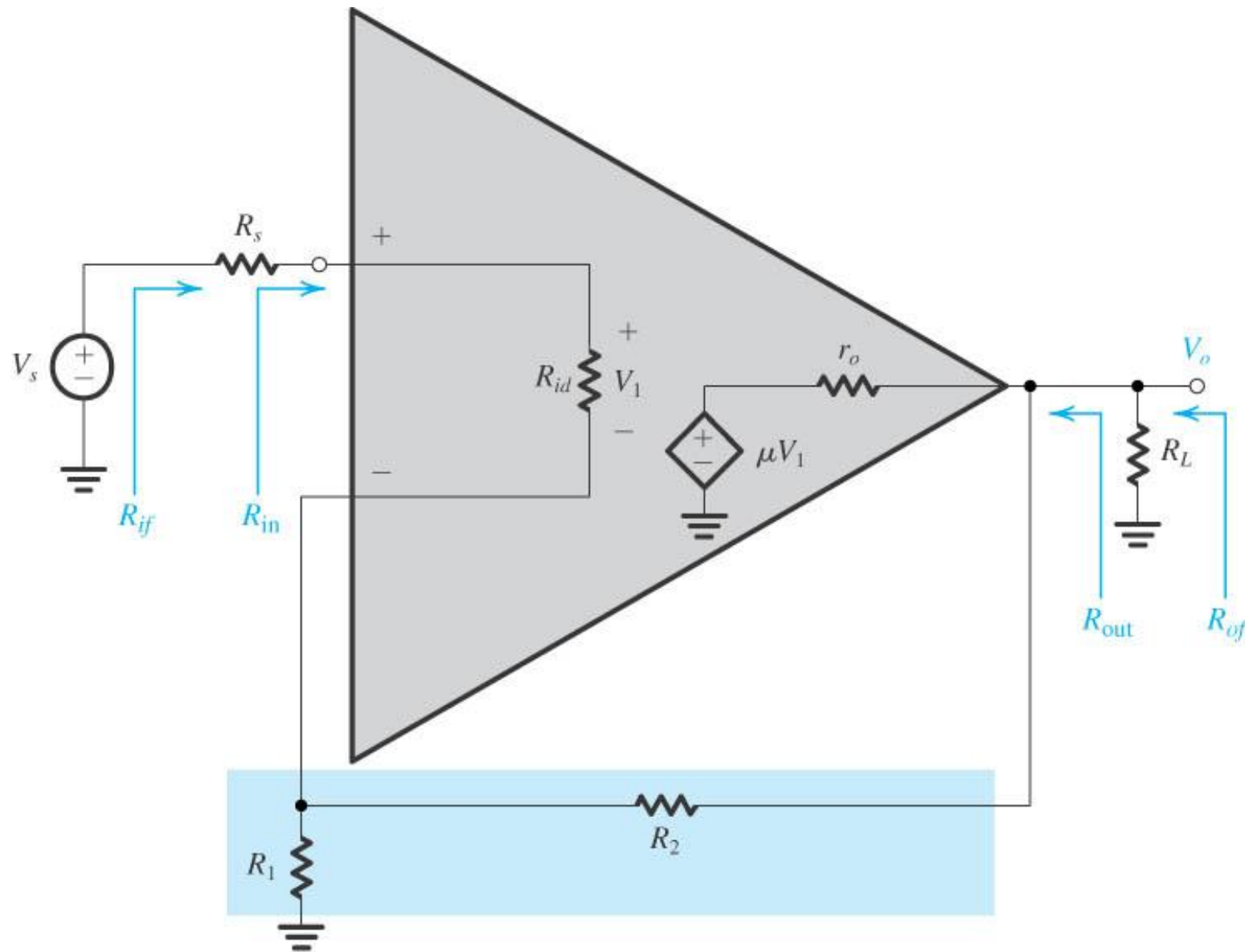
and the gain  $A$  is defined  $A \equiv \frac{V_o}{V_i}$

(b)  $\beta$  is obtained from



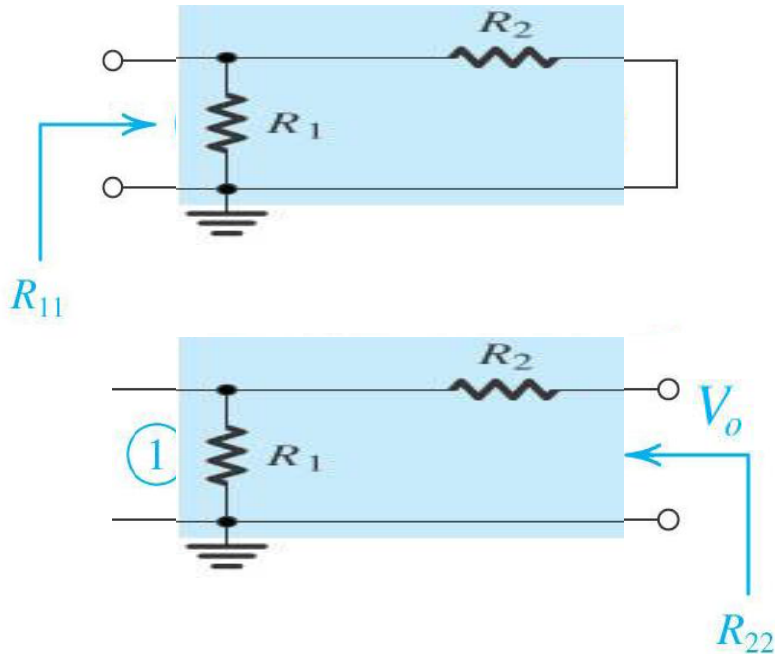
$$\beta \equiv \left. \frac{V_f}{V_o} \right|_{I_1 = 0}$$

## Example 8.1



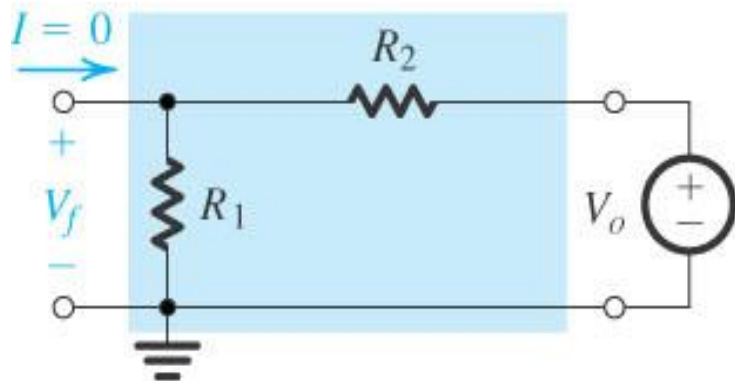
(a)

## Step 1 : Determine $\beta$ and the Loading Effects



$$R_{11} = \frac{V_f}{I_1} \Big|_{V_o=0} = R_1 // R_2$$

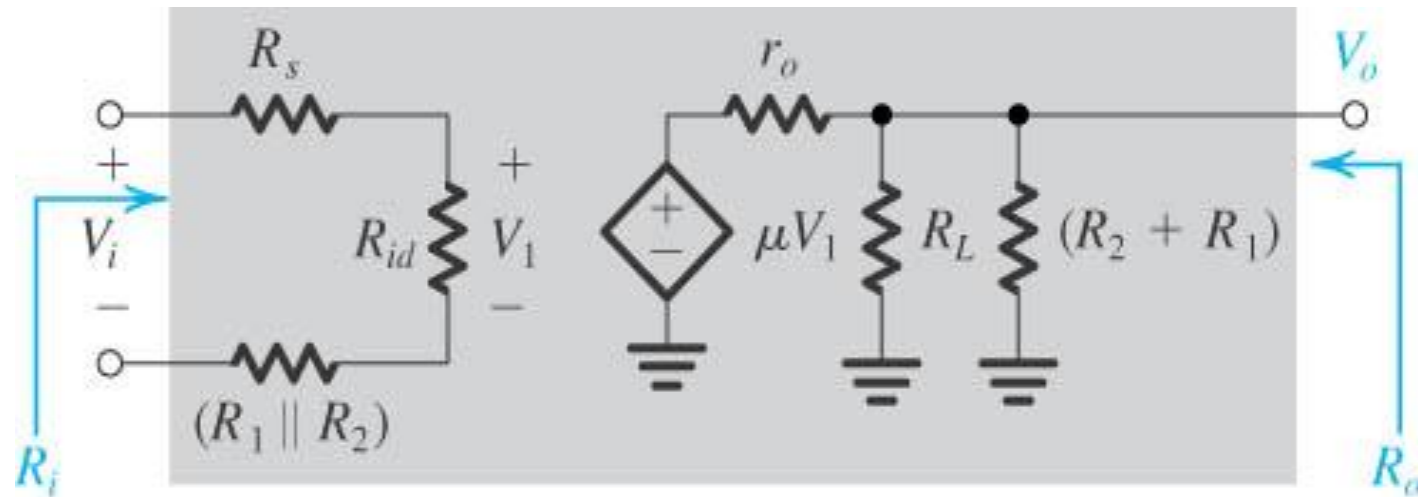
$$R_{22} = \frac{V_o}{I_o} \Big|_{I_1=0} = R_1 + R_2$$



$$\frac{V_f}{V_o} \Big|_{I_1=0} = \frac{R_1}{R_1 + R_2} = \beta$$

(c)

## Step 2 : Form the A-Circuit to Determine Gain and Resistances



(b)

$$R_{if} = (1 + \beta A)(R_s + R_{id} + R_{11}) = (1 + \beta A)(R_s + R_{id} + (R_1 \parallel R_2)) = R_s + R_{in}$$

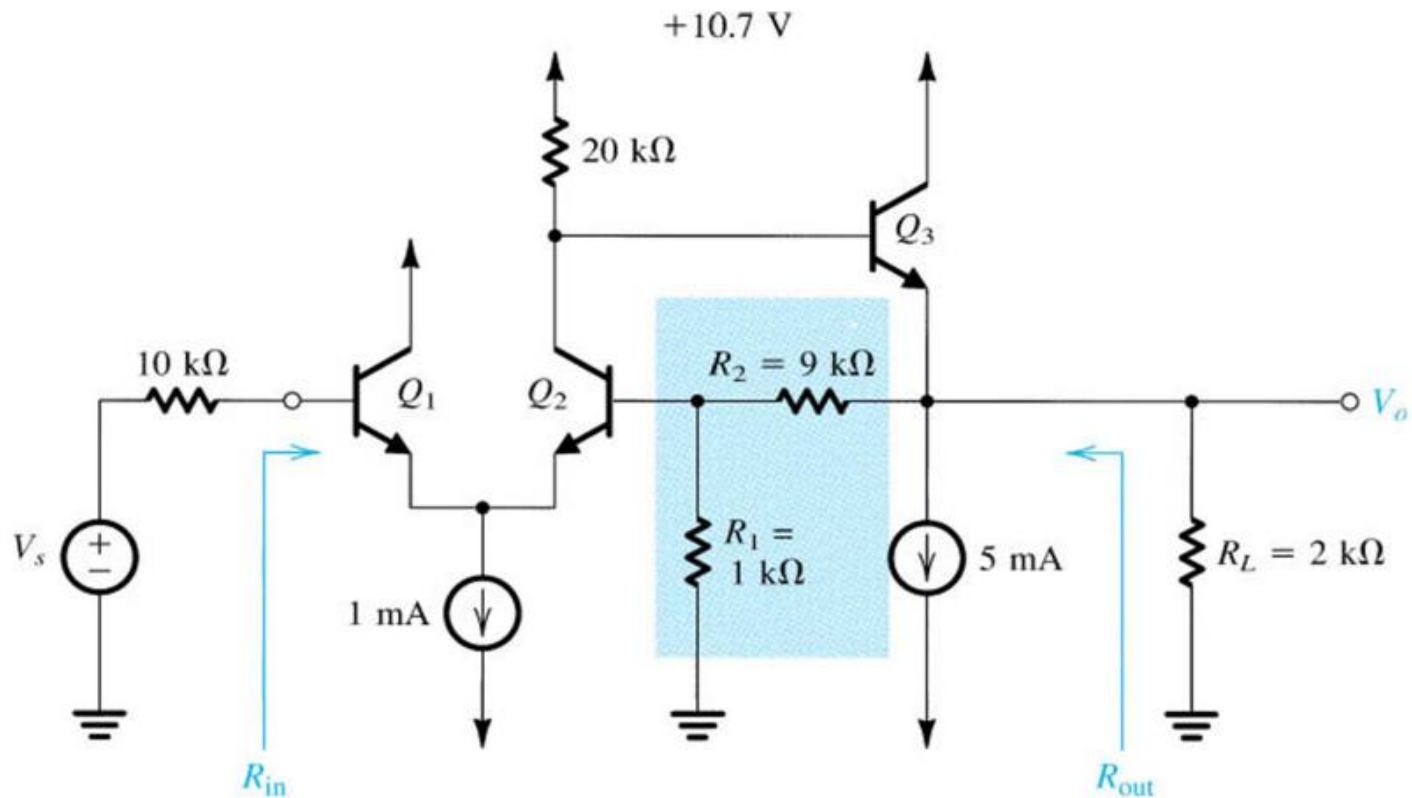
$$R_{in} = R_s - R_{if}$$

$$R_{of} = \frac{r_o \parallel R_{22} \parallel R_L}{(1 + \beta A)} = \frac{r_o \parallel (R_1 + R_2) \parallel R_L}{(1 + \beta A)} = R_{out} \parallel R_L$$

$$R_{out} \Rightarrow \text{find}$$

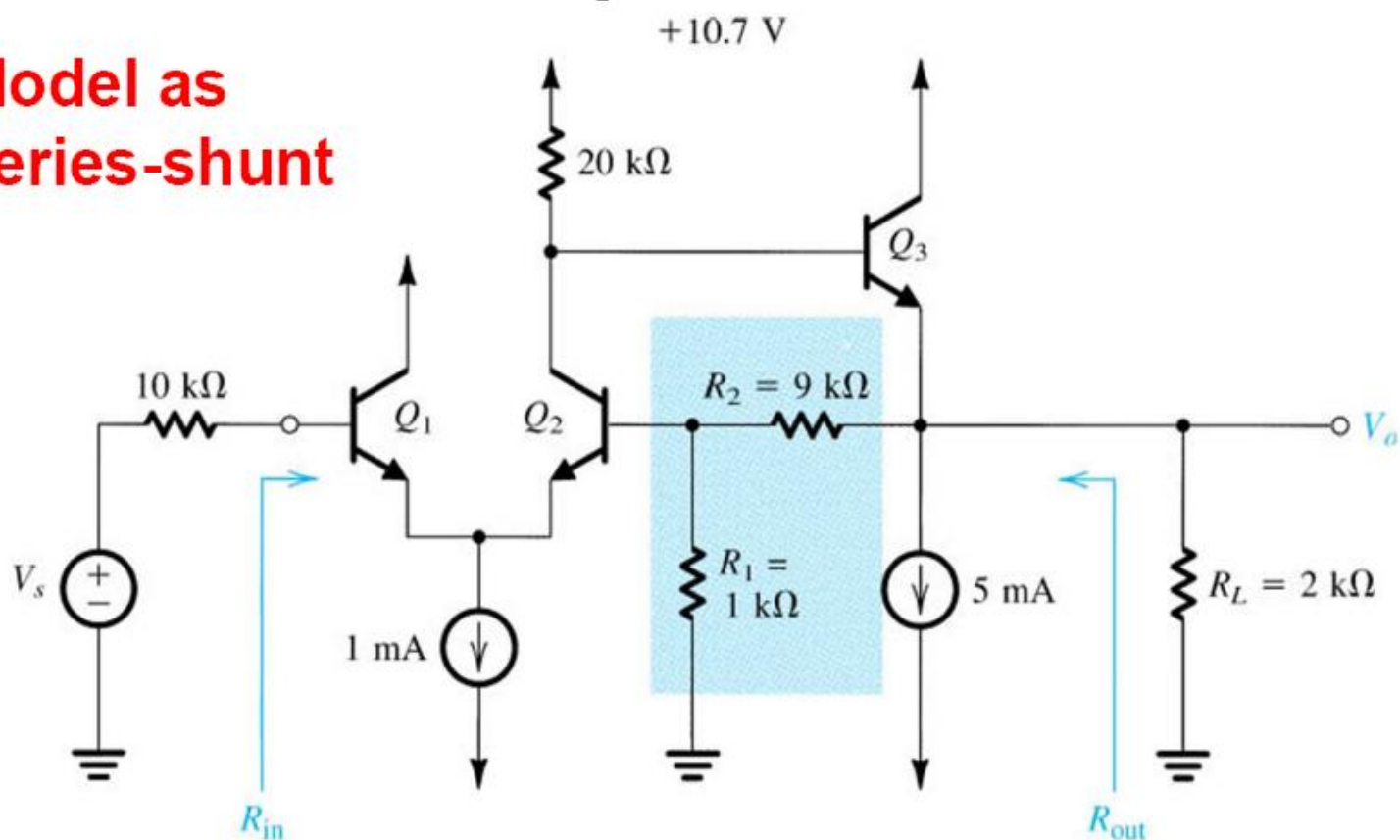
$$A_f = \frac{A}{1 + \beta A}, \quad A = \frac{V_o}{V_i} = \mu \frac{(R_L \parallel R_{22})}{(R_L \parallel R_{22}) + r_o} \frac{R_{id}}{R_{id} + R_s + R_{11}}$$

## Example - Feedback



Differential stage followed by an emitter follower, with series-shunt feedback supplied by the resistors  $R_1$  and  $R_2$ . Perform DC analysis and find  $A$ ,  $\beta$ ,  $A_f$ ,  $R_{in}$  and  $R_{out}$

**Model as  
series-shunt**



$$I_{E1} = I_{E2} = 0.5 \text{ mA}$$

$$V_{c2} = 10.7 - 0.5 \times 20 = +0.7 \text{ V}$$

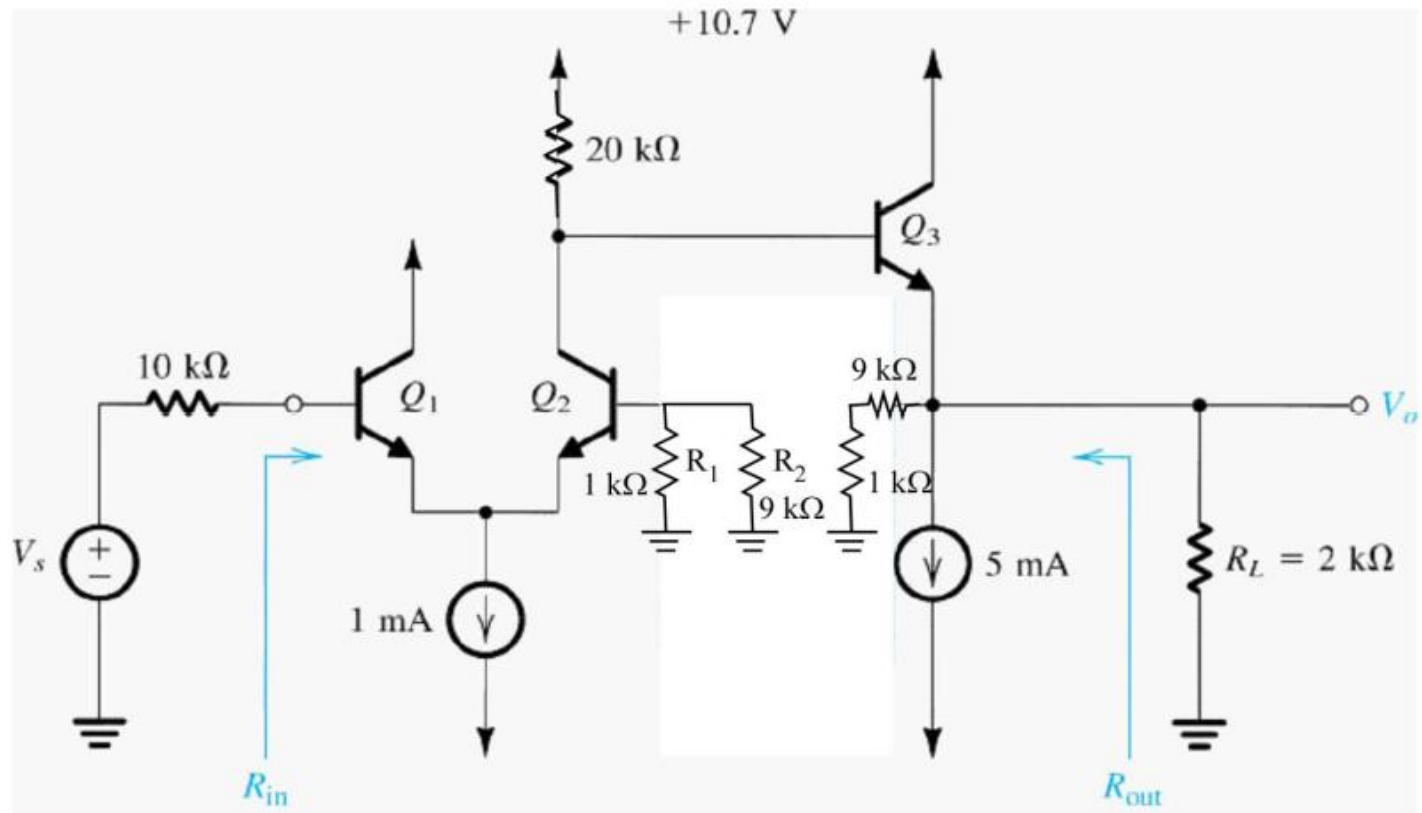
$$V_o = 0.7 - V_{BE3} = 0$$

$$I_{E3} = 5 \text{ mA}$$

$$r_{e1} = r_{e2} = \frac{V_T}{I_C} = 50 \Omega$$

$$r_{e3} = 5 \Omega$$

## A - Circuit



$$A = \frac{V_o}{V_s} = \frac{\left[ 20 \parallel (\beta_2 + 1)(r_{e3} + (2 \parallel 10)) \right]}{r_{e1} + r_{e1} + \frac{10}{\beta_1 + 1} + \frac{(1 \parallel 9)}{\beta_2 + 1}} \times \frac{(2 \parallel 10)}{r_{e3} + (2 \parallel 10)} = 85.7\text{ V/V}$$

## A - Circuit – cont'

$$R_i = R_s + (\beta + 1)(r_{e1} + r_{e2}) + R_E \parallel R_4$$

$$R_i = 10 + 101(50 + 50) + (1 \parallel 9) = 21 \text{ k}\Omega$$

$$R_o = 2 \parallel 10 \parallel \left[ r_{e3} + \frac{20}{\beta_2 + 1} \right] = 181 \Omega$$

## $\beta$ - Circuit

$$\beta = V_f' / V_o' = \frac{1}{9+1} = 0.1 V$$

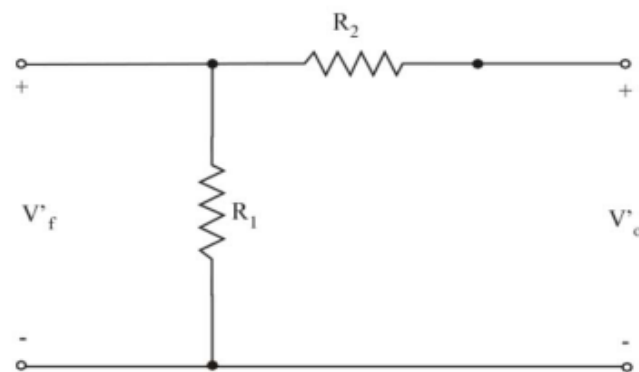
$$A_f = \frac{V_o}{V_s} = \frac{A}{1+A\beta} = \frac{85.7}{1+85.7 \times 0.1} = 8.96 V/V$$

$$R_{if} = R_1 (1+A\beta) = 21 \times 9.37 = 201 k\Omega$$

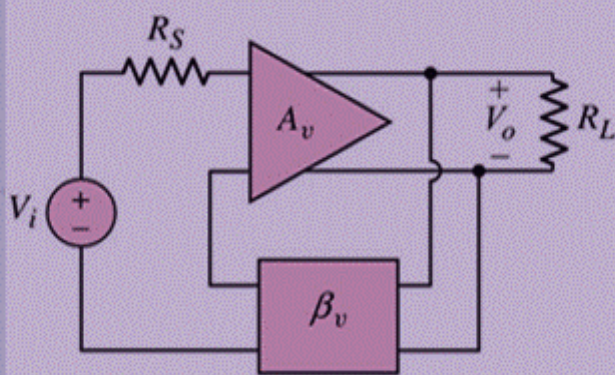
$$R_{IN} = R_{if} - R_s = 201 - 10 = 191 k\Omega$$

$$R_{of} = (R_{out} \parallel R_L) = \frac{R_o}{1+A\beta} = \frac{181}{9.57} = 18.8 \Omega$$

$$R_{out} = 19.1 \Omega$$

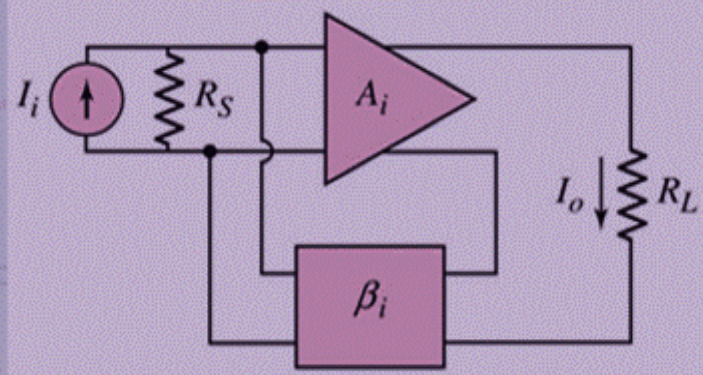


# Ideal Basic Feedback Configurations



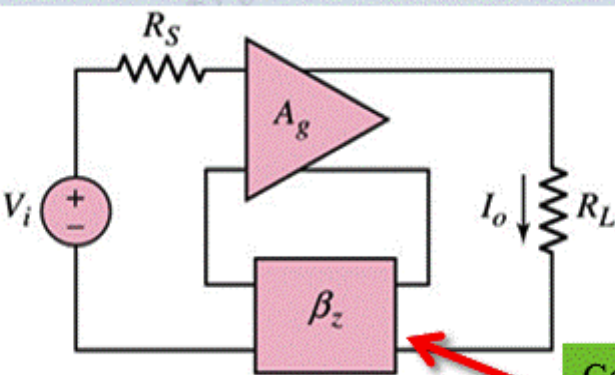
**Series-shunt**

Voltage Amplifier



**Shunt-series**

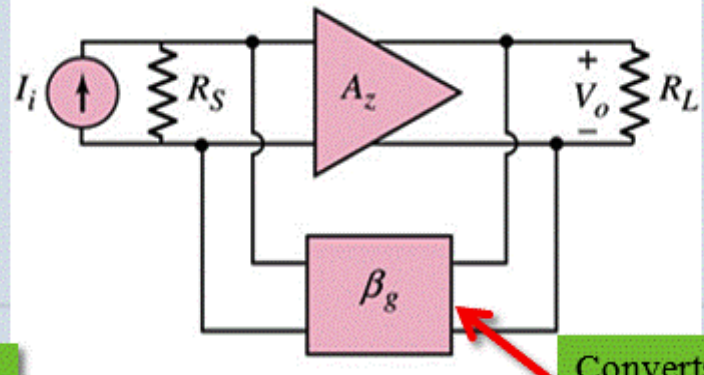
Current Amplifier



**Series-series**

Transconductance Amplifier  
(voltage in-current out)

Converts current  
to voltage

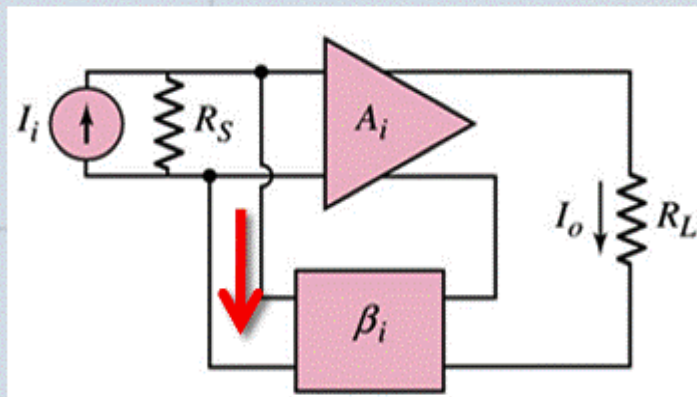


**Shunt-shunt**

Transresistance Amplifier  
(current in-voltage out)

Converts voltage  
to current

# Ideal Shunt-Series Feedback



**Shunt-series**

**Current Amplifier**

Sample output current and feed it back to input

Ideal: assume feedback network does not load output, so that  $I_o$  is unaffected

$$A_{if} = \frac{A_i}{1 + \beta_i A_i}$$

“Feedback” = “Subtract”,  
“Reduce”, “Steal From”

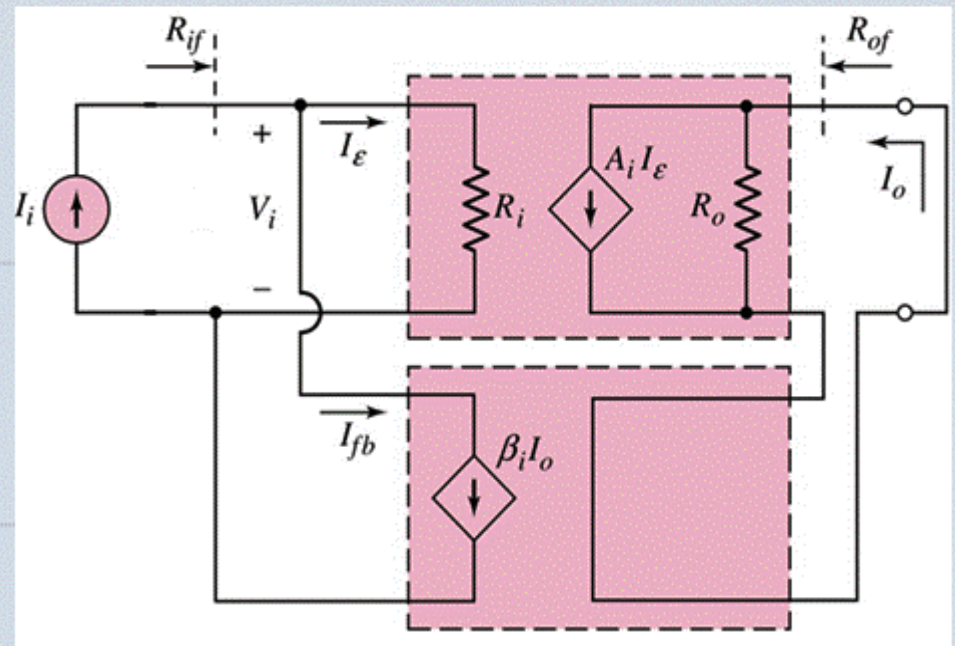
$$I_i = I_e + \beta I_o$$

$$= I_e + \beta (A_i I_e)$$

$$I_e = \frac{I_i}{(1 + \beta_i A_i)}$$

$$V_i = I_e R_i = \frac{I_i R_i}{(1 + \beta_i A_i)}$$

$$R_{if} = \frac{V_i}{I_i} = \frac{R_i}{(1 + \beta_i A_i)}$$



# Ideal Shunt-Series Feedback

How do we determine output resistance?

1. Turn off independent sources
2. Add test current  $I_x$  output
3. See what test current  $V_x$  results
4. Determine  $V_x/I_x$

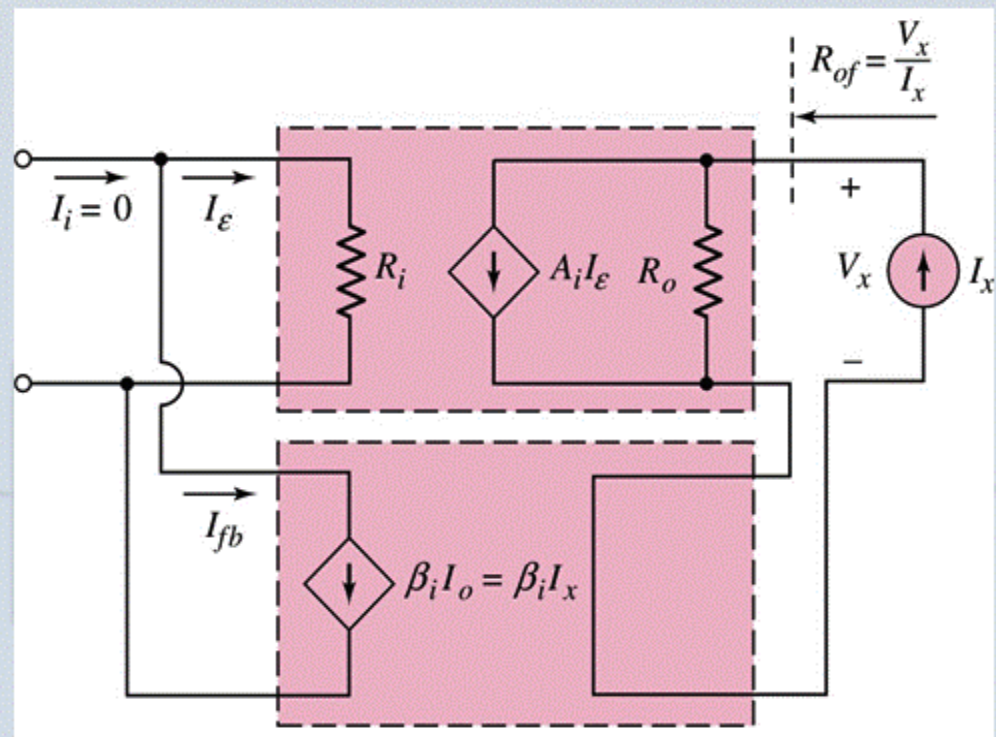
$$I_e = -\beta I_x$$

$$V_x = (I_x - A_i I_e) R_o$$

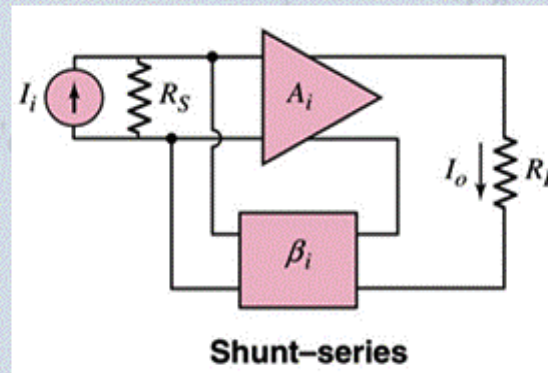
$$= (I_x - A_i (-\beta I_x)) R_o$$

$$= I_x (1 + \beta A_i) R_o$$

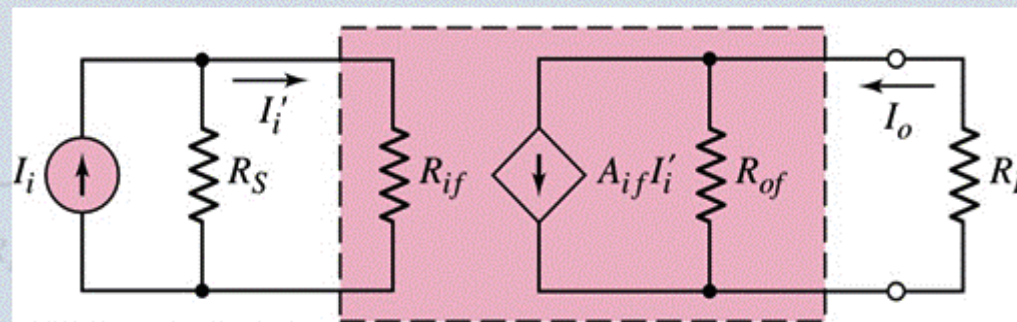
$$R_{of} = \frac{V_x}{I_x} = (1 + \beta A_i) R_o$$



# Equivalent Circuit: Shunt-Series Feedback Circuit



Current Amplifier

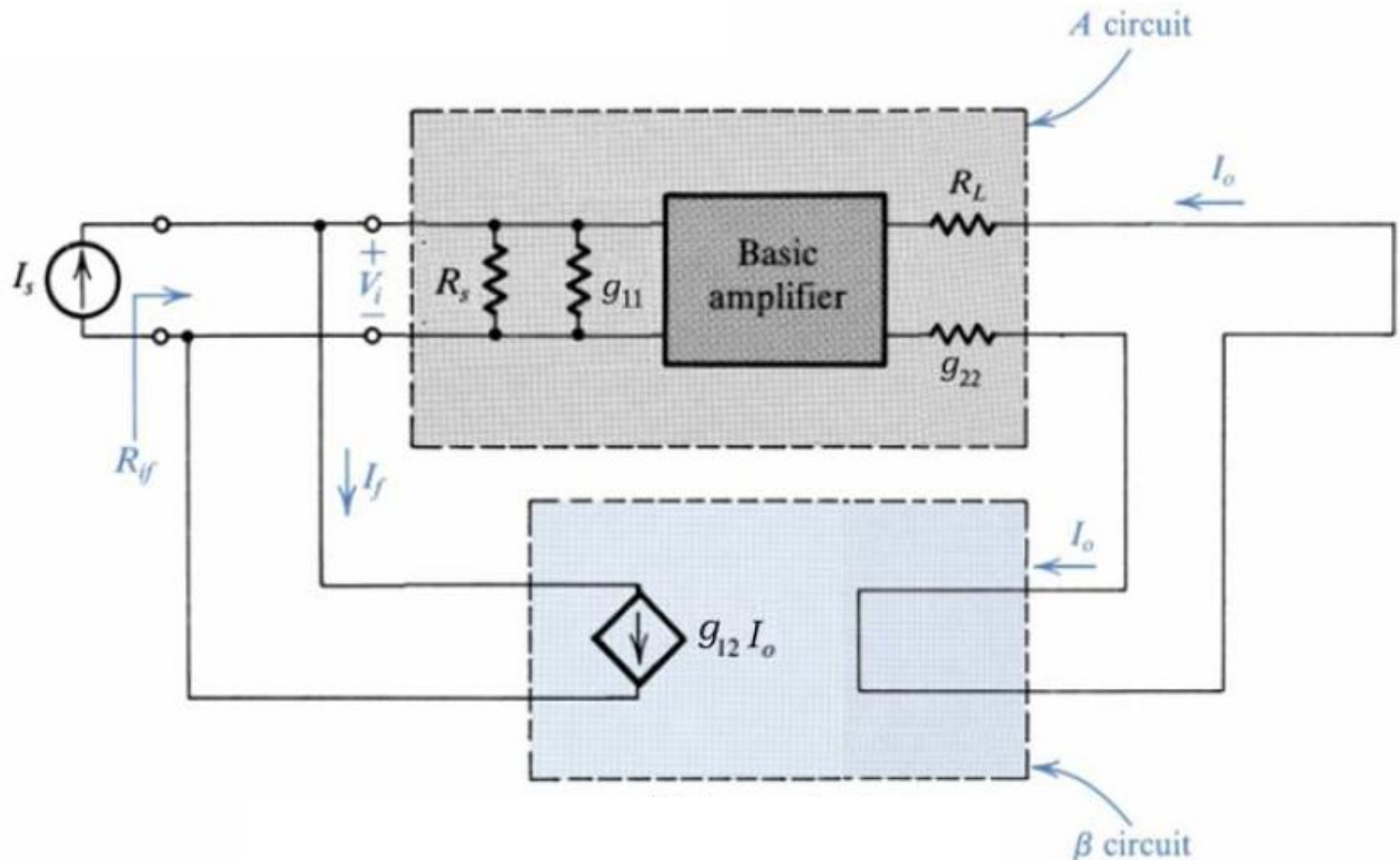


$$R_{if} = \frac{R_i}{(1 + \beta_i A_i)}$$

$$A_{if} = \frac{A_i}{1 + \beta_i A_i}$$

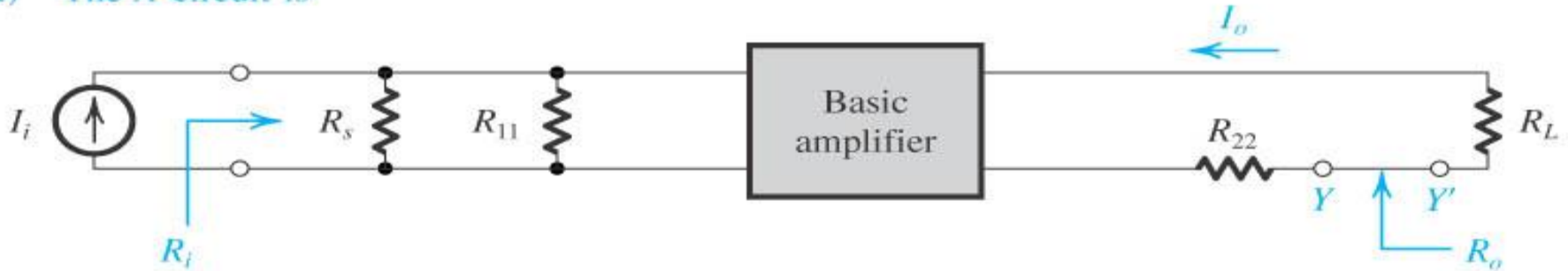
$$R_{of} = \frac{V_x}{I_x} = (1 + \beta_i A_i) R_o$$

# Actual Shunt-Series Feedback

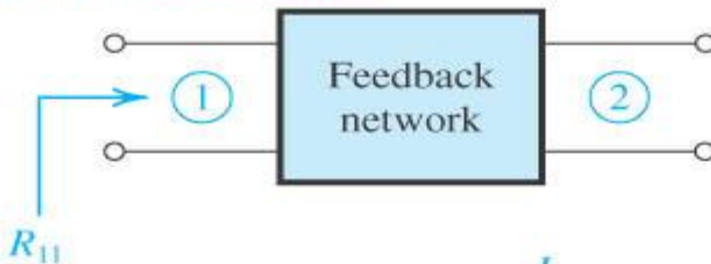


# Analysis Procedure – Rules to Determine Parameters

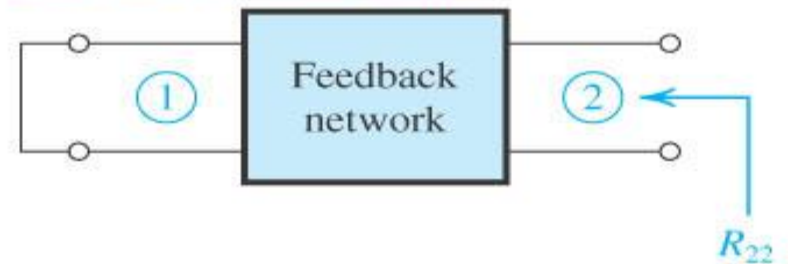
(a) The  $A$  circuit is



where  $R_{11}$  is obtained from

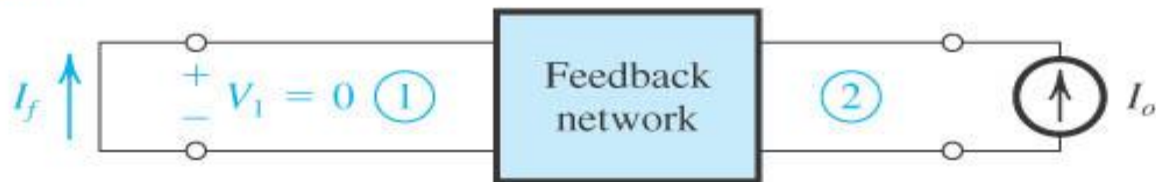


and  $R_{22}$  is obtained from



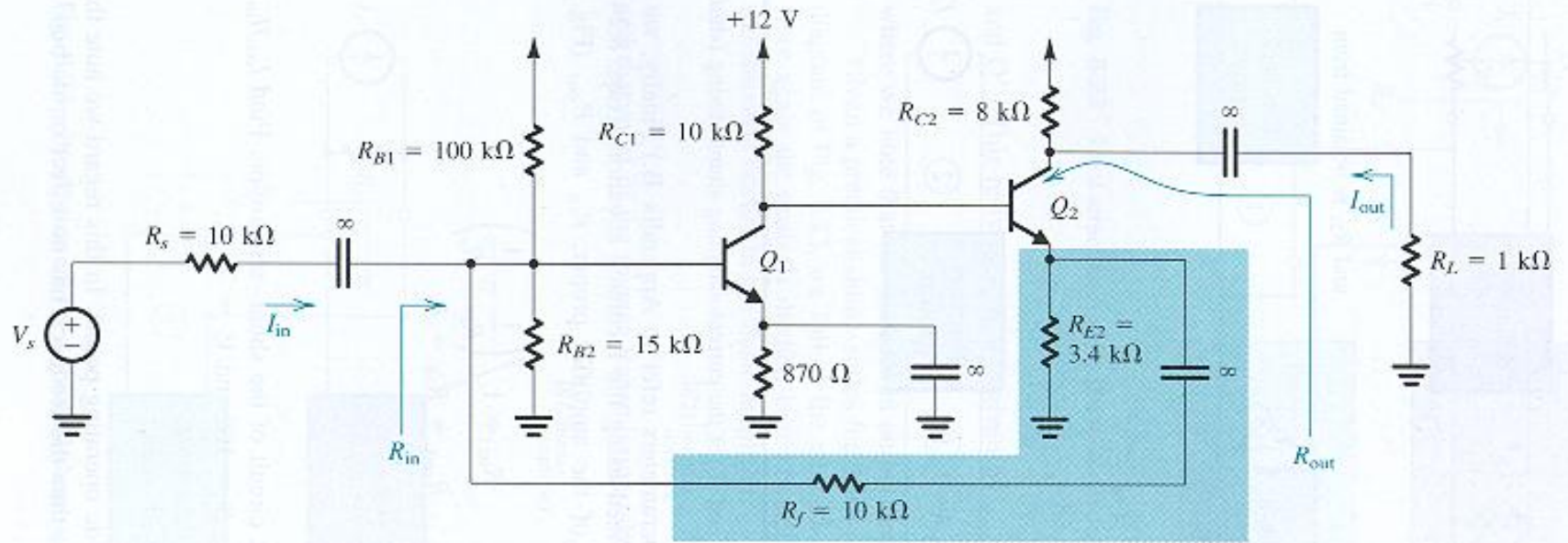
and the gain  $A$  is defined as  $A \equiv \frac{I_o}{I_i}$

(b)  $\beta$  is obtained from



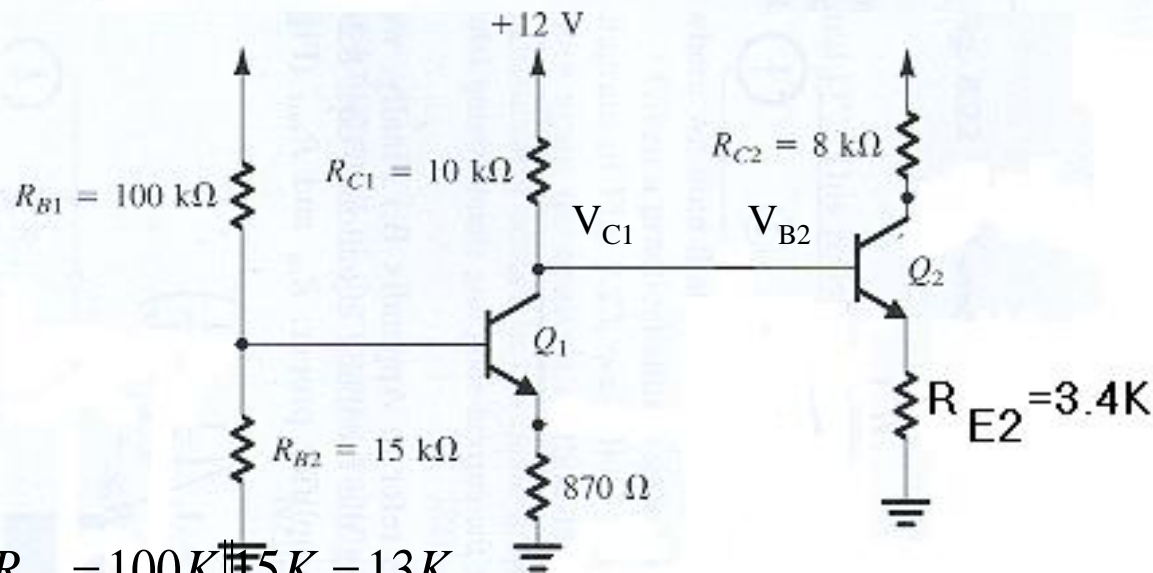
$$\beta \equiv \left. \frac{I_f}{I_o} \right|_{V_1 = 0}$$

# Example - Shunt-Series Feedback Amplifier



- Two stage [CE+CE] amplifier
- Transistor parameters Given:  $\beta=100, r_x=0$
- Input and output coupling and emitter bypass capacitors, but direct coupling between stages
- Capacitor in feedback connection removes  $R_f$  from DC bias
- DC bias of two stages is coupled (bias of one affects the other)

# DC Bias Analysis



Given:

$$\beta_1 = \beta_2 = 100$$

$$r_{x1} = r_{x2} = 0$$

$$R_{B1} \parallel R_{B2} = 100K \parallel 15K = 13K$$

$$\frac{R_{B2}}{R_{B1} + R_{B2}} 12V = \frac{15K}{15K + 100K} 12V = 1.6V$$

$$\frac{V_{TH1} - V_{BE1}}{R_{TH1} + (\beta + 1)R_{E1}} = \frac{1.6V - 0.7V}{13K + (101)0.87K} = 8.7 \mu A$$

$$I_{B1} = 100(8.7 \mu A) = 0.87 \text{ mA} \quad (\text{neglecting } I_{B2})$$

$$g_{m1} = \frac{0.87 \text{ mA}}{0.0256 \text{ V}} = 34 \text{ mA/V}$$

$$r_{\pi1} = \frac{\beta}{g_{m1}} = \frac{100}{34 \text{ mA/V}} = 2.9K$$

$$V_{C1} = 12 \text{ V} - I_{C1}R_{C1} = 12 \text{ V} - (0.87 \text{ mA})10K = 3.3 \text{ V}$$

$$V_{B2} = V_{C1} = V_{BE2} + I_{E2}R_{E2} = 0.7V + (\beta + 1)I_{B2}R_{E2}$$

$$I_{B2} = \frac{3.3V - 0.7V}{(\beta + 1)R_{E2}} = \frac{2.6V}{101(3.4K)} = 7.6 \mu A \quad (<< I_{C1} = 870 \mu A)$$

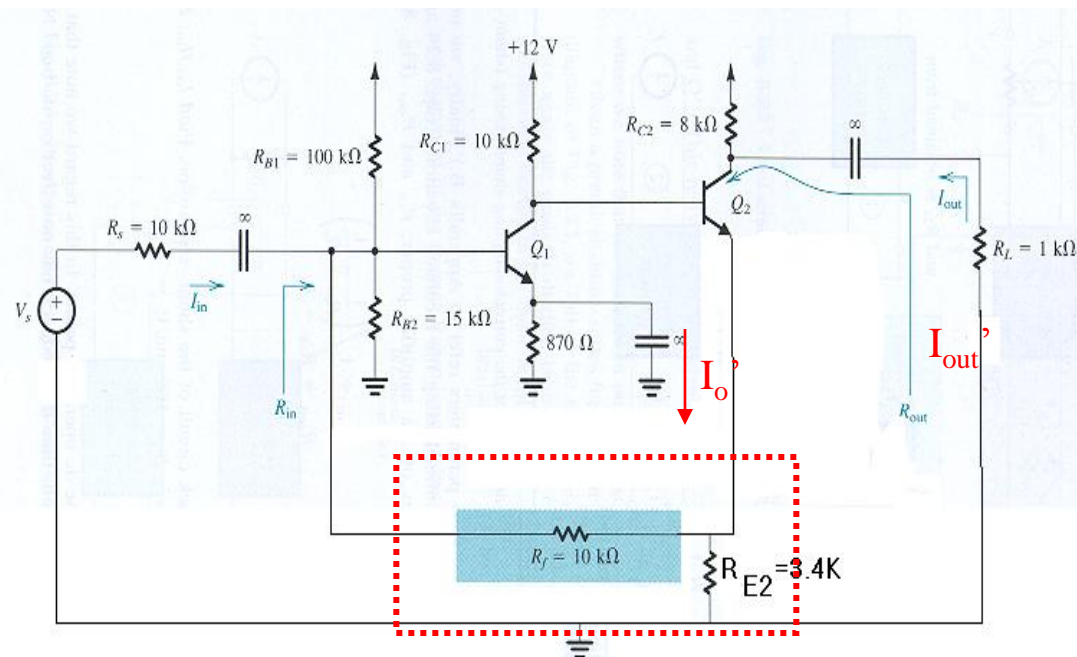
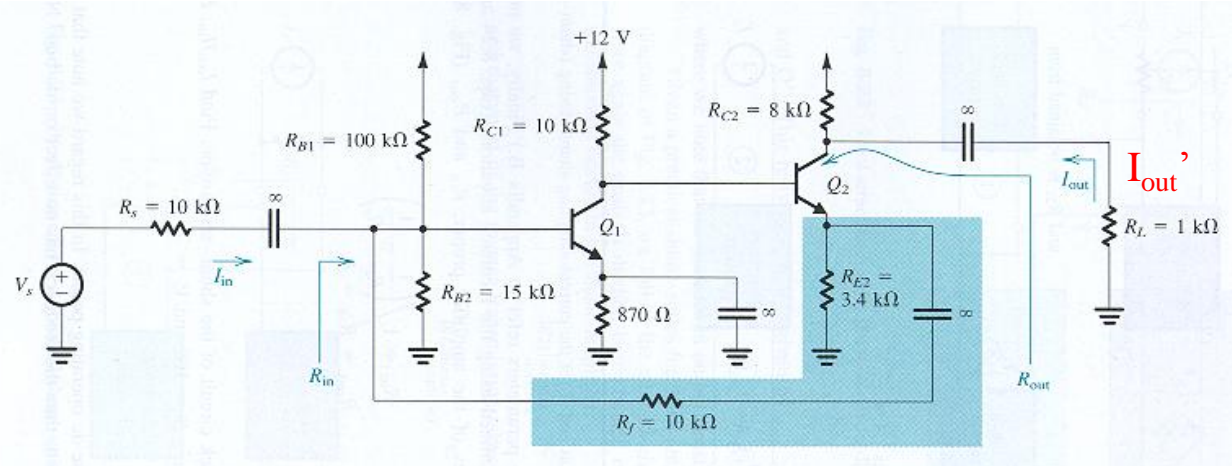
$$I_{C2} = \beta I_{B2} = 100(7.6 \mu A) = 0.76 \text{ mA}$$

$$g_{m2} = \frac{I_{C2}}{V_T} = \frac{0.76 \text{ mA}}{0.0256V} = 30 \text{ mA/V}$$

$$r_{\pi2} = \frac{\beta}{g_{m2}} = \frac{100}{30 \text{ mA/V}} = 3.3K$$

# Example - Shunt-Series Feedback Amplifier

- Redraw circuit to show
  - Feedback circuit
  - Type of output sampling (current in this case =  $I_o$ )
  - Type of feedback signal to input (current in this case =  $I_f$ )



# Example - Shunt-Series Feedback Amplifier

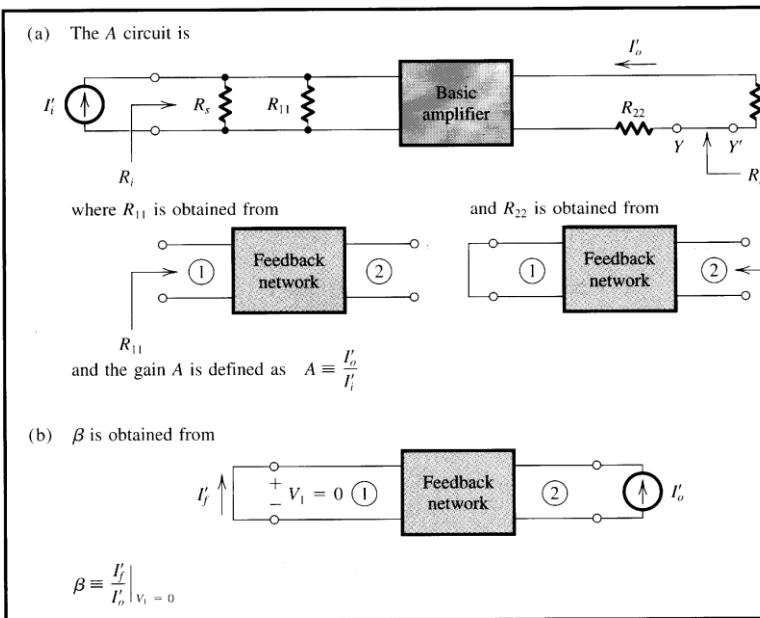
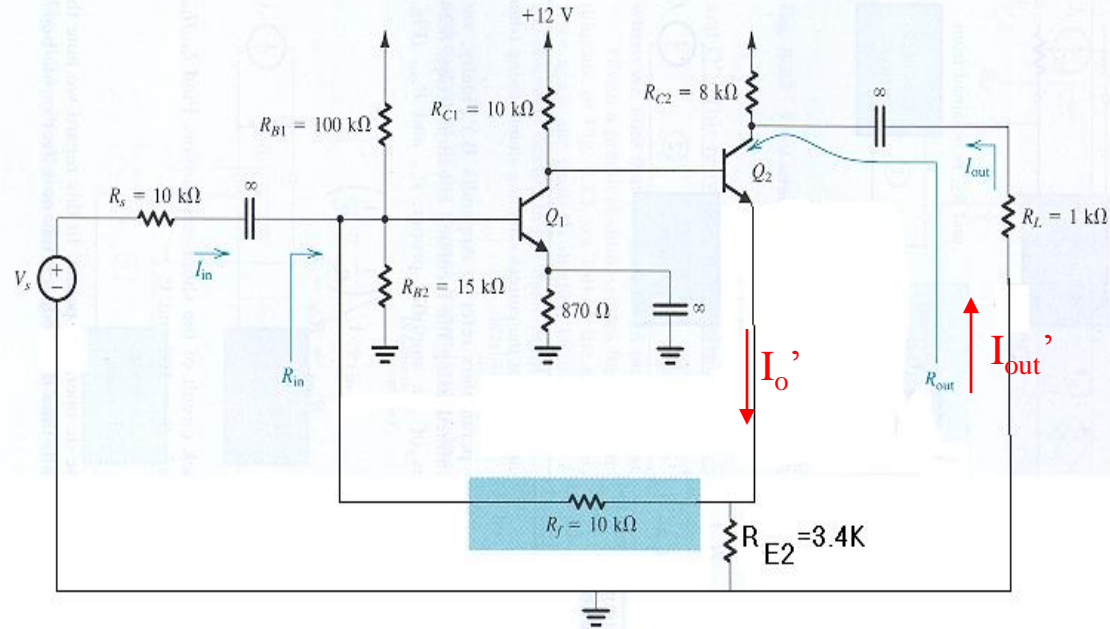
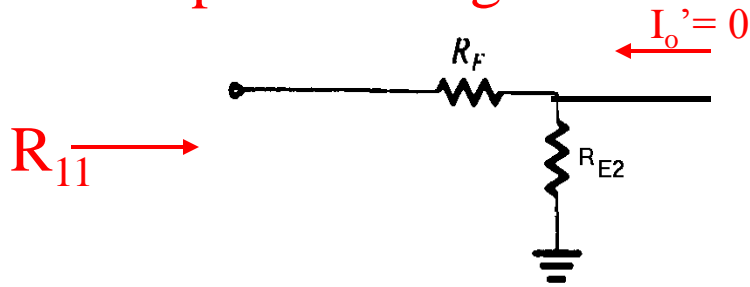


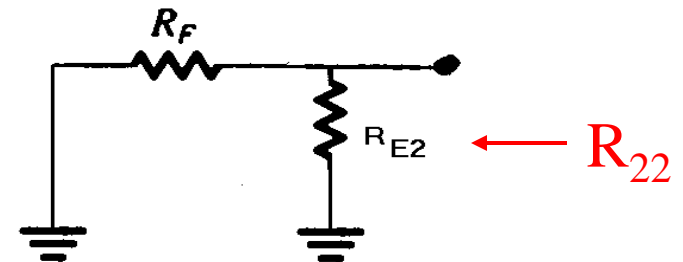
Fig. 8.24 Finding the A circuit and  $\beta$  for the current-sampling shunt-mixing (shunt-series) c



## Input Loading Effects



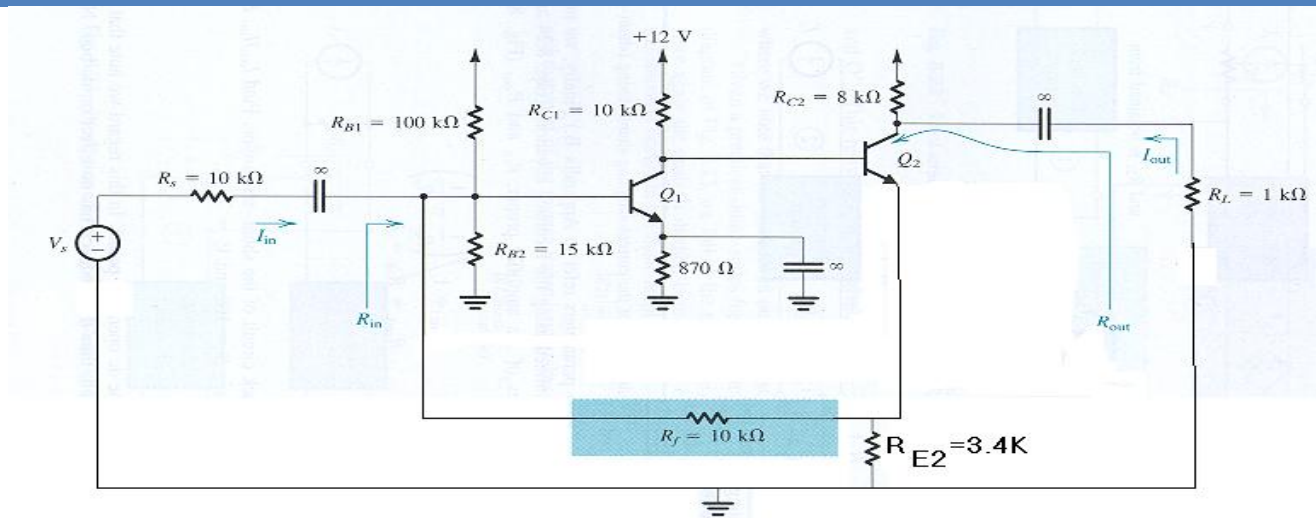
## Output Loading Effects



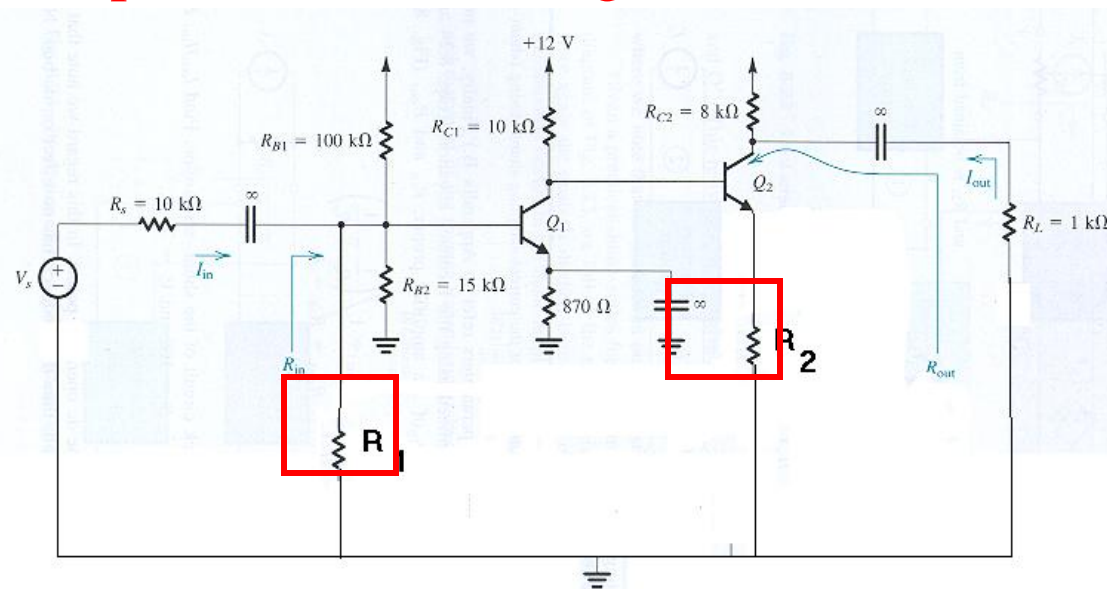
$$R_{22} = R_F \parallel R_{E2} = 10K \parallel 3.4K = 2.5K$$

$$R_{11} = R_F + R_1 = 10K + 3.4K = 13.4K$$

## Example - Shunt-Series Feedback Amplifier

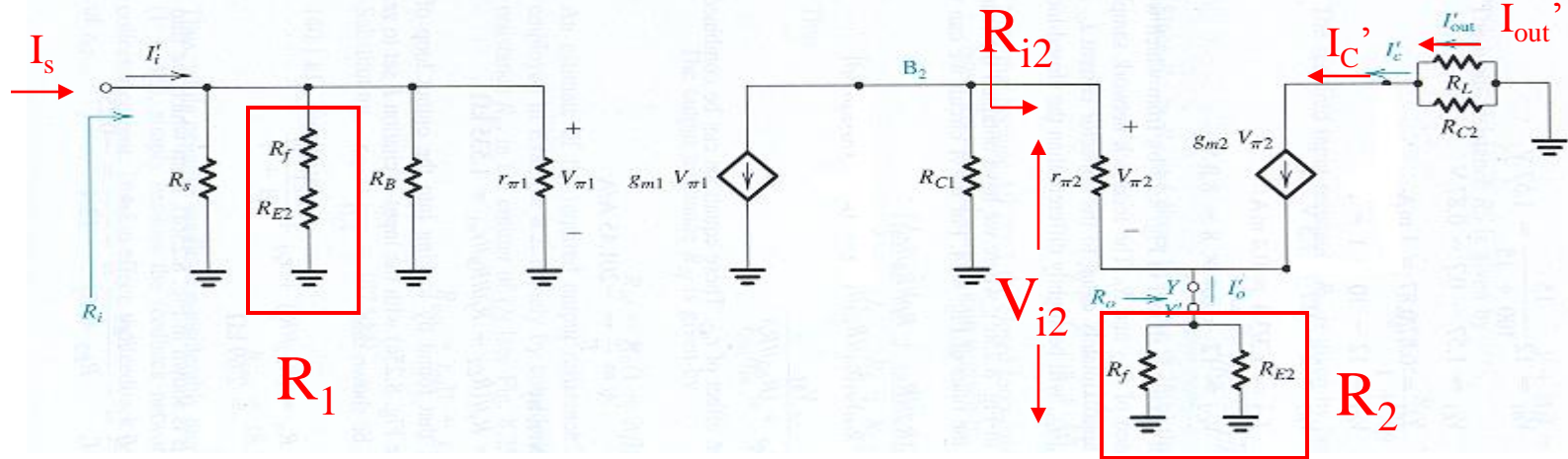


Amplifier with Loading Effects but Without Feedback



# Example - Shunt-Series Feedback Amplifier

## Midband Gain Analysis



$$A_{Io} = \frac{I_{out}'}{I_s} = \left( \frac{I_{out}'}{I_c'} \right) \left( \frac{I_c'}{V_{\pi 2}} \right) \left( \frac{V_{\pi 2}}{V_{i2}} \right) \left( \frac{V_{i2}}{V_{\pi 1}} \right) \left( \frac{V_{\pi 1}}{I_s} \right)$$

$$\frac{I_{out}'}{I_c'} = \frac{R_{C2}}{R_{C2} + R_L} = \frac{8K}{8K + 1K} = 0.89$$

$$\frac{I_c'}{V_{\pi 2}} = \frac{g_{m2} V_{\pi 2}}{V_{\pi 2}} = g_{m2} = 30 \text{ mA/V}$$

$$\frac{V_{\pi 2}}{V_{i2}} = \frac{I_{\pi 2} r_{\pi 2}}{I_{\pi 2} r_{\pi 2} + I_{\pi 2} (1 + g_{m2} r_{\pi 2}) R_2} = \frac{r_{\pi 2}}{R_{i2}} = \frac{r_{\pi 2}}{r_{\pi 2} + (1 + g_{m2} r_{\pi 2}) R_2} = \frac{3.3K}{3.3K + 101(2.5K)} = 0.013$$

$$\frac{V_{i2}}{V_{\pi 1}} = -g_{m1} R_{C1} \parallel R_{i2} = -g_{m1} (R_{C1} \parallel [r_{\pi 2} + (1 + g_{m2} r_{\pi 2}) R_2]) = -34 \text{ mA/V} (10K \parallel [3.3K + 101(2.5K)]) = -327$$

$$\frac{V_{\pi 1}}{I_s} = (R_S \parallel R_1 \parallel r_{\pi 1} \parallel R_{B1}) = (10K \parallel 13.4K \parallel 2.9K \parallel 13K) = 1.7K$$

$$A_{Io} = \frac{I_{out}'}{I_s} = (0.89)(30 \text{ mA/V})(0.013)(-327)(1.7K) = -193$$

# Midband Gain with Feedback

- Determine the feedback factor  $\beta_f$

$$\beta_f = \frac{X_f}{X_o} = \frac{I_f'}{I_o'} = \frac{-R_{E2}}{(R_{E2} + R_f)} = \frac{-3.4K}{3.4K + 10K} = -0.25$$

- Calculate gain with feedback  $A_{If0}$

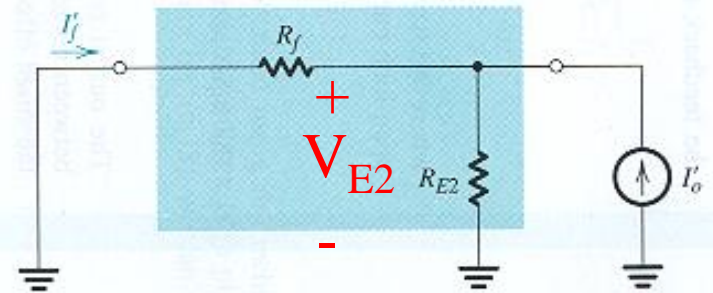
$$\beta_f A_{Io} = -193(-0.25) = 48$$

$$A_{If0} = \frac{A_{Io}}{1 + \beta_f A_{Io}} = \frac{-193}{1 + 48} = -3.9$$

$$A_{If0}(dB) = 20 \log 3.9 = 11.8 \text{ dB}$$

- Note

- $\beta_f < 0$  and  $A_{Io} < 0$
- $\beta_f A_{Io} > 0$  as necessary for negative feedback and dimensionless
- $\beta_f A_{Io}$  is large so there is significant feedback.
- Can change  $\beta_f$  and the amount of feedback by changing  $R_f$ .
- Gain is determined by feedback resistance



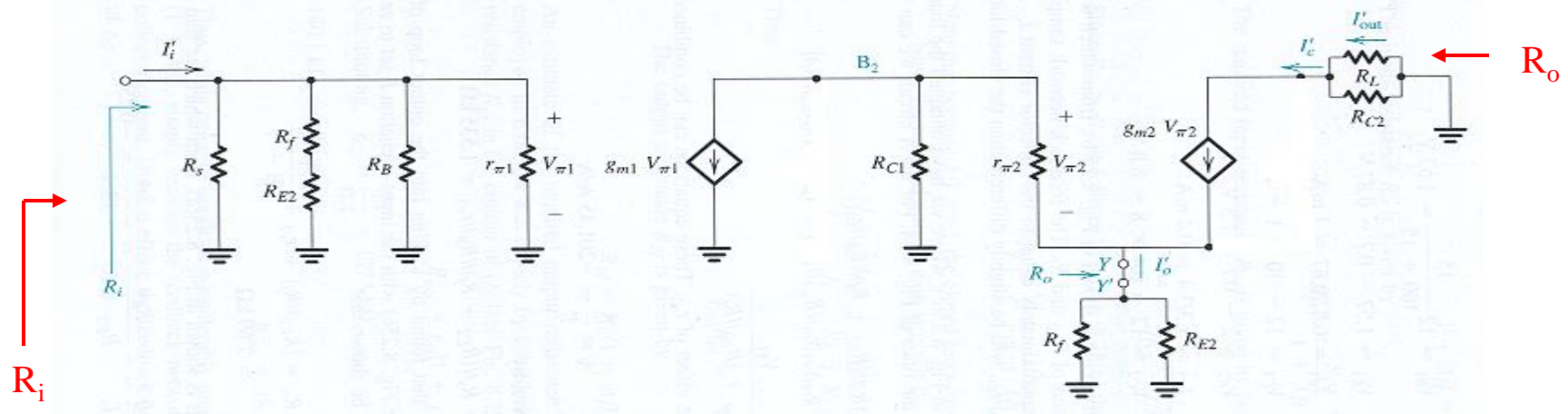
$$V_{E2} = -I_f' R_f = (I_o' + I_f') R_{E2}$$

$$-I_f' (R_f + R_{E2}) = I_o' R_{E2}$$

$$\frac{I_f'}{I_o'} = \frac{-R_{E2}}{R_f + R_{E2}}$$

$$A_{If0} \approx \frac{1}{\beta_f} = - \frac{R_{E2} + R_f}{R_{E2}} = -4.0$$

# Input and Output Resistances with Feedback



- Determine input  $R_i$  and output  $R_o$  resistances with loading effects of feedback network.

$$R_i = R_S \parallel R_1 \parallel R_{B1} \parallel r_{\pi 1} = 10K \parallel 13.4K \parallel 13K \parallel 2.9K = 1.7K$$

$$R_o = R_{C2} \parallel R_L + \infty = \infty$$

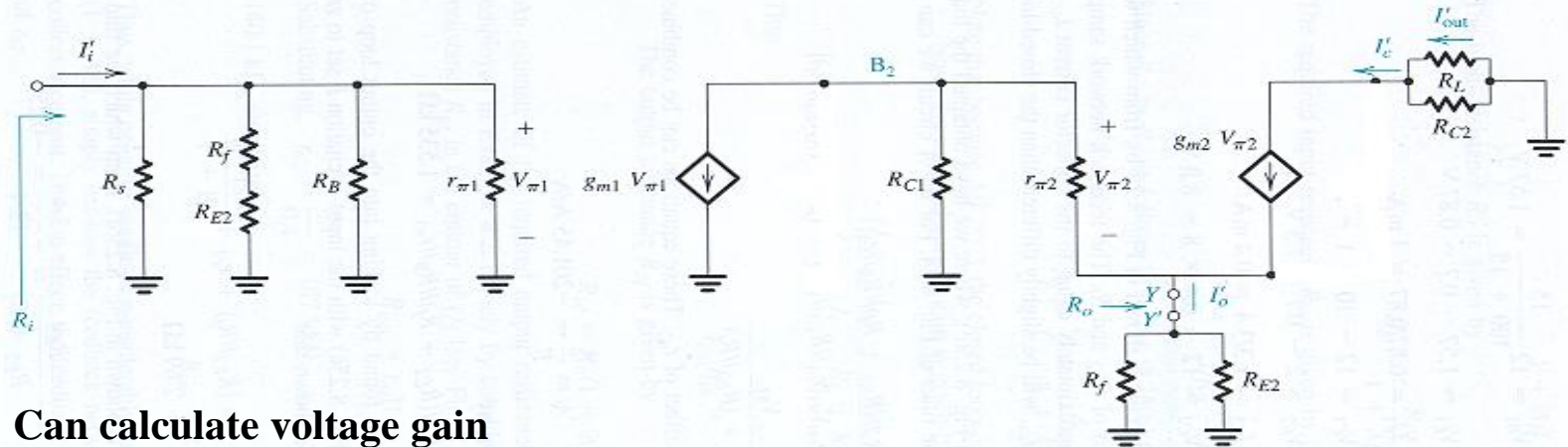
- Calculate input  $R_{if}$  and output  $R_{of}$  resistances for the complete feedback amplifier.

$$R_{if} = \frac{R_i}{(1 + \beta_f A_{Io})}$$

$$= \frac{1.7K}{49} = 0.035K$$

$$R_{of} = R_o (1 + \beta_f A_{Io}) = \infty(49) = \infty$$

# Voltage Gain for Current Gain Feedback Amplifier



- **Can calculate voltage gain**

$$A_{Vfo} = \left( \frac{V_o}{V_s} \right)_f = \left( \frac{-I_{out}' R_L}{I_s R_s} \right)_f = \frac{-R_L}{R_s} \left( \frac{I_{out}'}{I_s} \right)_f = \frac{-R_L A_{If_o}}{R_s} = \frac{-1K}{10K} (-4.2) = +0.42 \text{ V/V}$$

$$A_{Vfo}(\text{dB}) = 20 \log(0.42) = -7.5 \text{ dB}$$

- **Note - can't calculate the voltage gain as follows:**

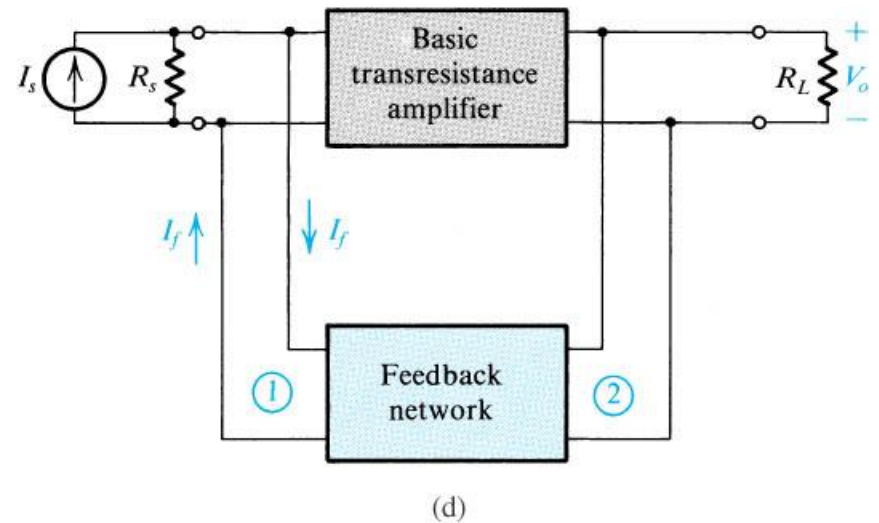
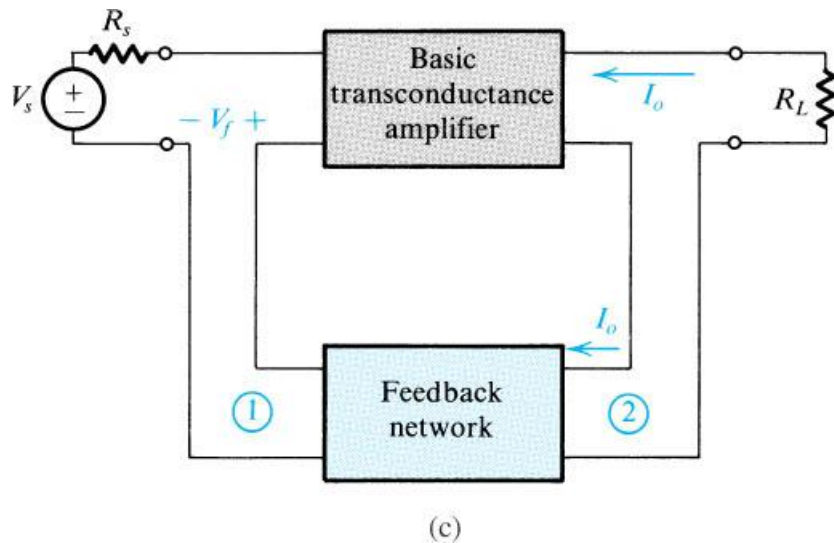
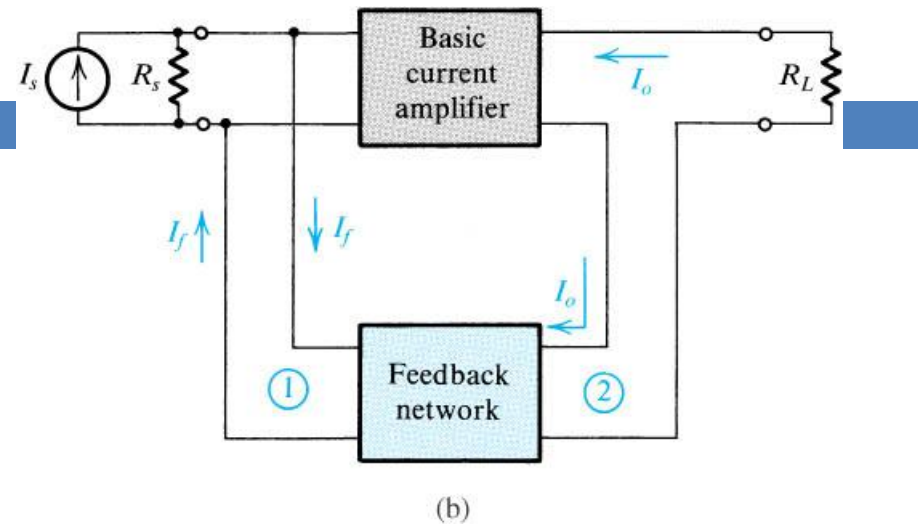
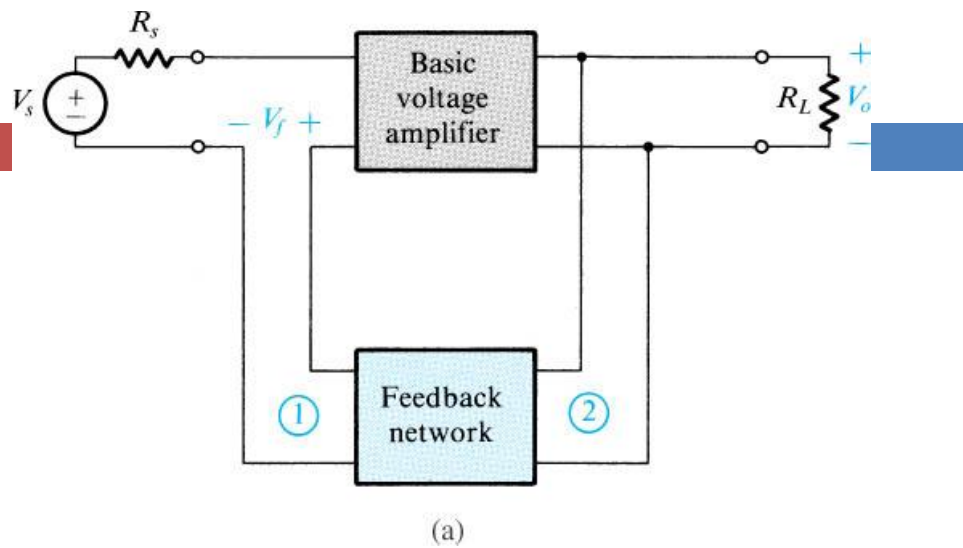
$$\text{Assume } A_{Vfo} = \frac{A_{Vo}}{1 + \beta_f A_{Vo}}$$

$$\text{Find } A_{Vo} = \frac{V_o}{V_s} = \frac{-I_o R_L}{I_s R_s} = \frac{-A_{Io} R_L}{R_s} = \frac{-(-193)(1K)}{10K} = +19.3 \text{ V/V}$$

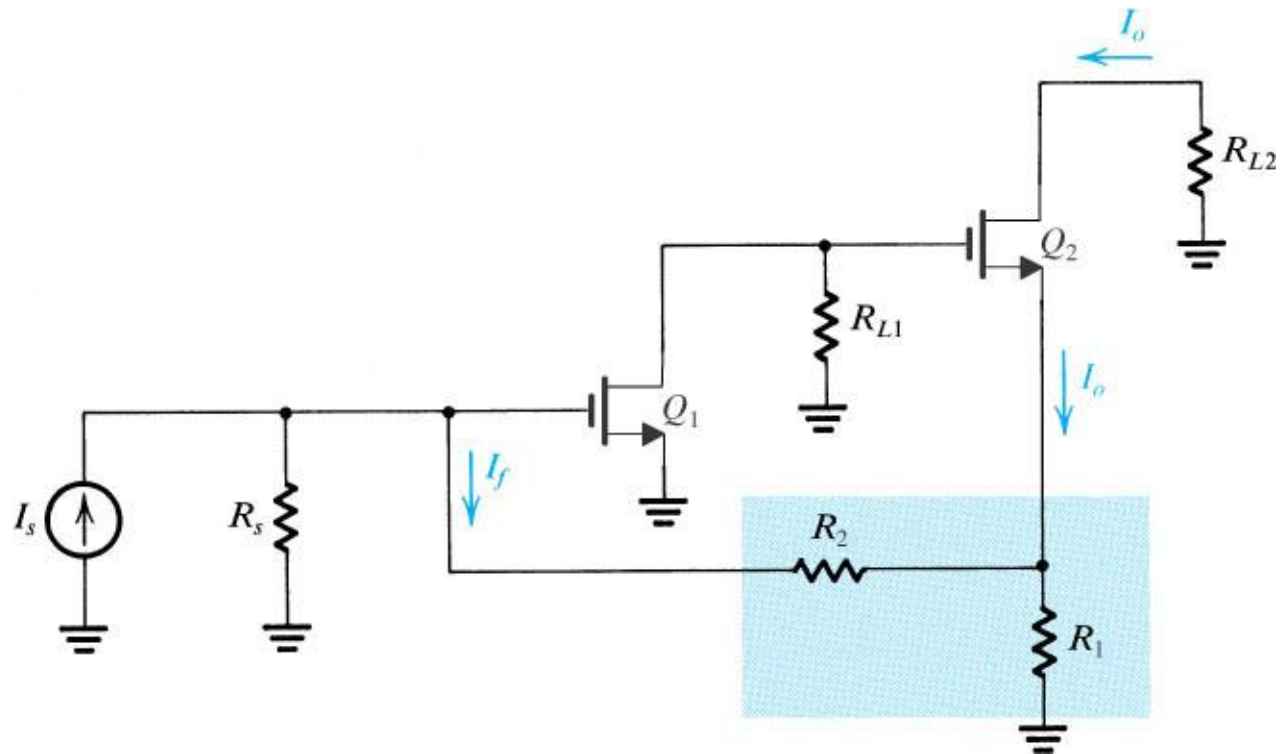
$$\text{Calculate } \beta_f A_{Vo} = (-0.25)(19.3 \text{ V/V}) = -4.8$$

$$\text{Calculate voltage gain with feedback from } A_{Vfo} = \frac{A_{Vo}}{1 + \beta_f A_{Vo}} = \frac{-19.3 \text{ V/V}}{1 - 4.8} = +5.8 \text{ V/V}$$

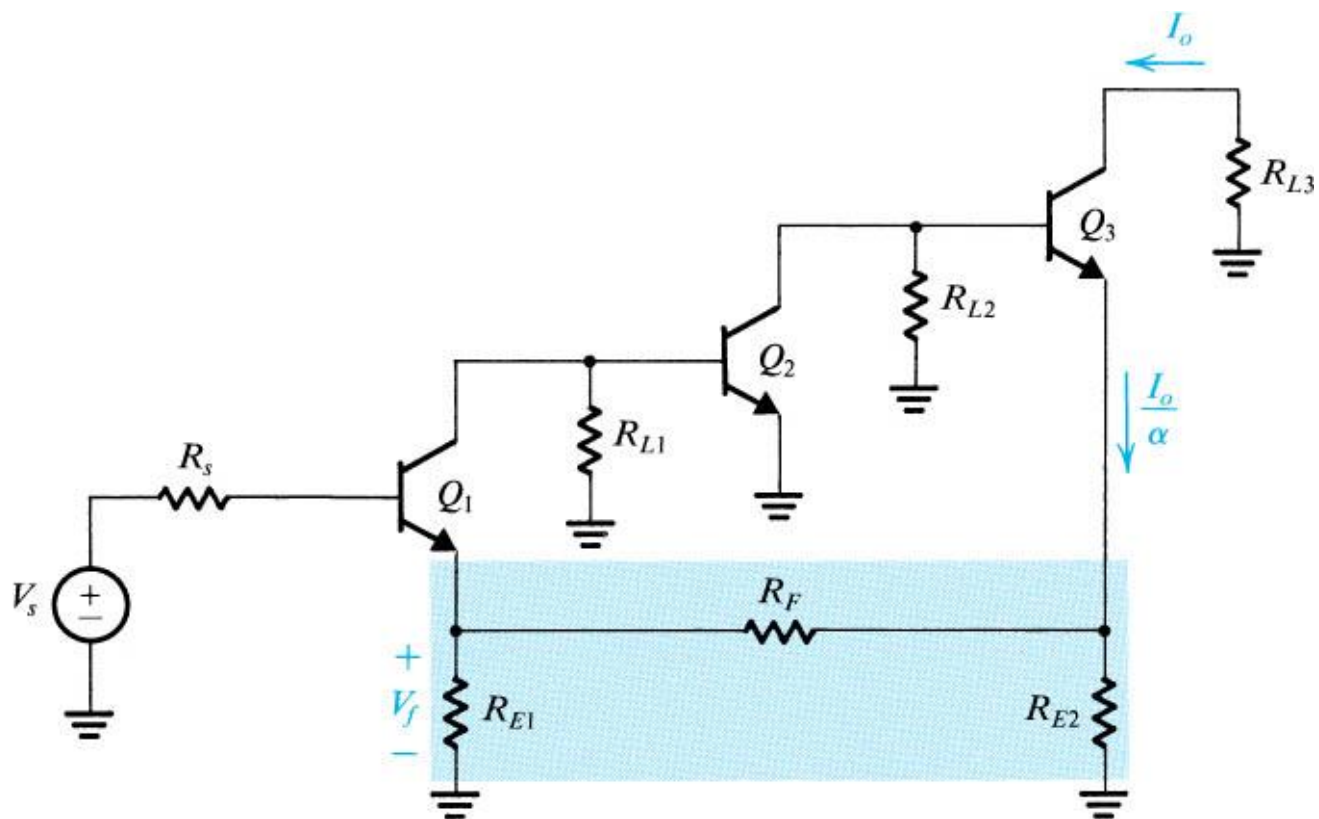
Magnitude is off by nearly a factor of ten!



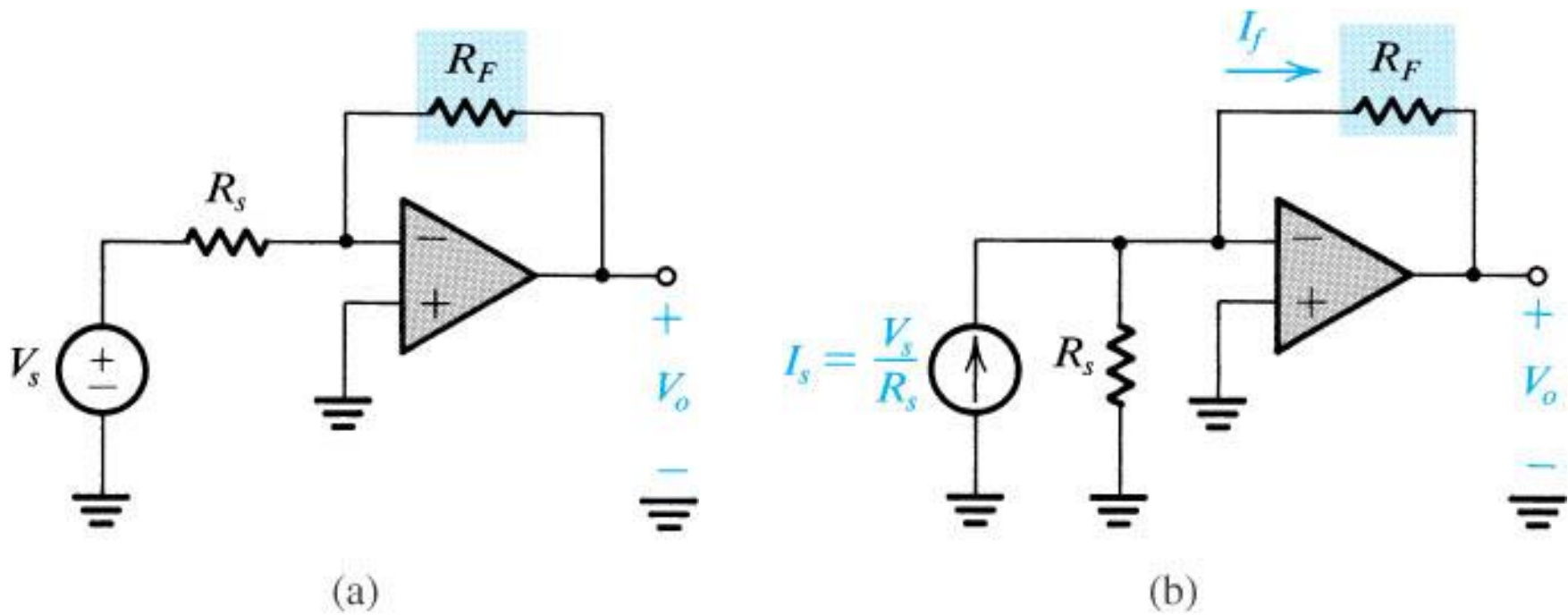
**Figure 8.4** The four basic feedback topologies: (a) voltage-mixing voltage-sampling (series–shunt) topology; (b) current-mixing current-sampling (shunt–series) topology; (c) voltage-mixing current-sampling (series–series) topology; (d) current-mixing voltage-sampling (shunt–shunt) topology.



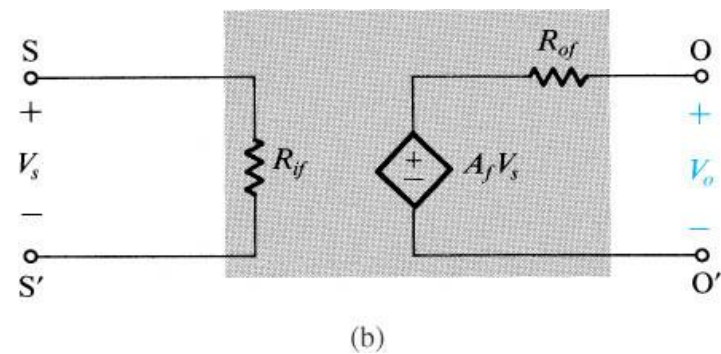
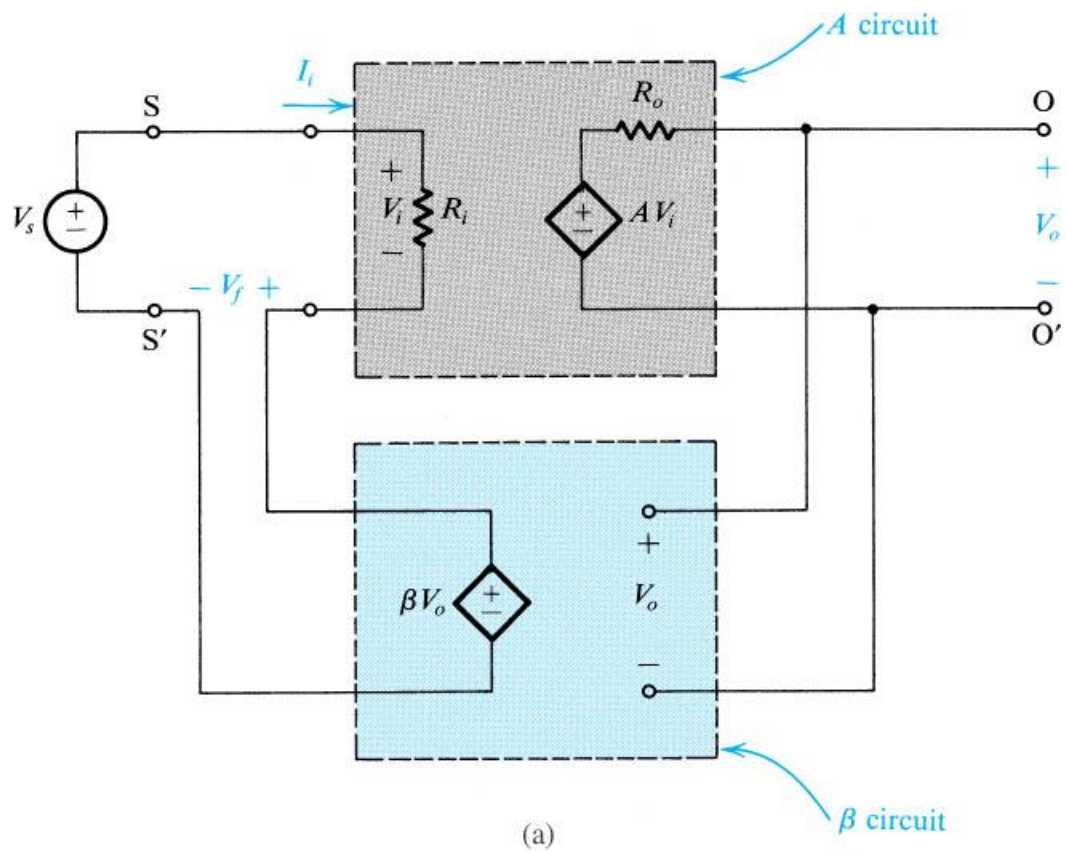
**Figure 8.5** A transistor amplifier with shunt–series feedback. (Biasing not shown.)



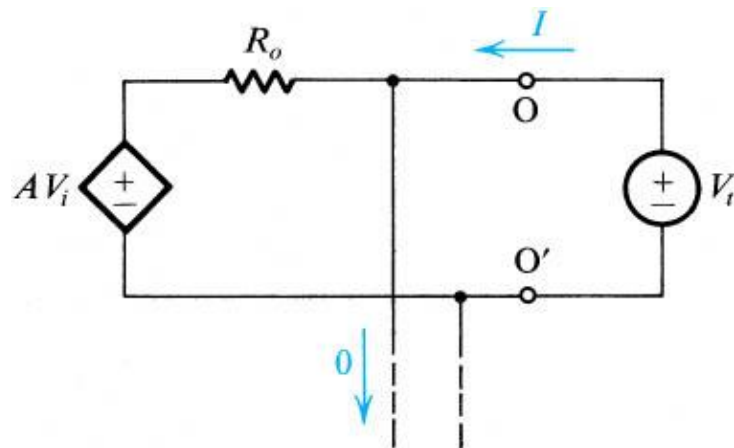
**Figure 8.6** An example of the series-series feedback topology. (Biasing not shown.)



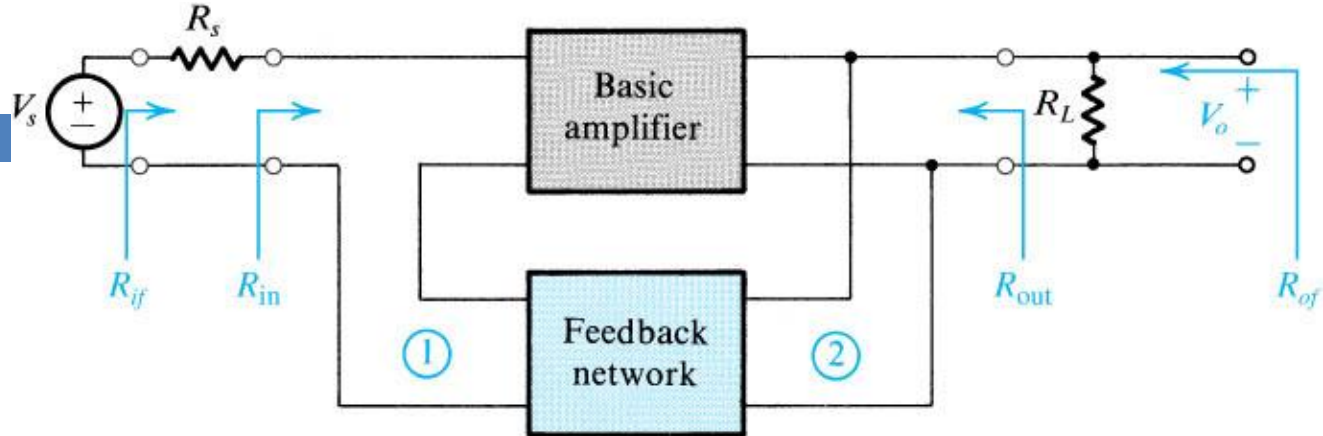
**Figure 8.7** (a) The inverting op-amp configuration redrawn as (b) an example of shunt–shunt feedback.



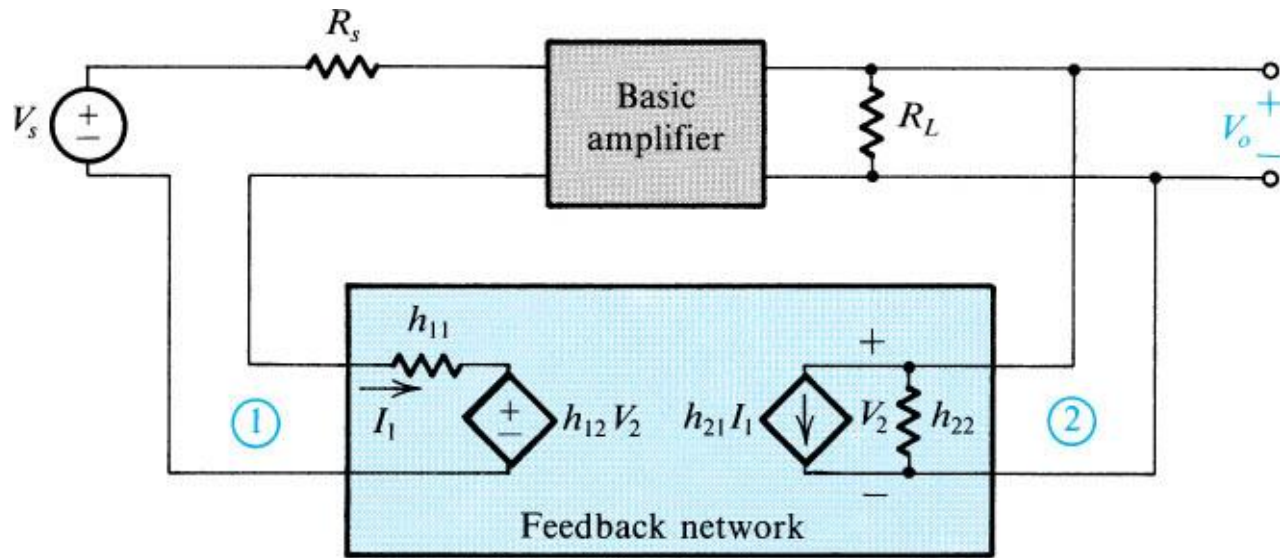
**Figure 8.8** The series–shunt feedback amplifier: (a) ideal structure and (b) equivalent circuit.



**Figure 8.9** Measuring the output resistance of the feedback amplifier of Fig. 8.8(a):  $R_{of} = V_t/I$ .

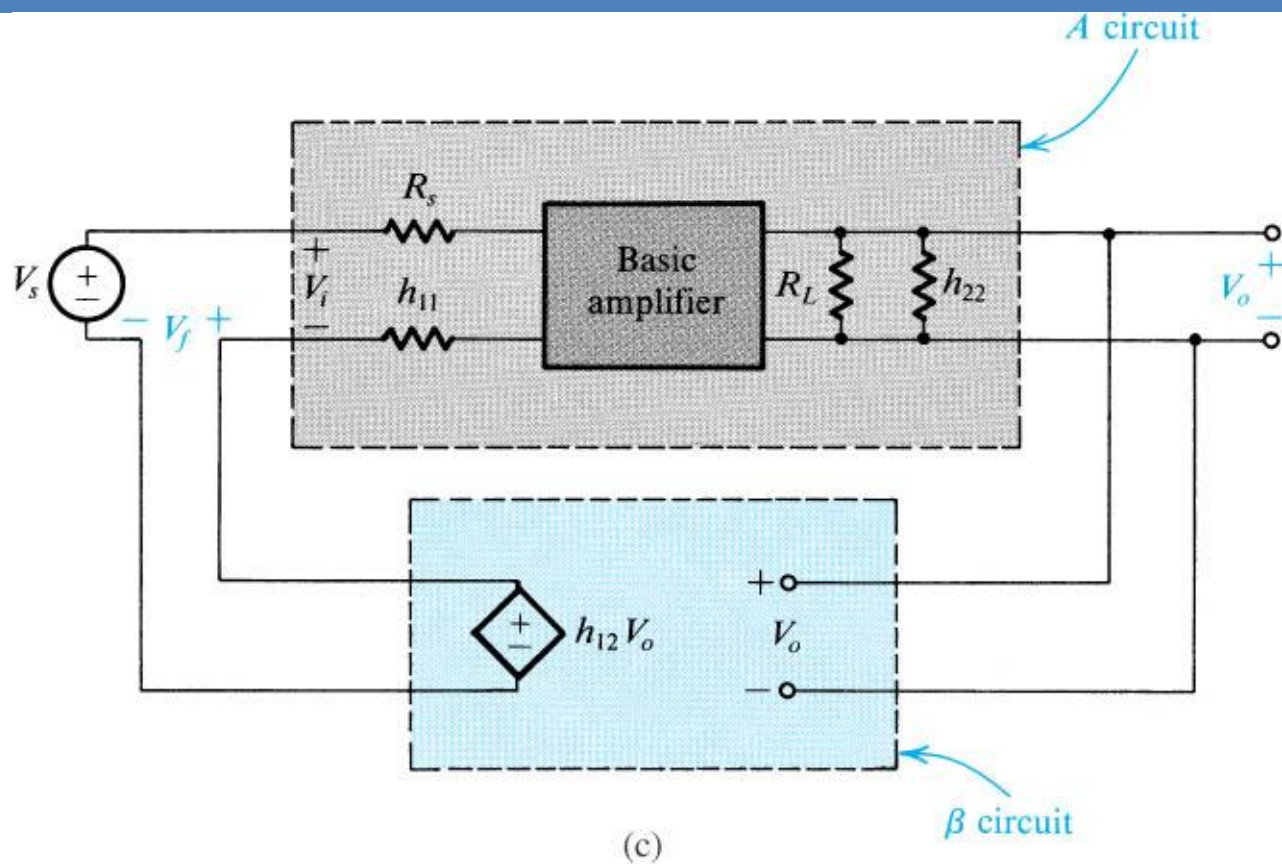


(a)

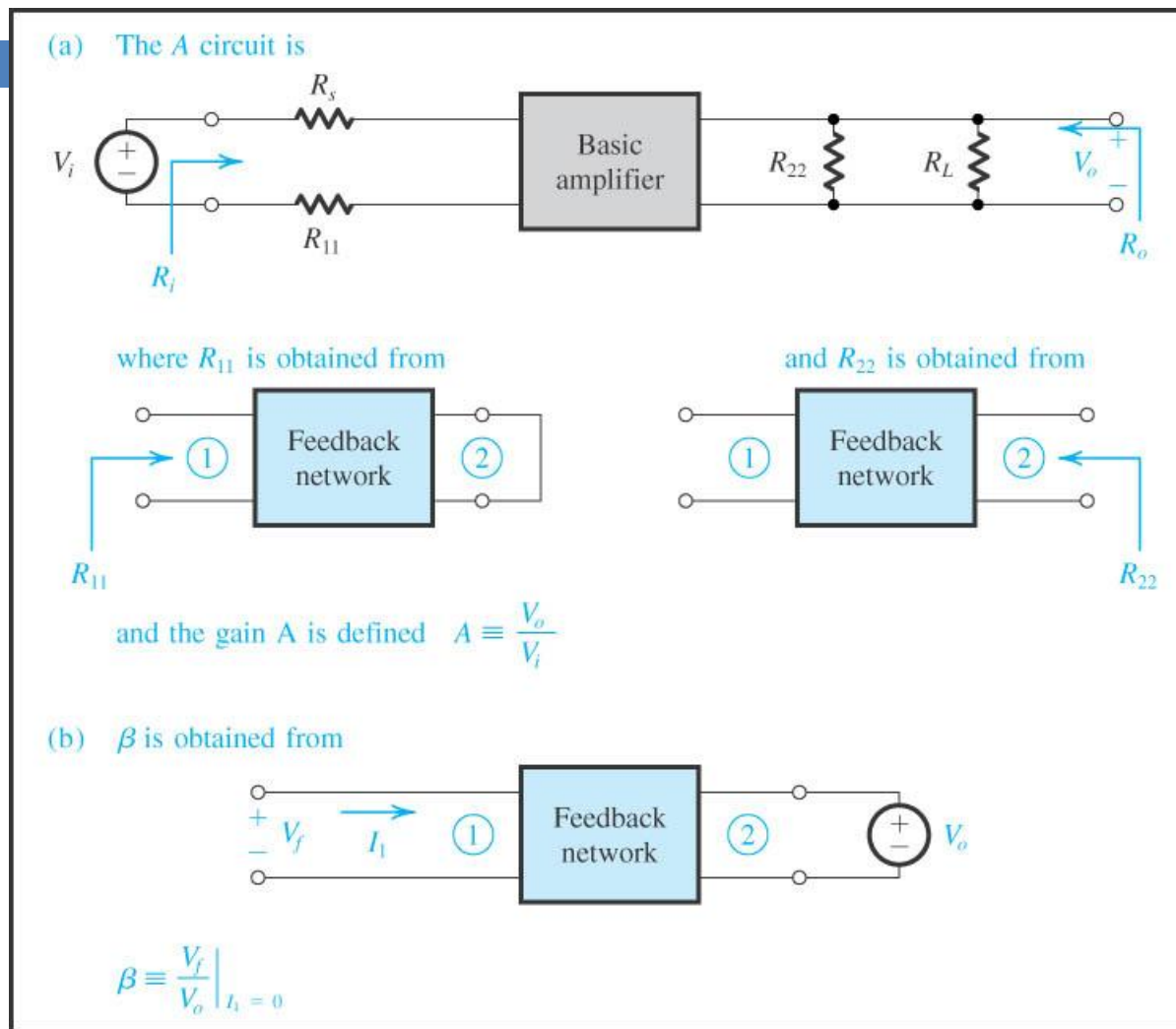


(b)

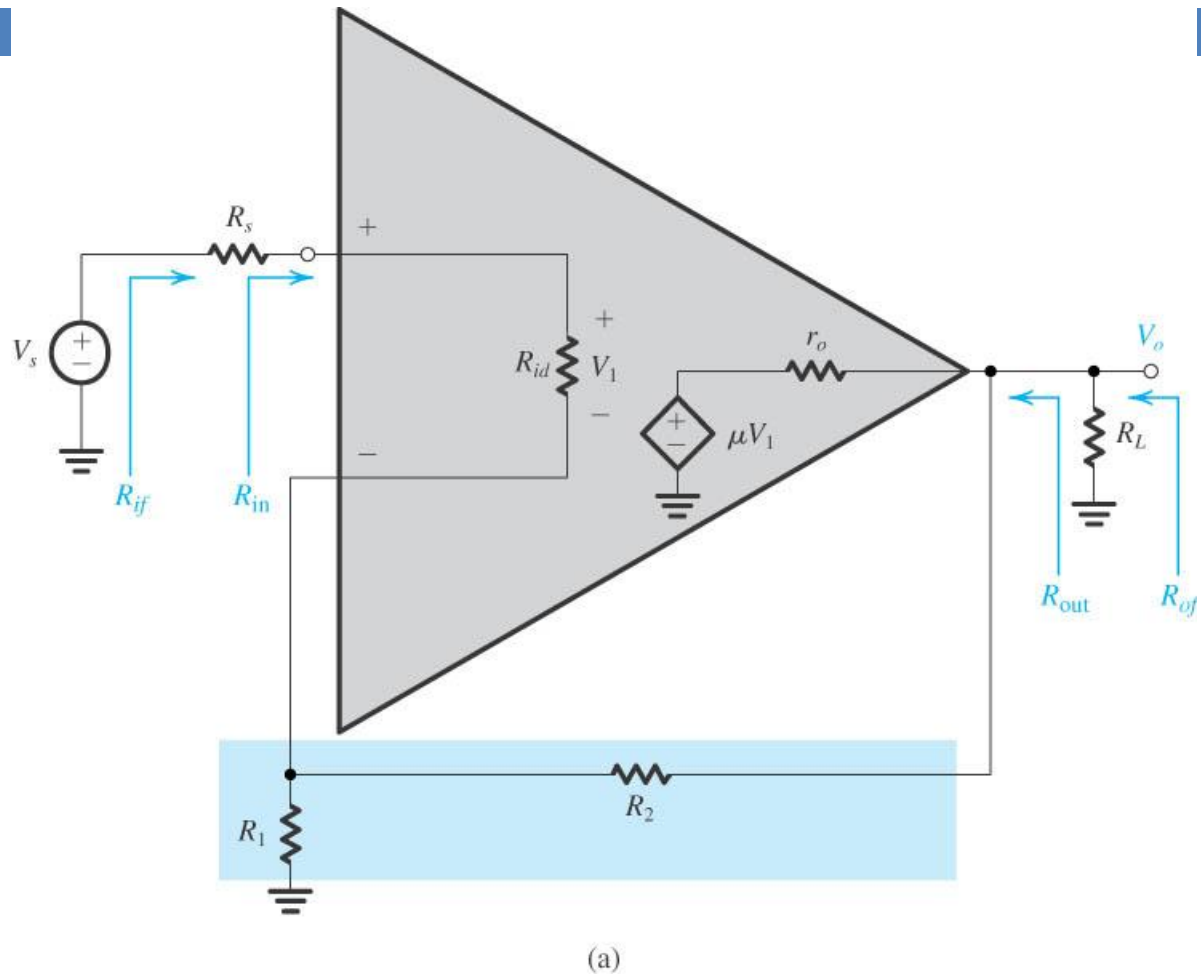
**Figure 8.10** Derivation of the  $A$  circuit and  $\beta$  circuit for the series-shunt feedback amplifier. (a) Block diagram of a practical series-shunt feedback amplifier. (b) The circuit in (a) with the feedback network represented by its  $h$  parameters.



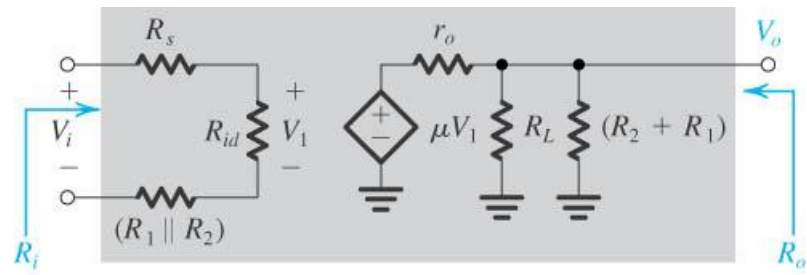
**Figure 8.10** (Continued) (c) The circuit in (b) with  $h_{21}$  neglected.



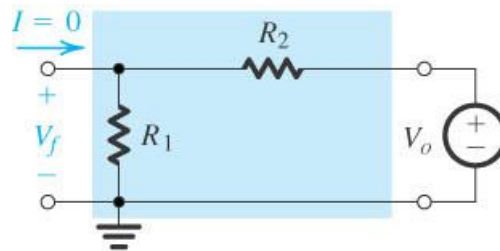
**Figure 8.11** Summary of the rules for finding the  $A$  circuit and  $\beta$  for the voltage-mixing voltage-sampling case of Fig. 8.10(a).



**Figure 8.12** Circuits for Example 8.1.



(b)



(c)

**Figure 8.12** (Continued)

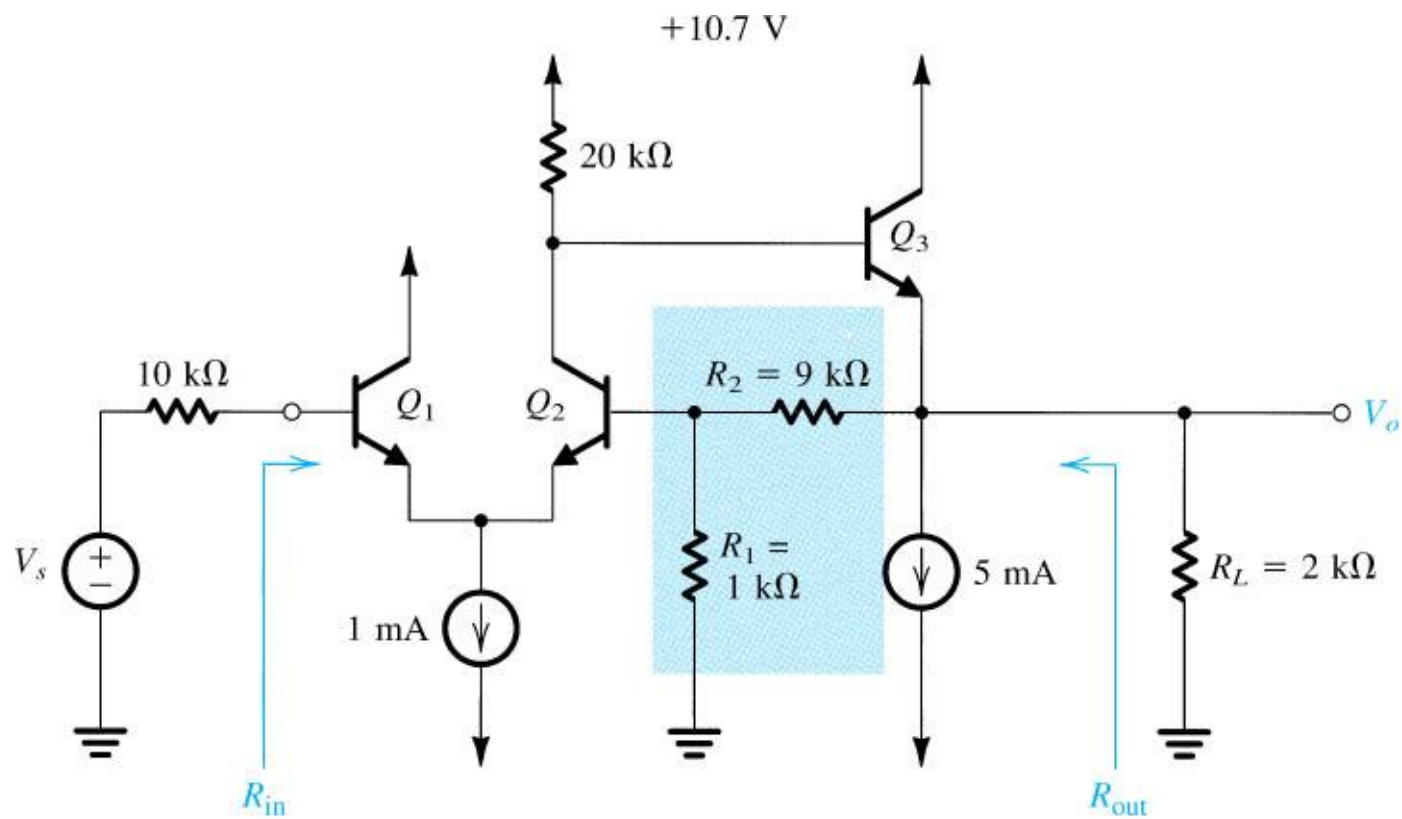
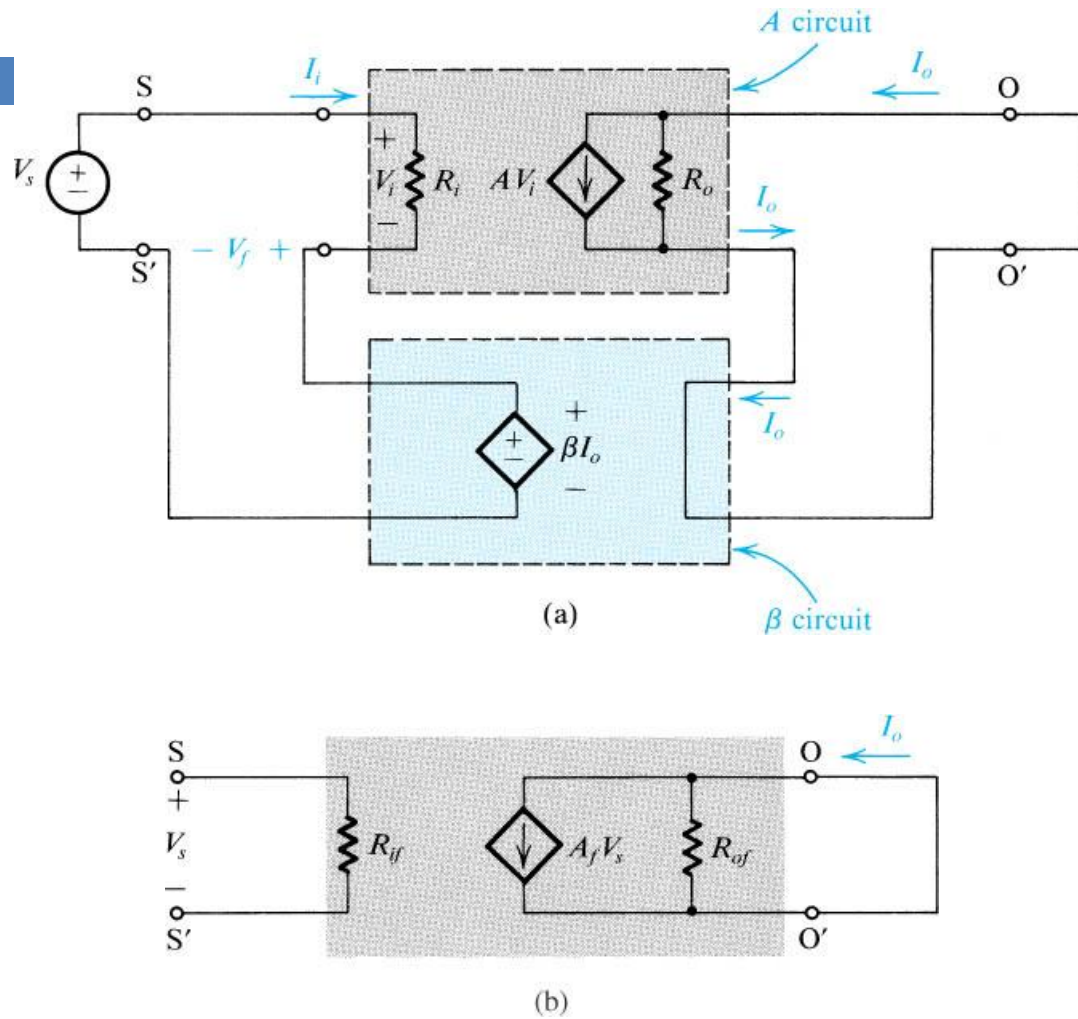
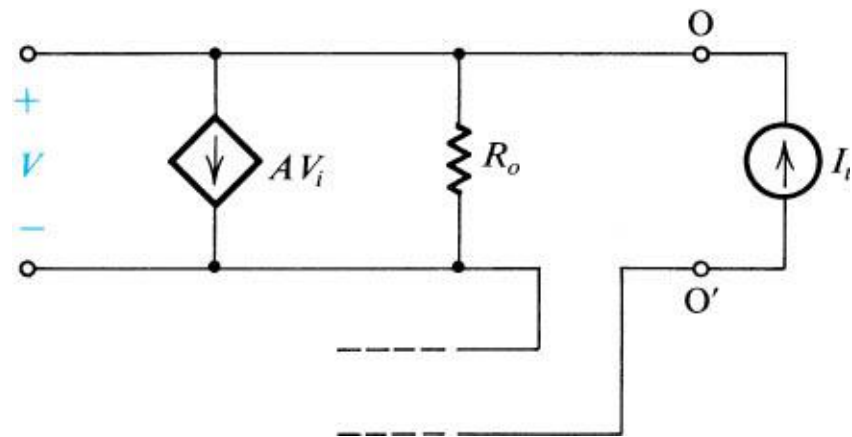


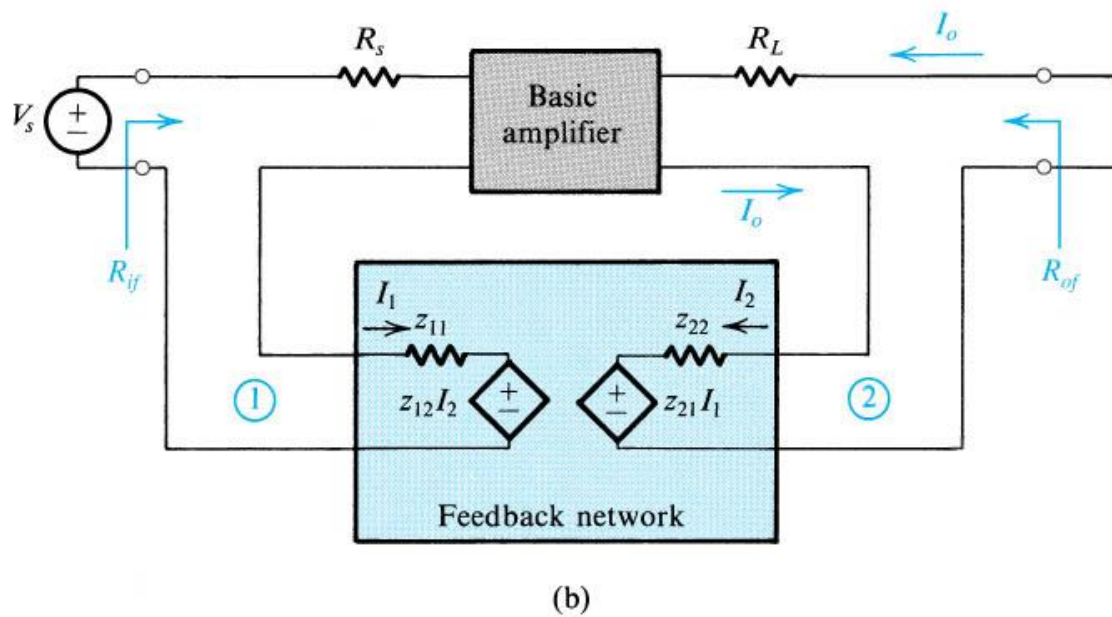
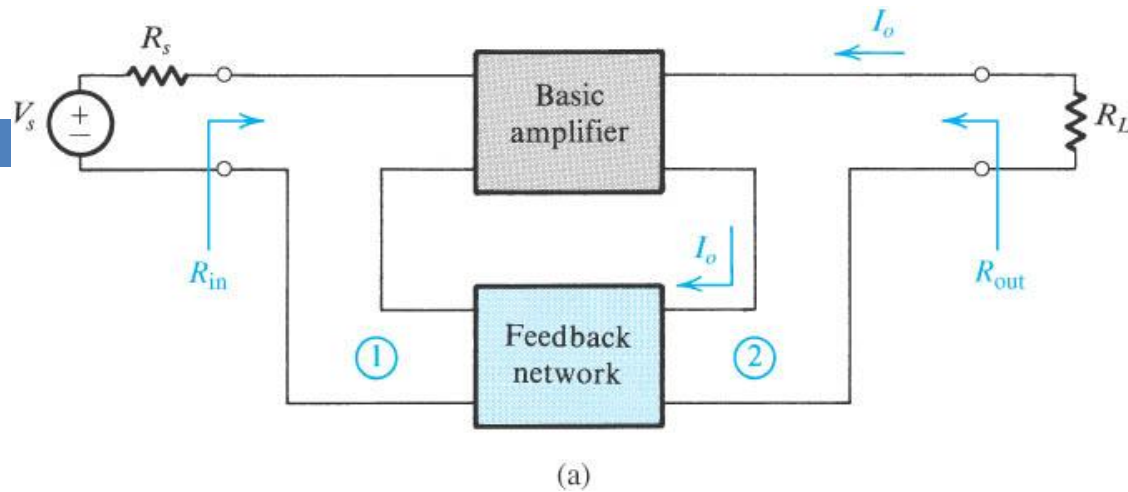
Figure E8.5



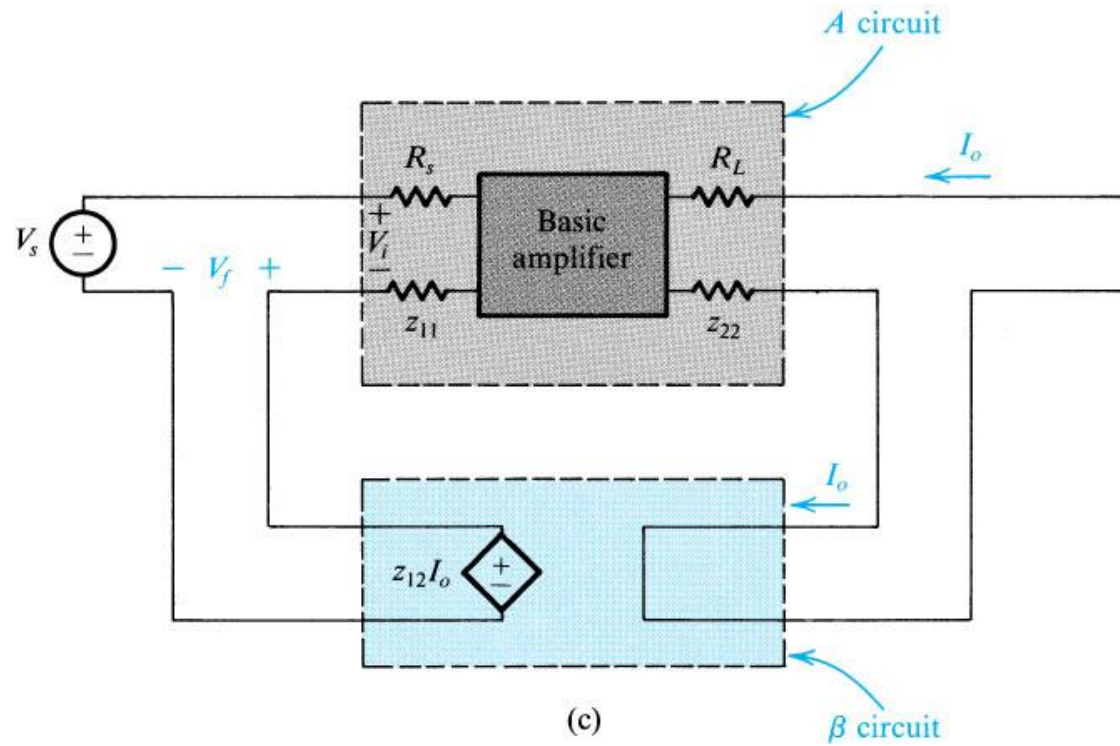
**Figure 8.13** The series-series feedback amplifier: (a) ideal structure and (b) equivalent circuit.



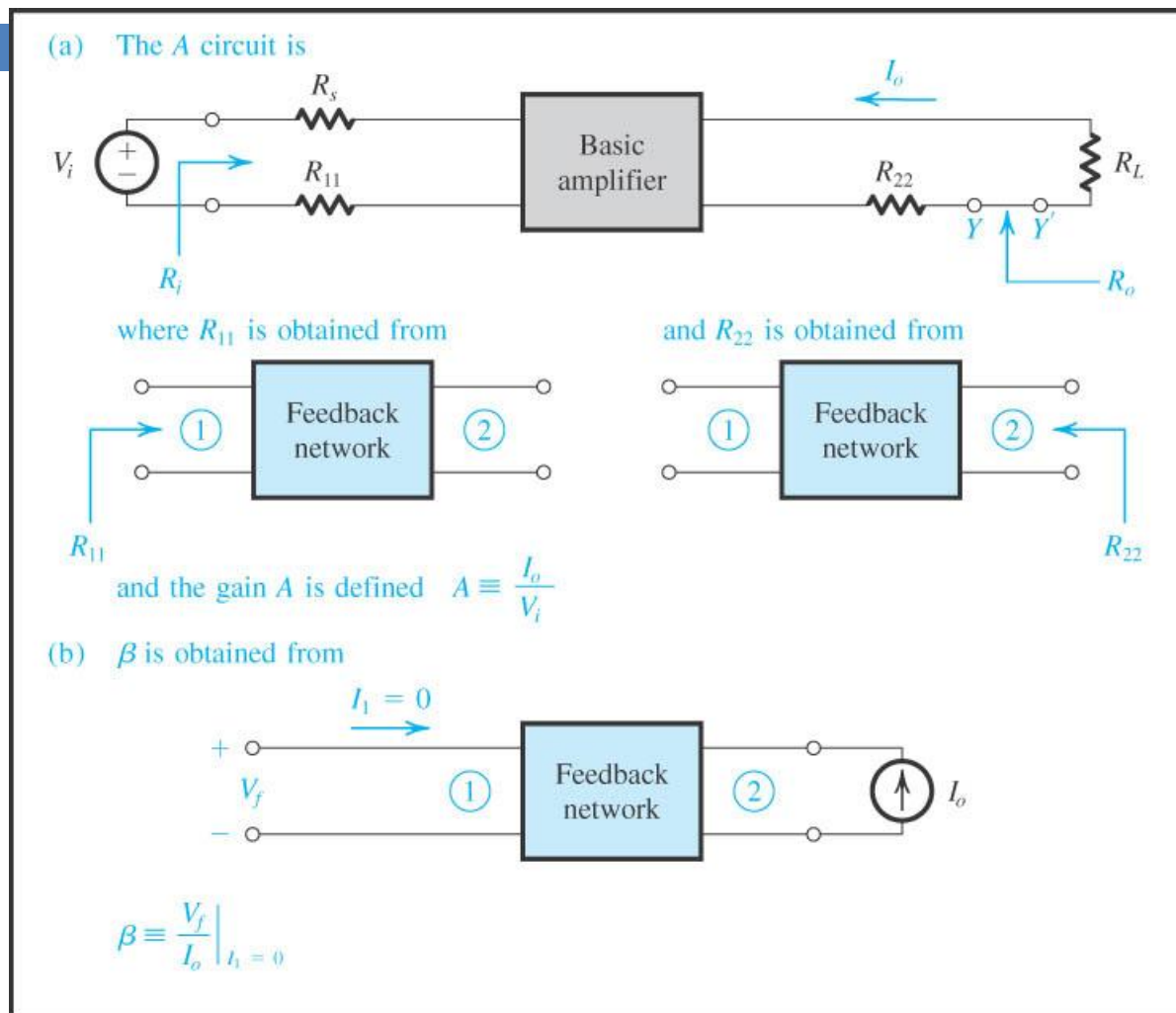
**Figure 8.14** Measuring the output resistance  $R_{of}$  of the series-series feedback amplifier.



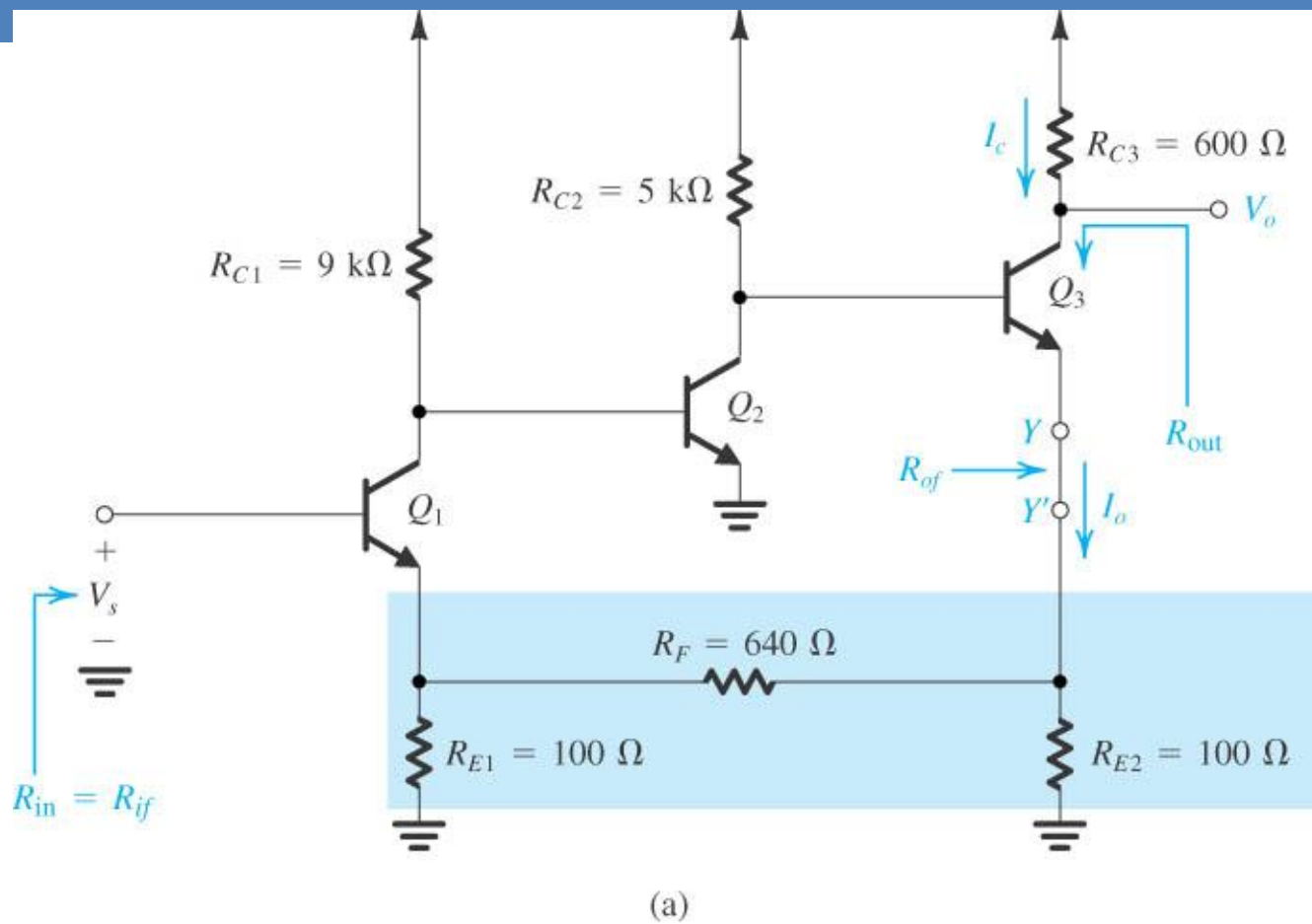
**Figure 8.15** Derivation of the  $A$  circuit and the  $\beta$  circuit for series–series feedback amplifiers. **(a)** A series–series feedback amplifier. **(b)** The circuit of (a) with the feedback network represented by its  $z$  parameters.



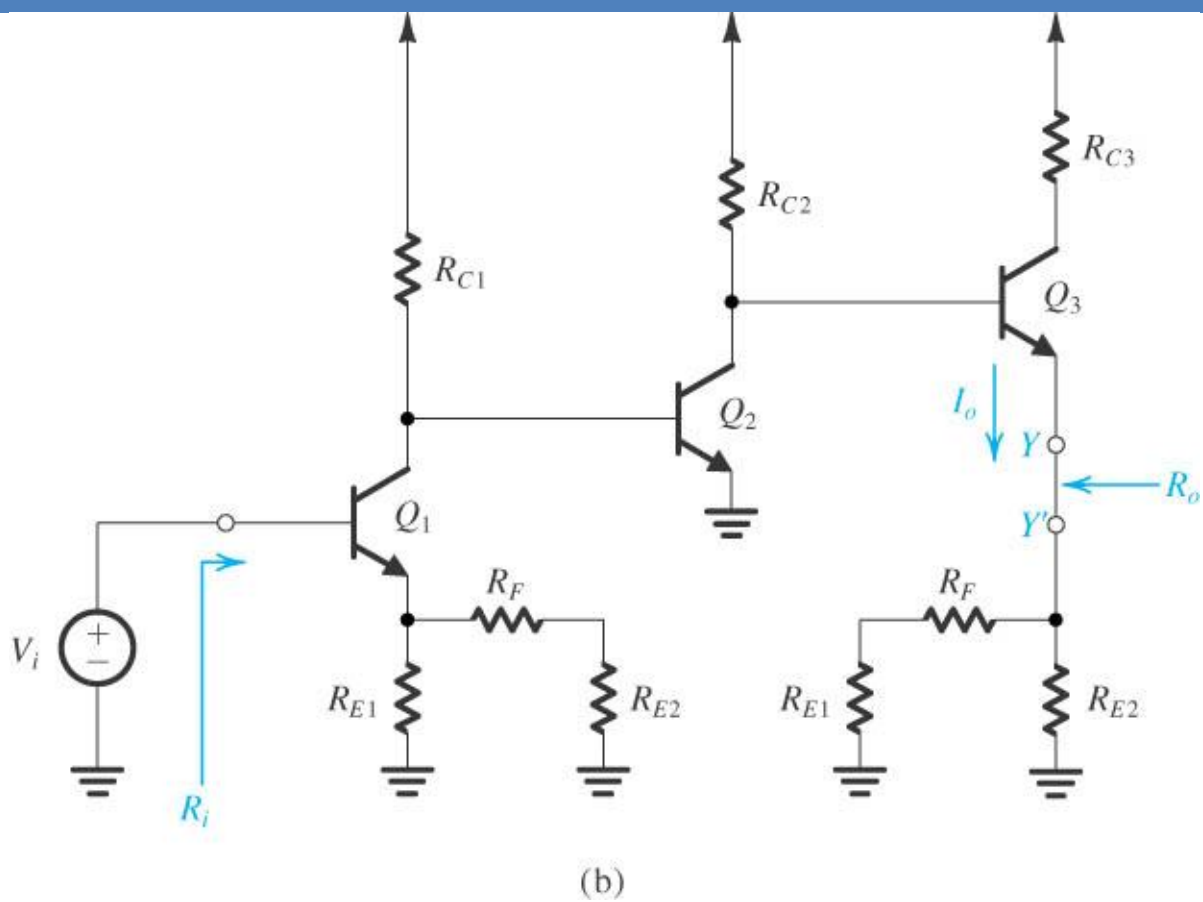
**Figure 8.15** (Continued) (c) A redrawing of the circuit in (b) with  $z_{21}$  neglected.



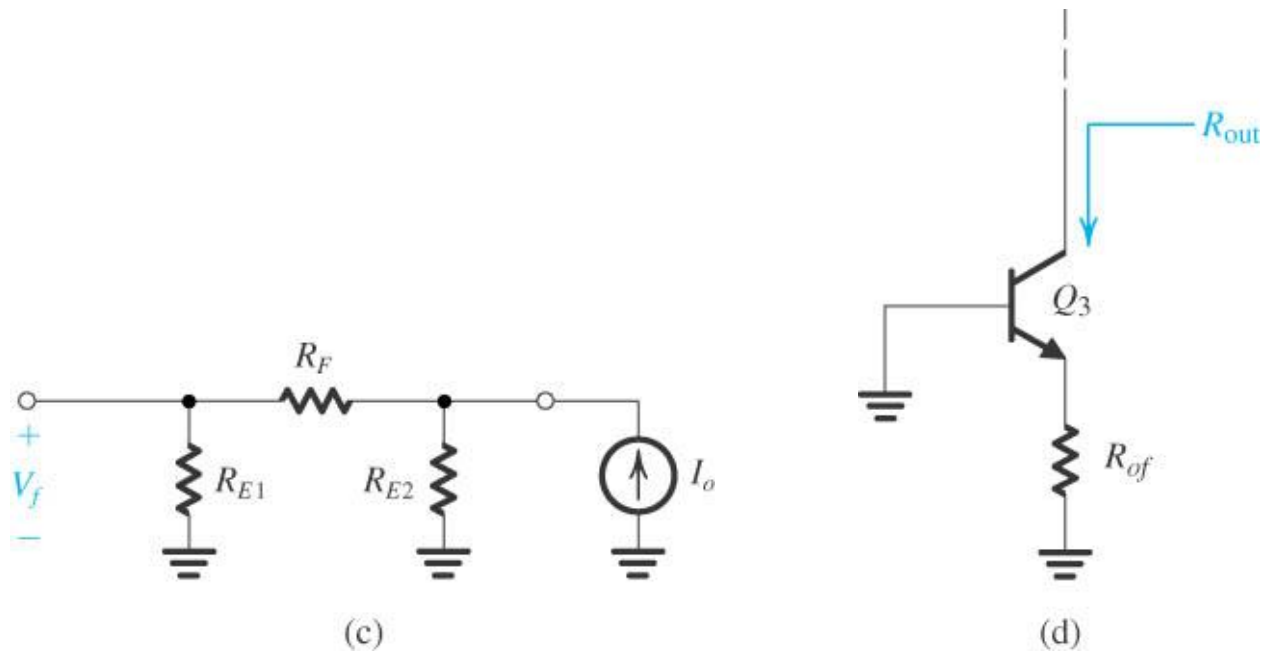
**Figure 8.16** Finding the  $A$  circuit and  $\beta$  for the voltage-mixing current-sampling (series-series) case.



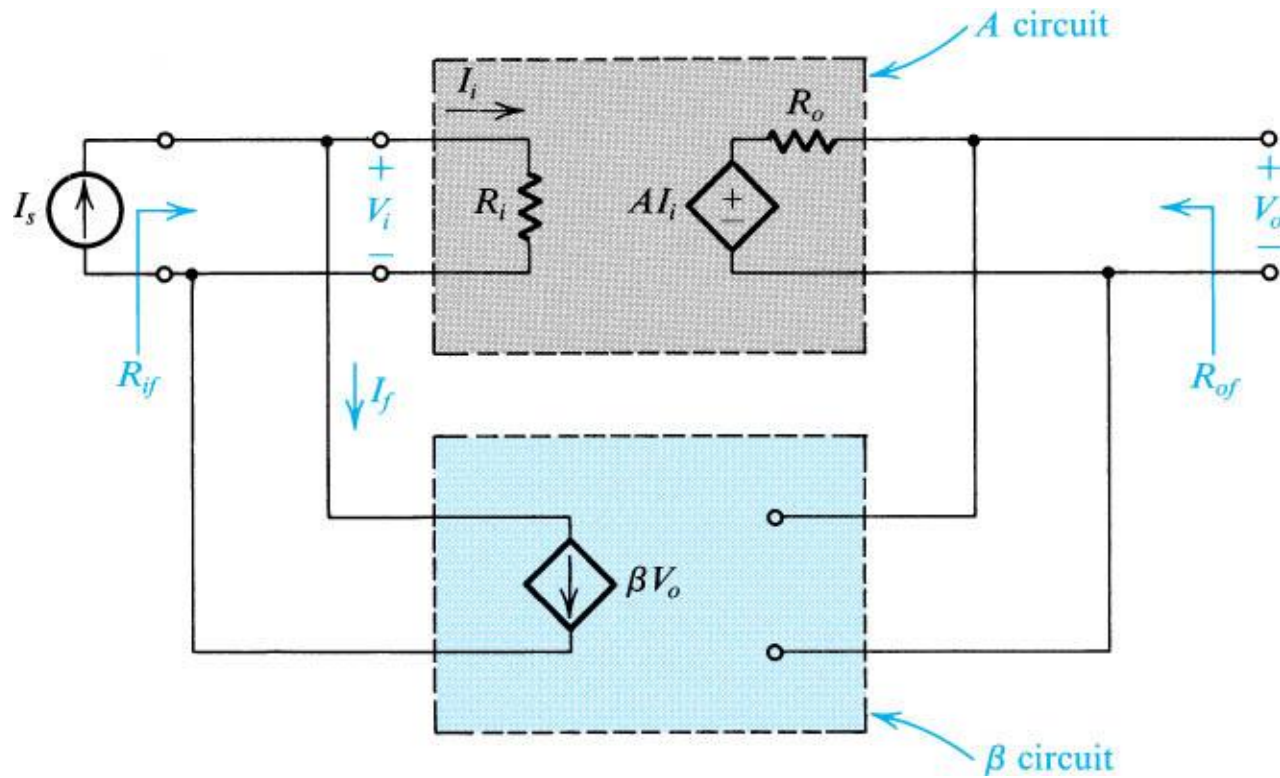
**Figure 8.17** Circuits for Example 8.2.



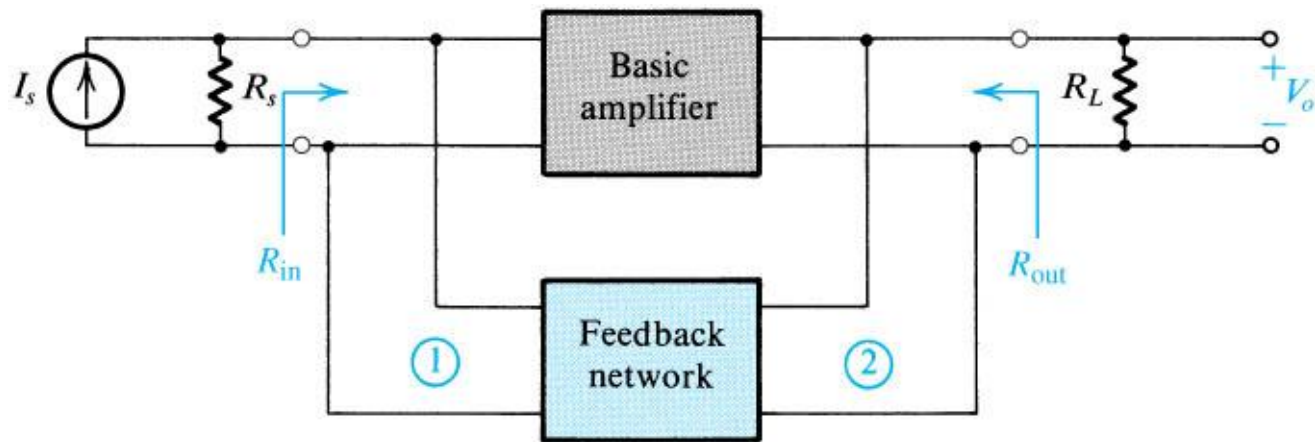
**Figure 8.17** (Continued)



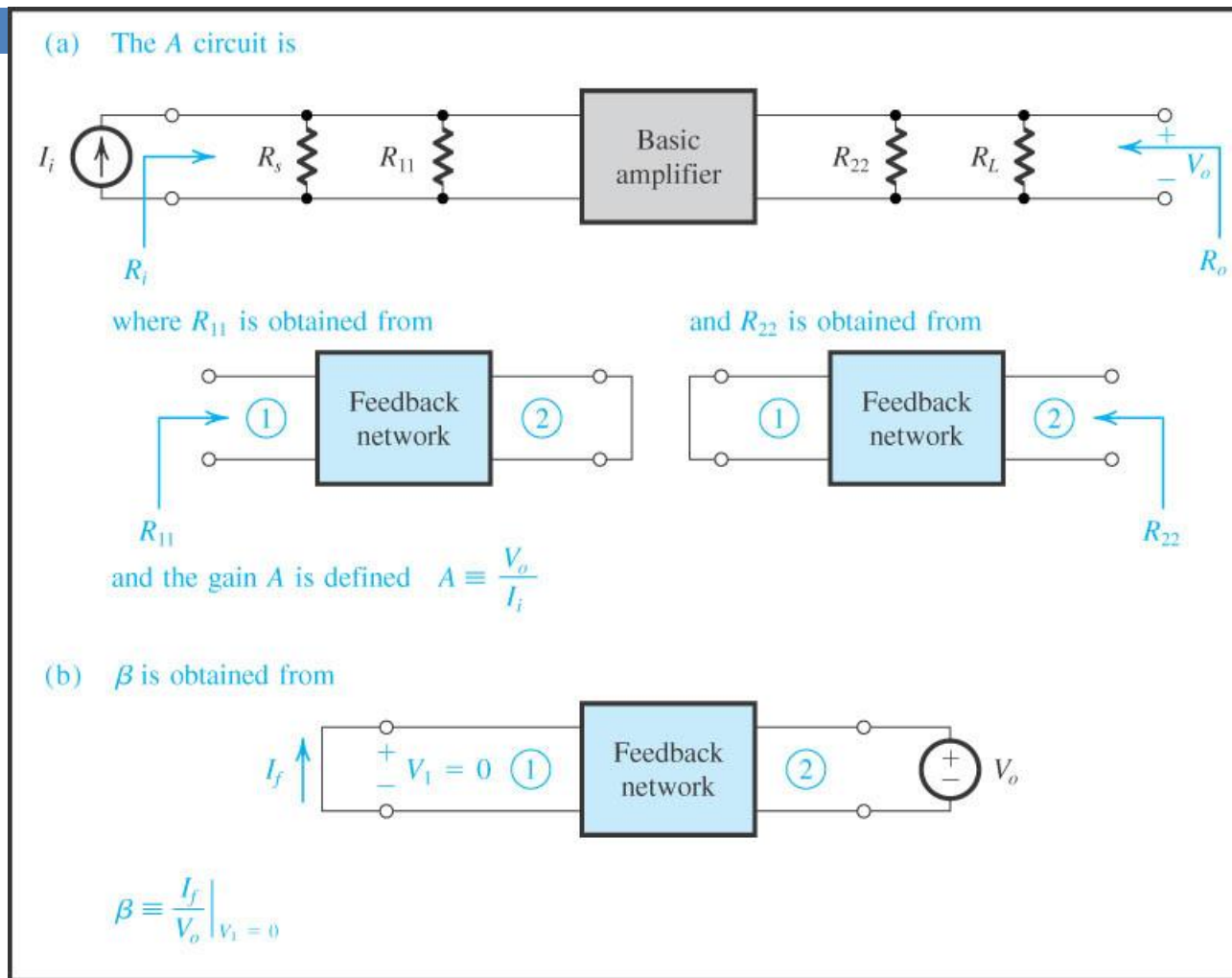
**Figure 8.17** (Continued).



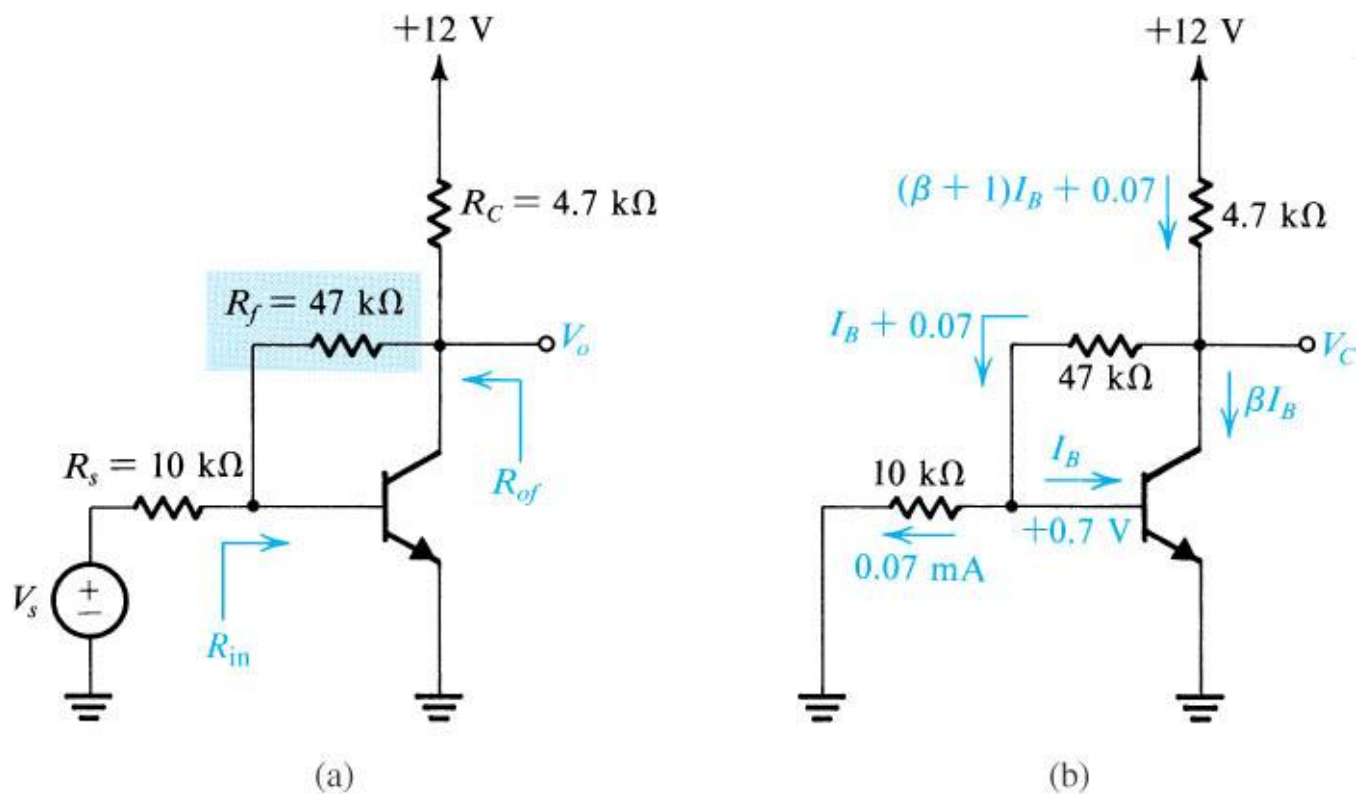
**Figure 8.18** Ideal structure for the shunt–shunt feedback amplifier.



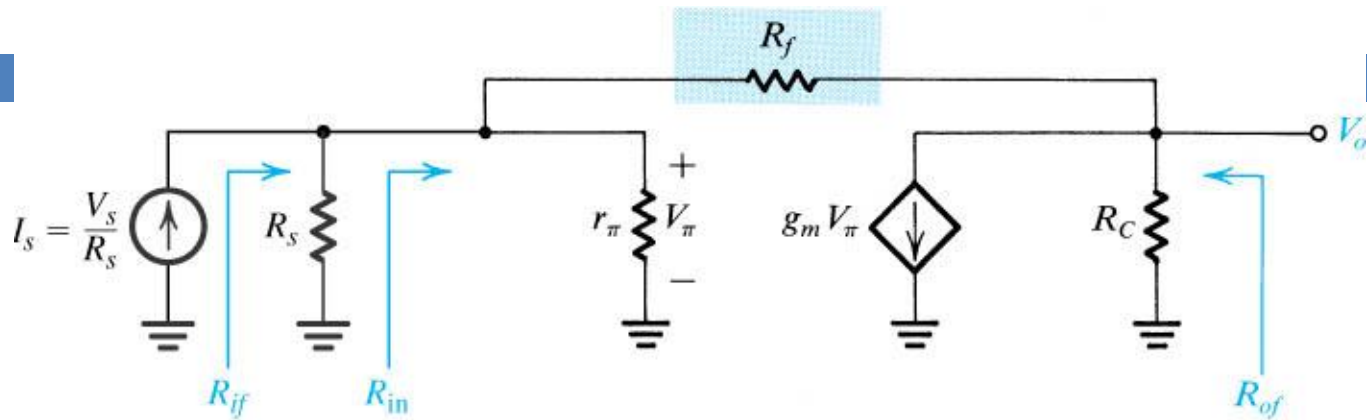
**Figure 8.19** Block diagram for a practical shunt–shunt feedback amplifier.



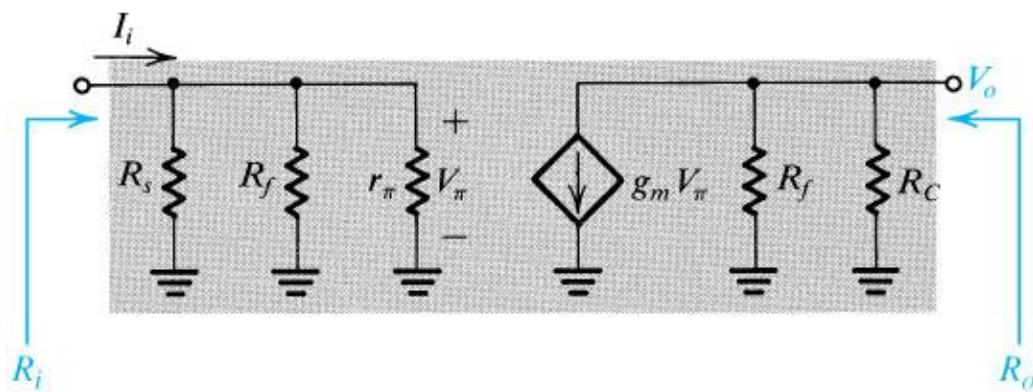
**Figure 8.20** Finding the  $A$  circuit and  $\beta$  for the current-mixing voltage-sampling (shunt–shunt) feedback amplifier in Fig. 8.19.



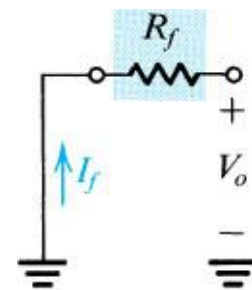
**Figure 8.21** Circuits for Example 8.3.



(c)

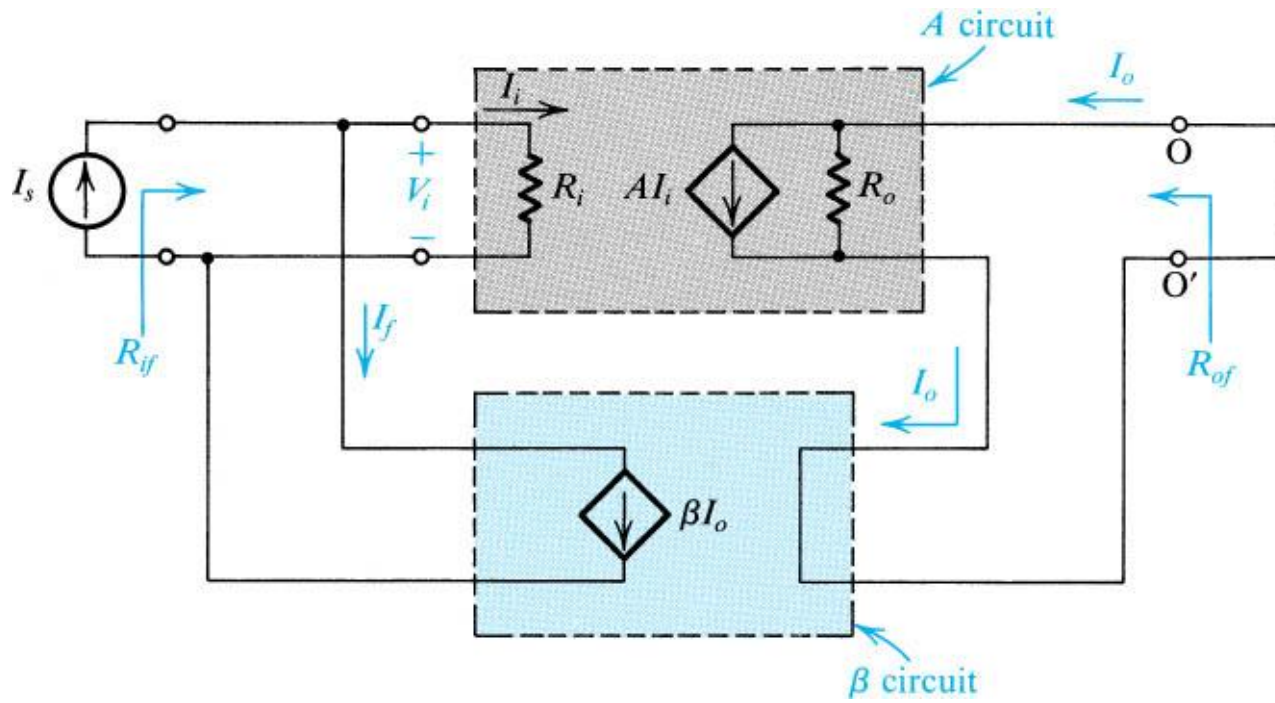


(d)

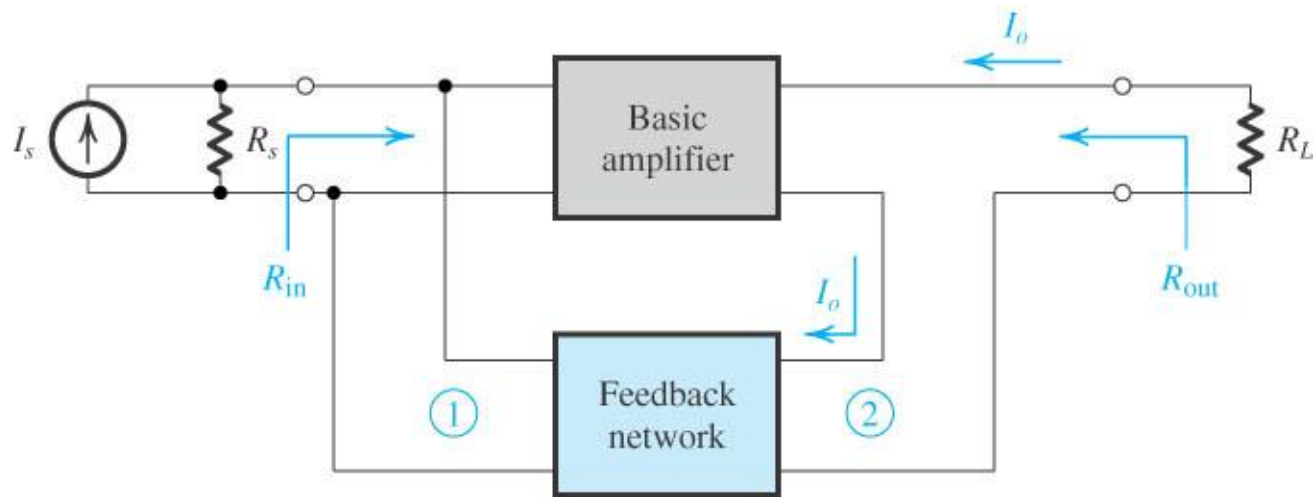


(e)

Figure 8.21 (Continued)

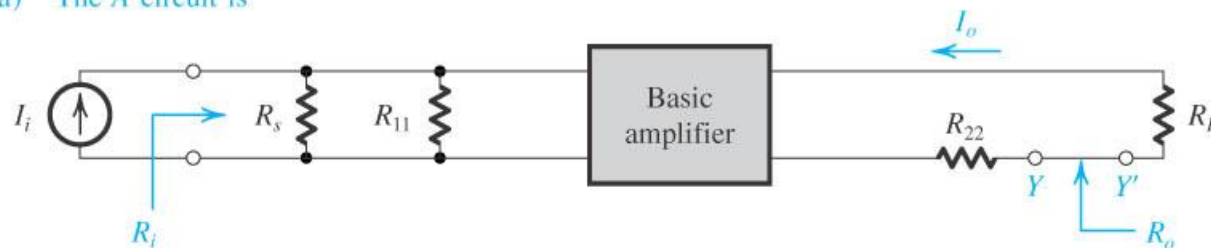


**Figure 8.22** Ideal structure for the shunt-series feedback amplifier.

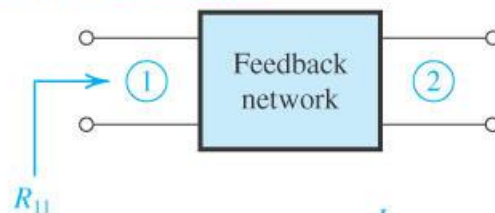


**Figure 8.23** Block diagram for a practical shunt-series feedback amplifier.

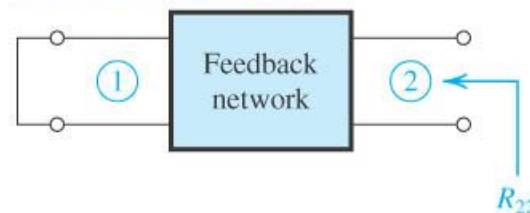
(a) The A circuit is



where  $R_{11}$  is obtained from

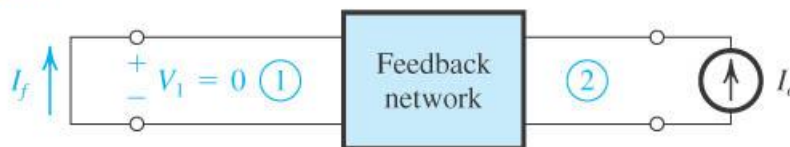


and  $R_{22}$  is obtained from



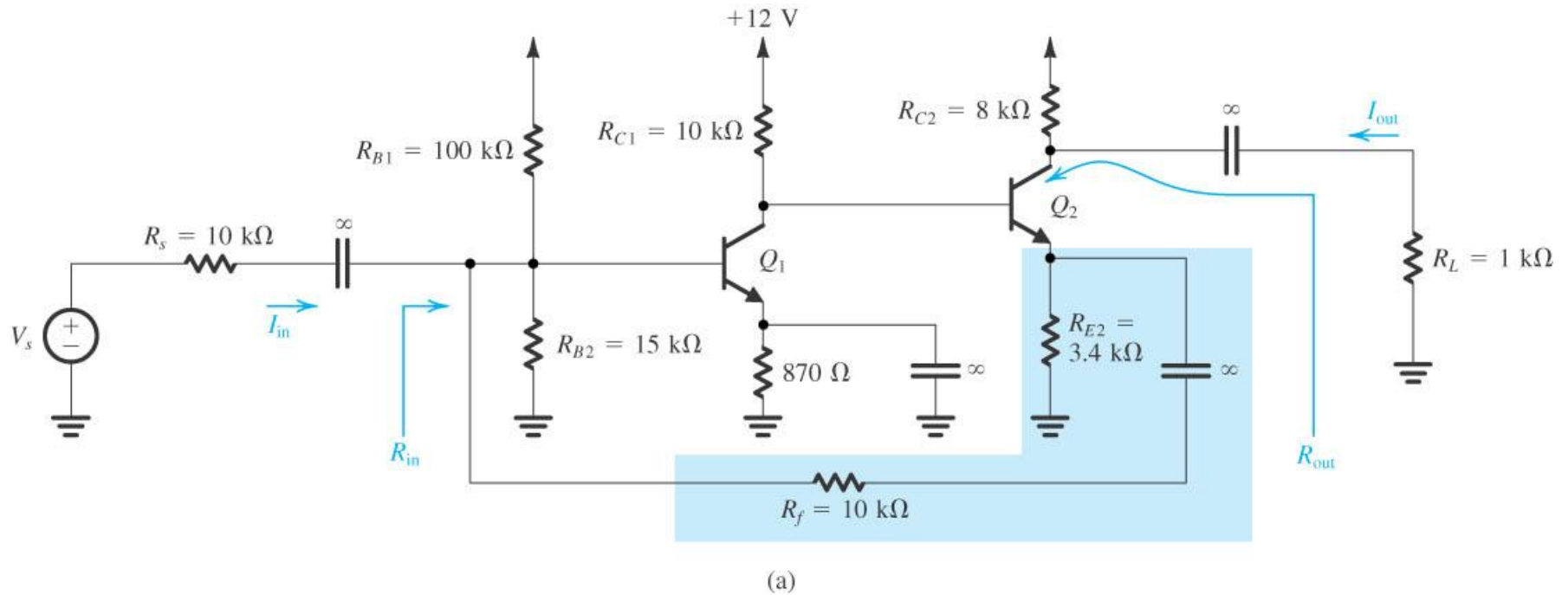
and the gain  $A$  is defined as  $A \equiv \frac{I_o}{I_i}$

(b)  $\beta$  is obtained from

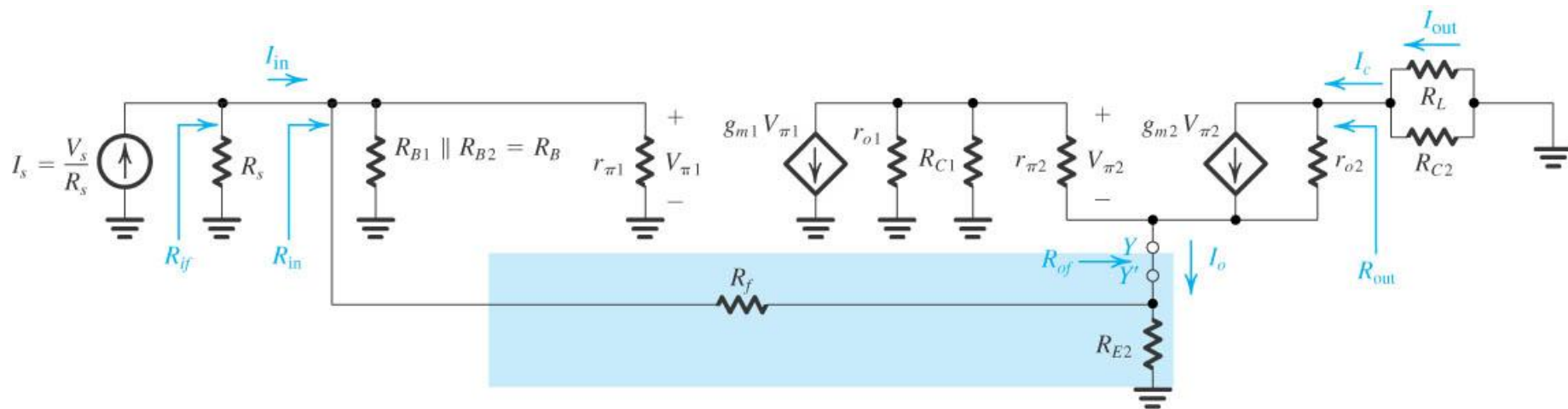


$$\beta \equiv \left. \frac{I_f}{I_o} \right|_{V_1 = 0}$$

**Figure 8.24** Finding the A circuit and  $\beta$  for the current-mixing current-sampling (shunt-series) feedback amplifier of Fig. 8.23.

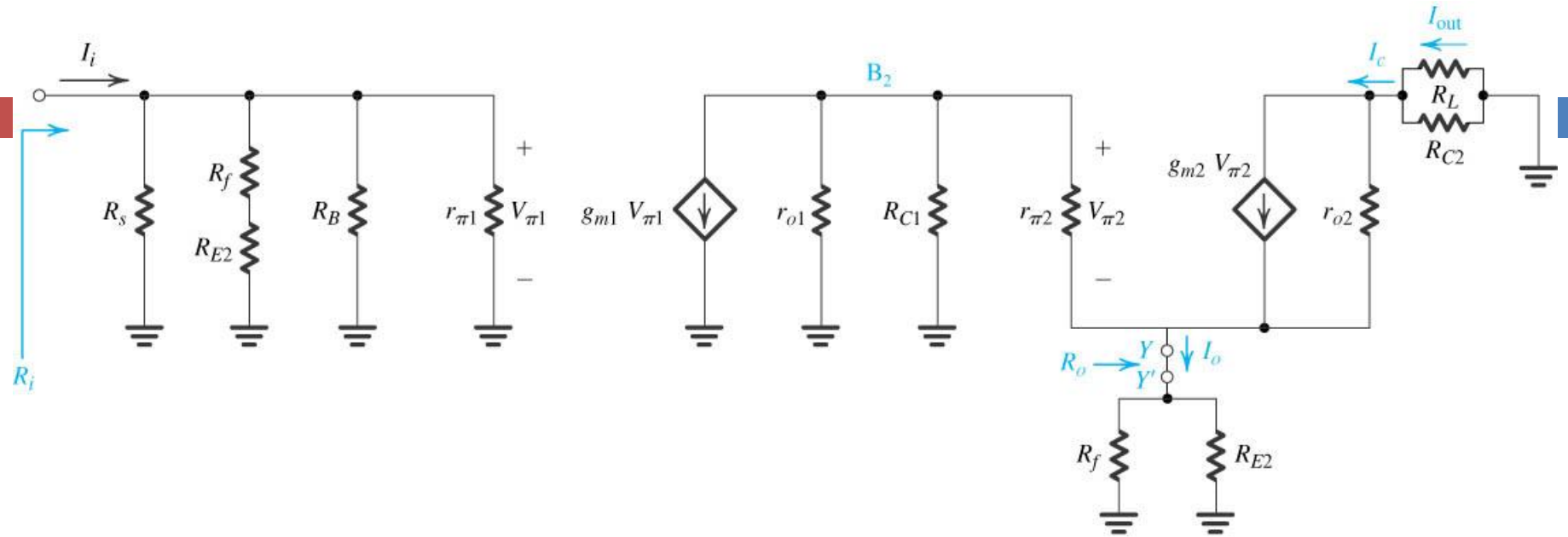


**Figure 8.25** Circuits for Example 8.4.

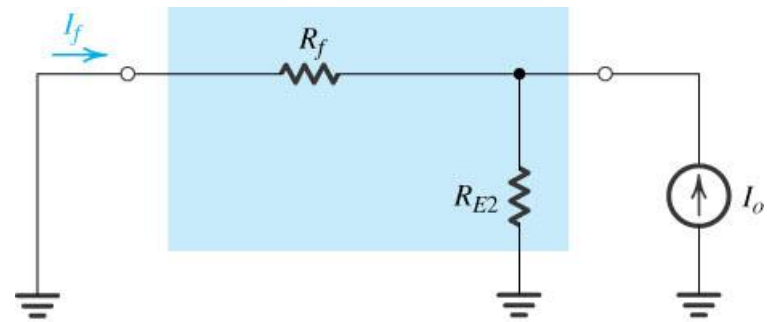


(b)

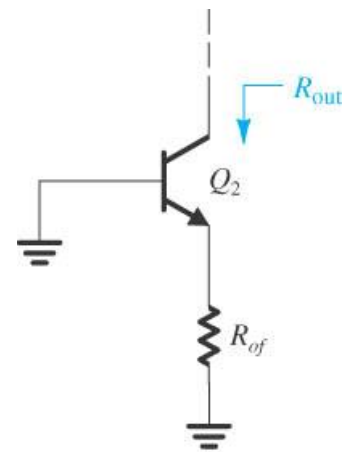
**Figure 8.25** (Continued)



(c)



(d)



(e)

**Figure 8.25** (Continued)

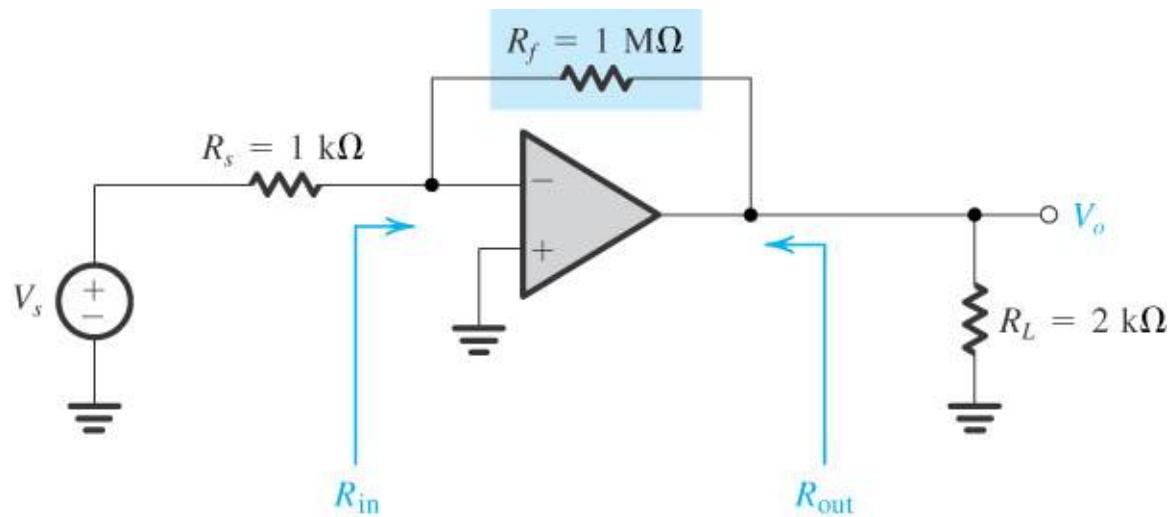
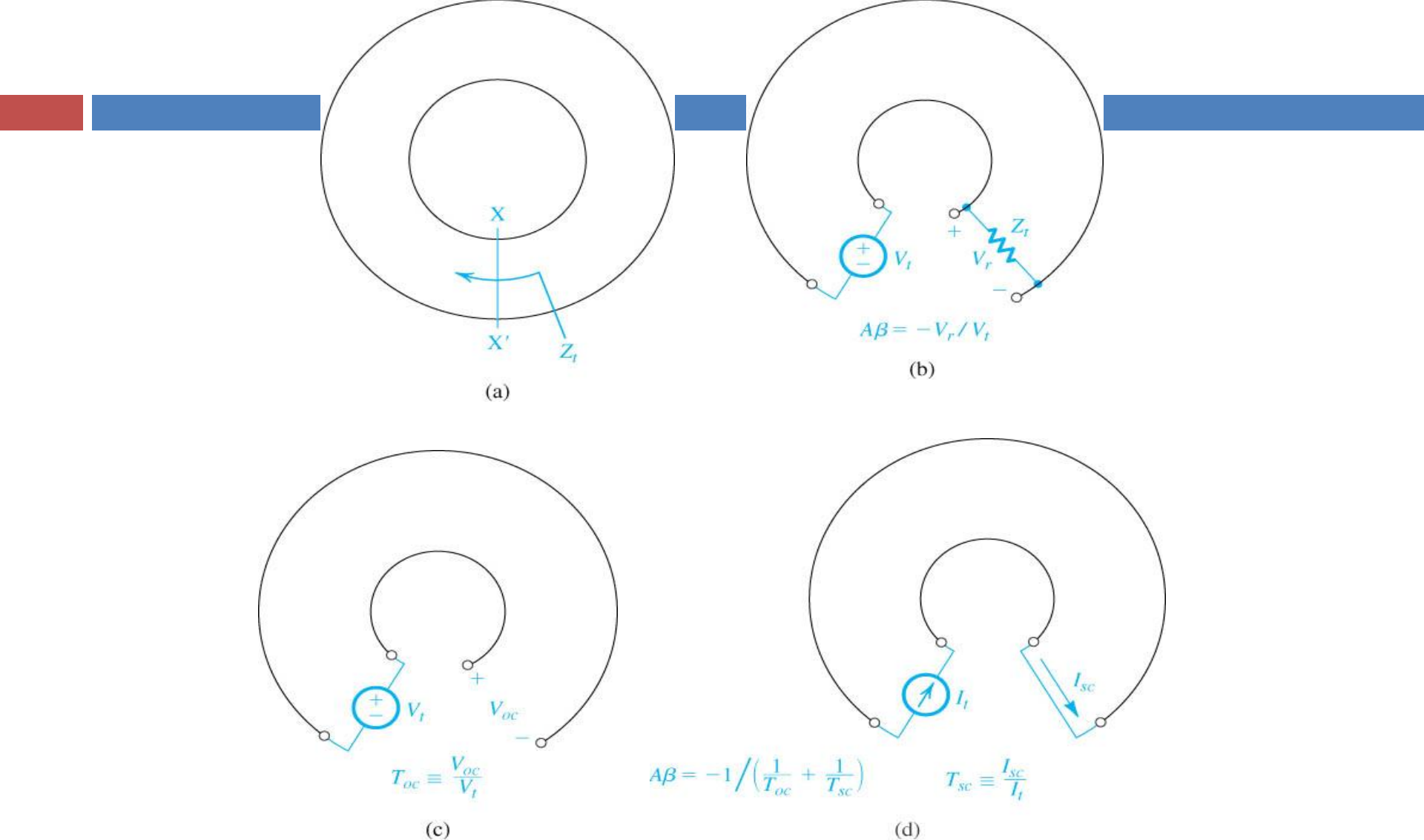
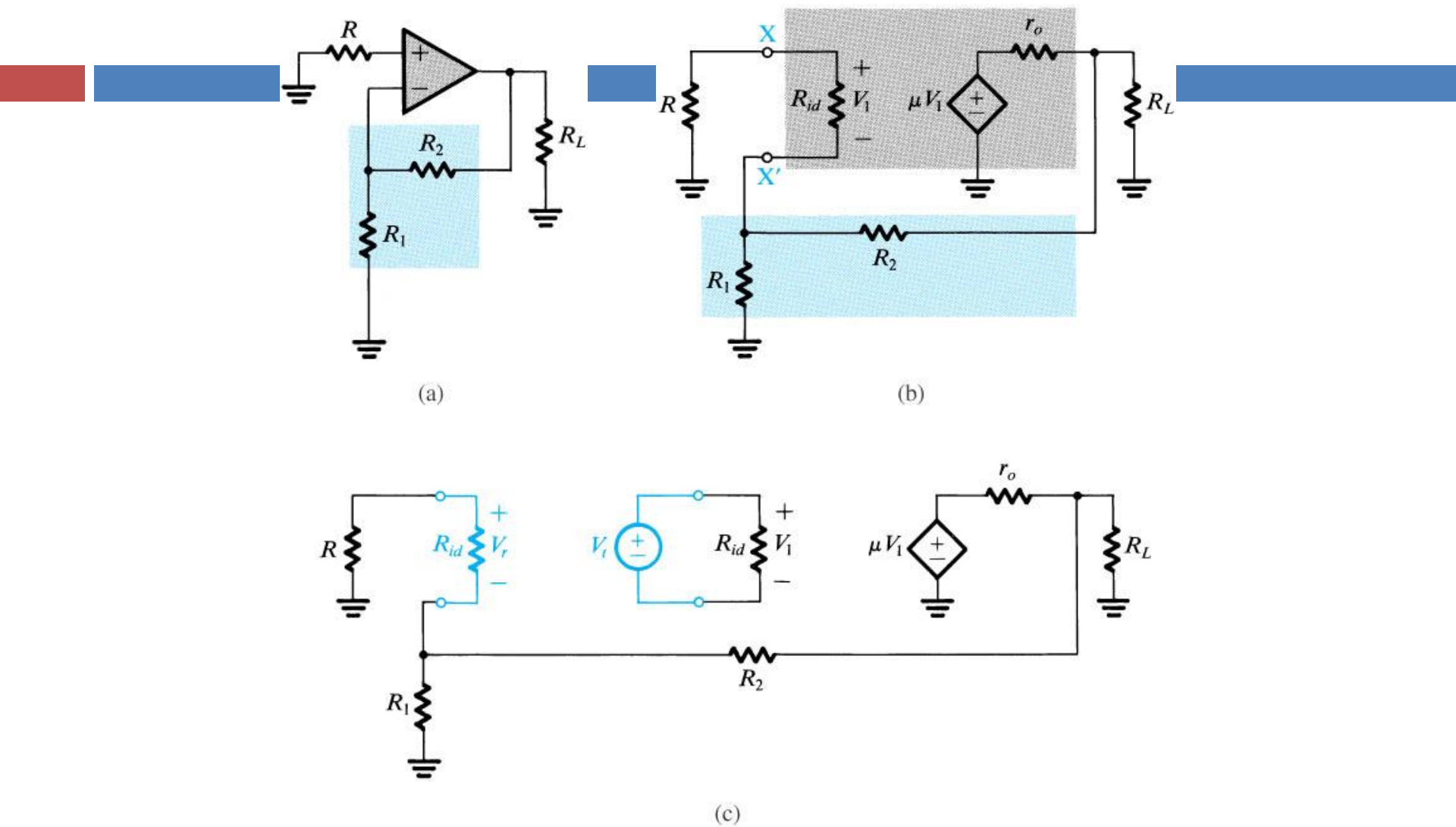


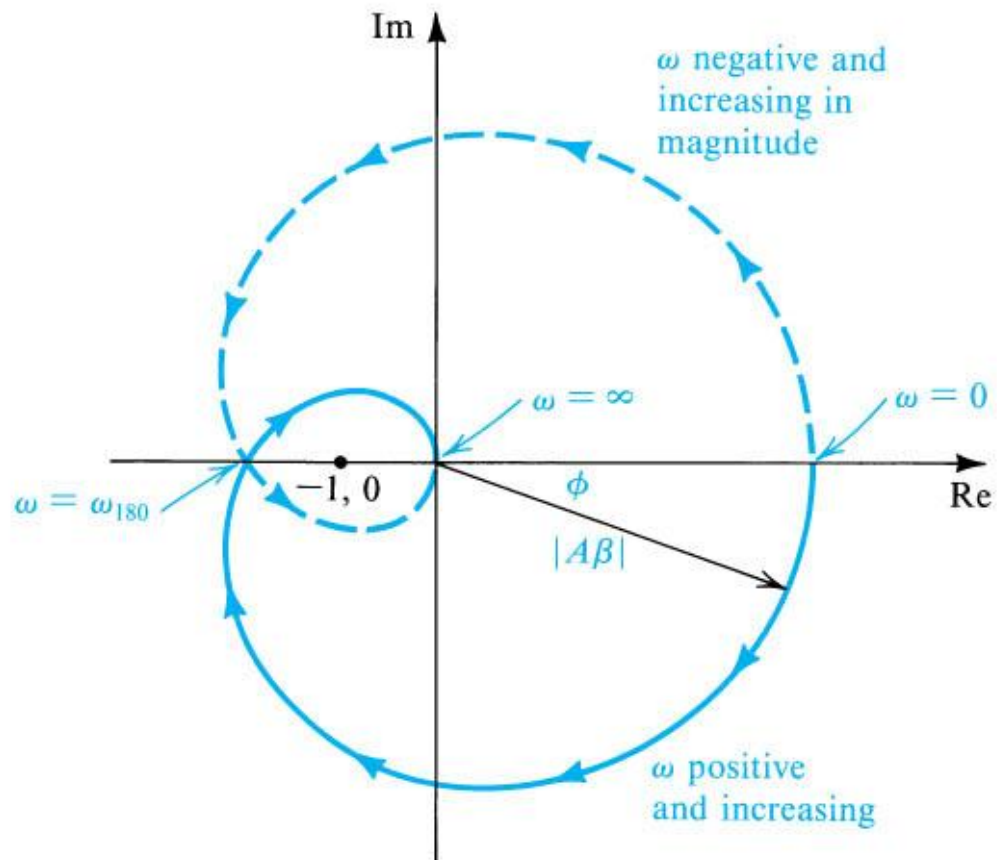
Figure E8.7



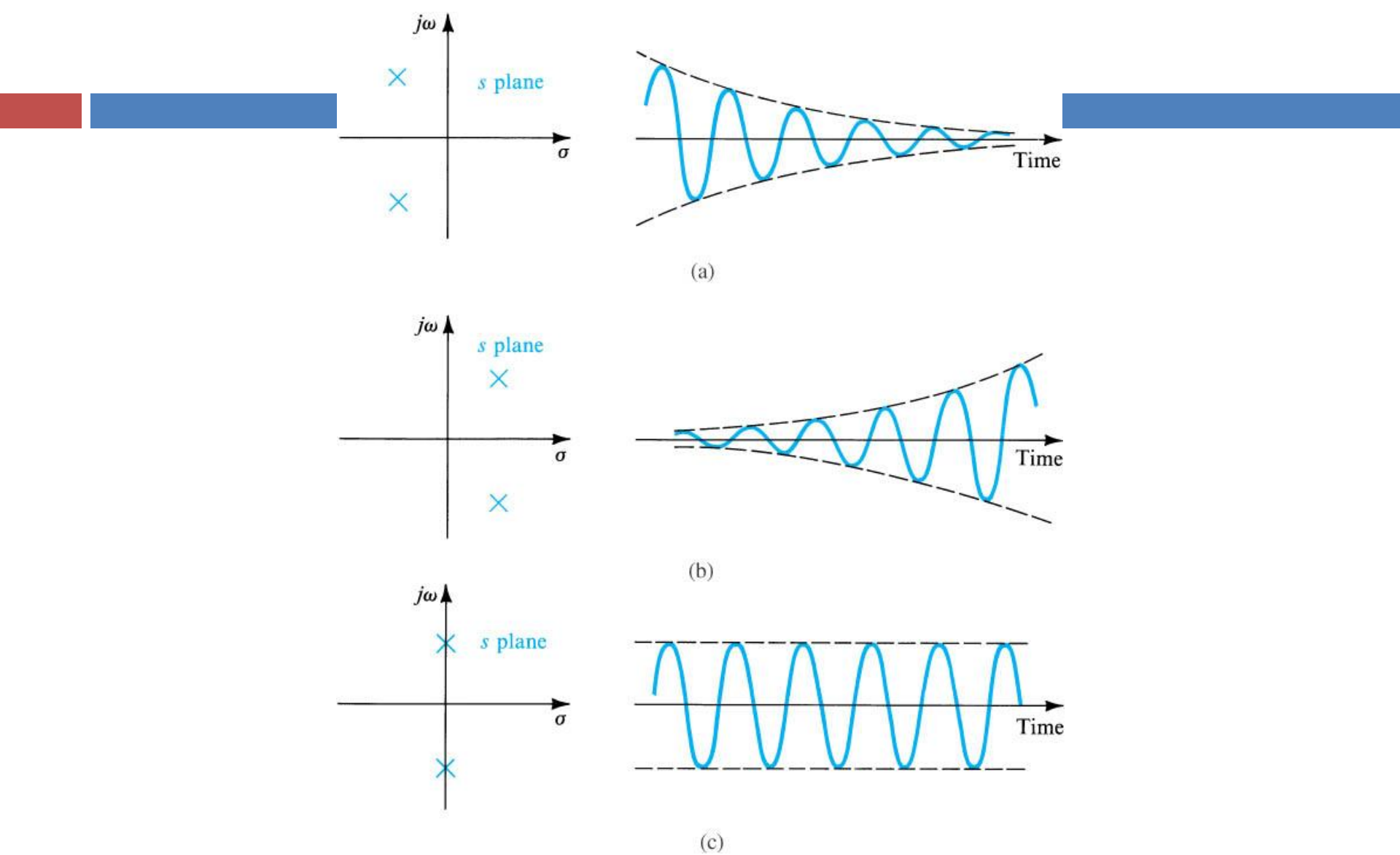
**Figure 8.26** A conceptual feedback loop is broken at  $XX'$  and a test voltage  $V_t$  is applied. The impedance  $Z_t$  is equal to that previously seen looking to the left of  $XX'$ . The loop gain  $A\beta = -V_r/V_t$ , where  $V_r$  is the *returned* voltage. As an alternative,  $A\beta$  can be determined by finding the open-circuit transfer function  $T_{oc}$ , as in (c), and the short-circuit transfer function  $T_{sc}$ , as in (d), and combining them as indicated.



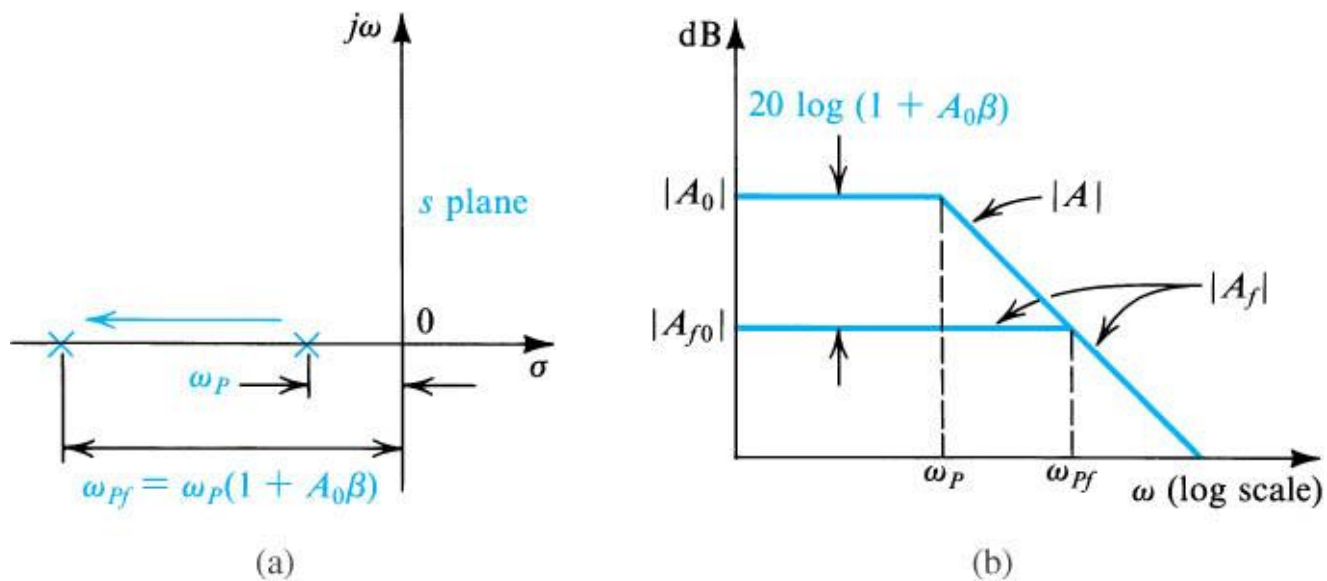
**Figure 8.27** The loop gain of the feedback loop in (a) is determined in (b) and (c).



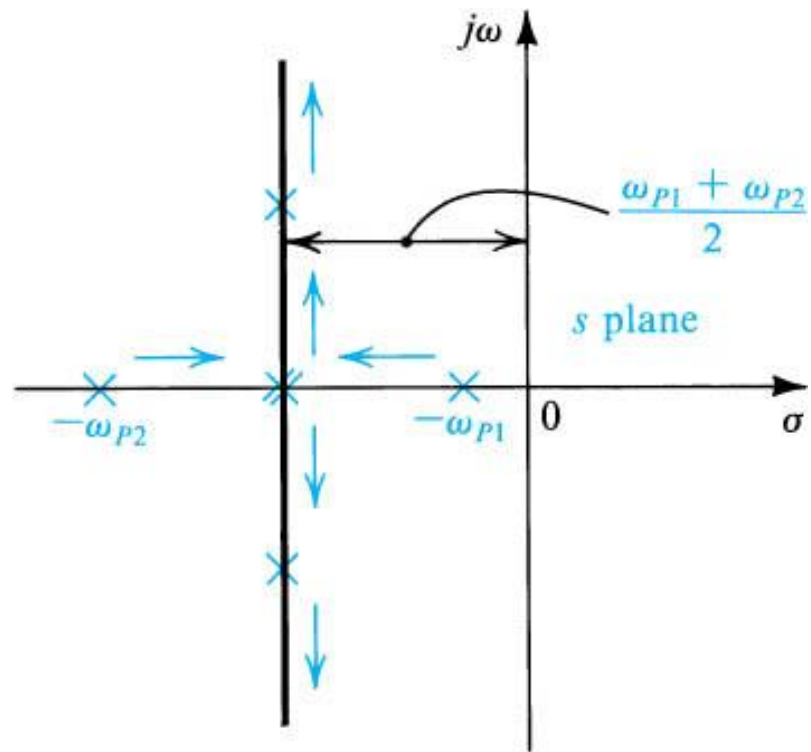
**Figure 8.28** The Nyquist plot of an unstable amplifier.



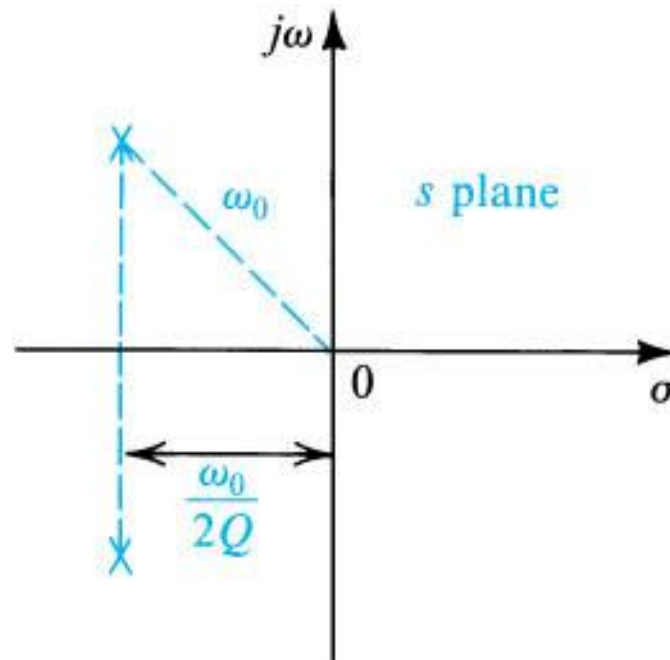
**Figure 8.29** Relationship between pole location and transient response.



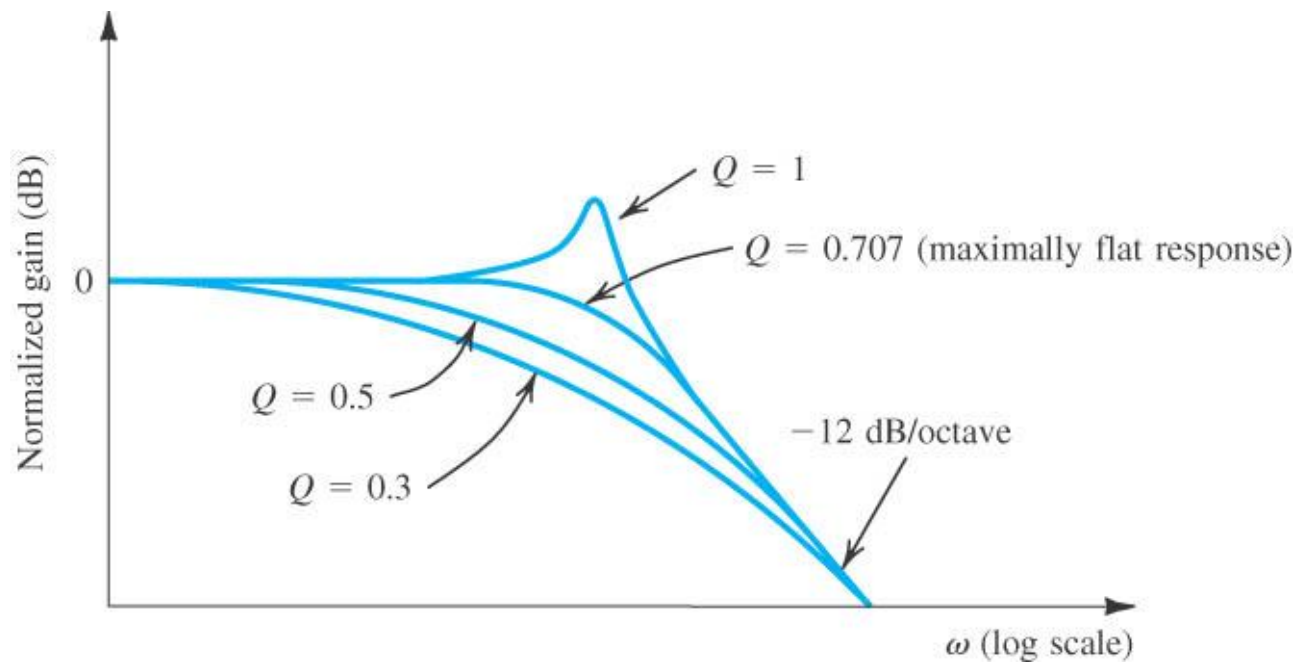
**Figure 8.30** Effect of feedback on (a) the pole location and (b) the frequency response of an amplifier having a single-pole open-loop response.



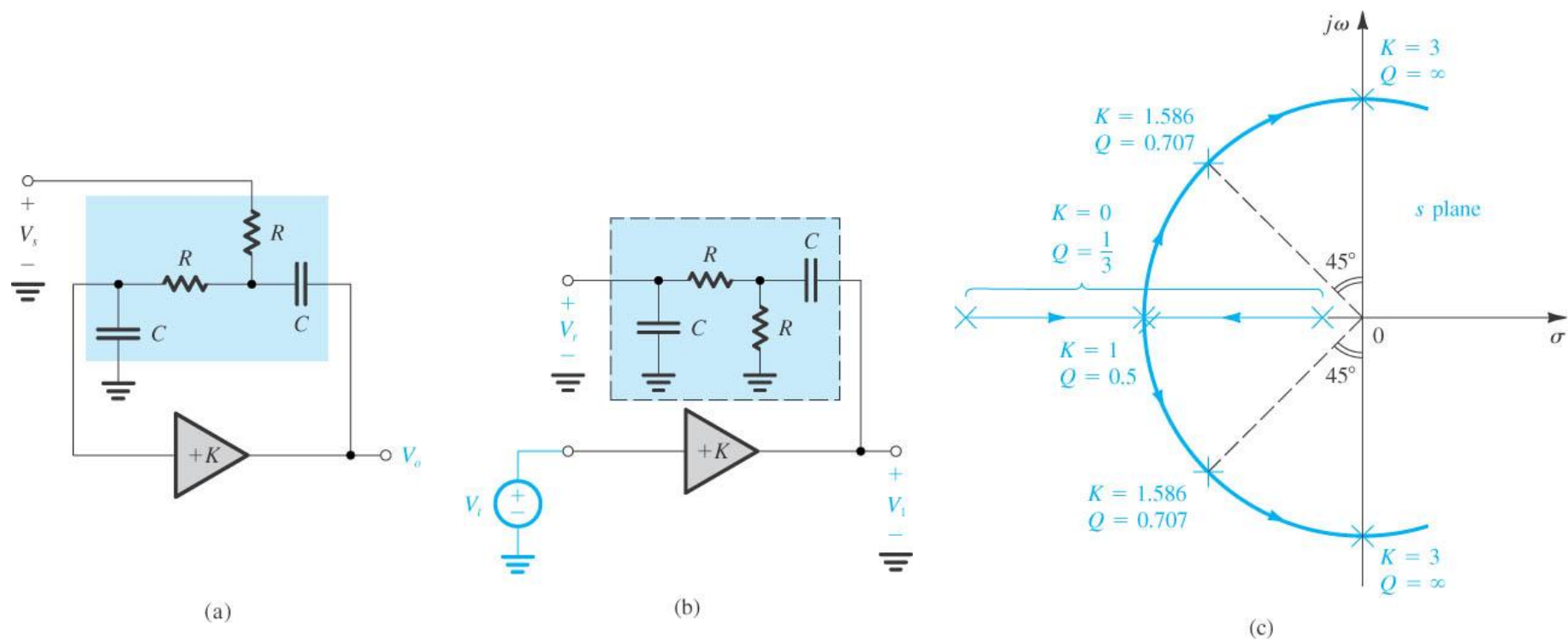
**Figure 8.31** Root-locus diagram for a feedback amplifier whose open-loop transfer function has two real poles.



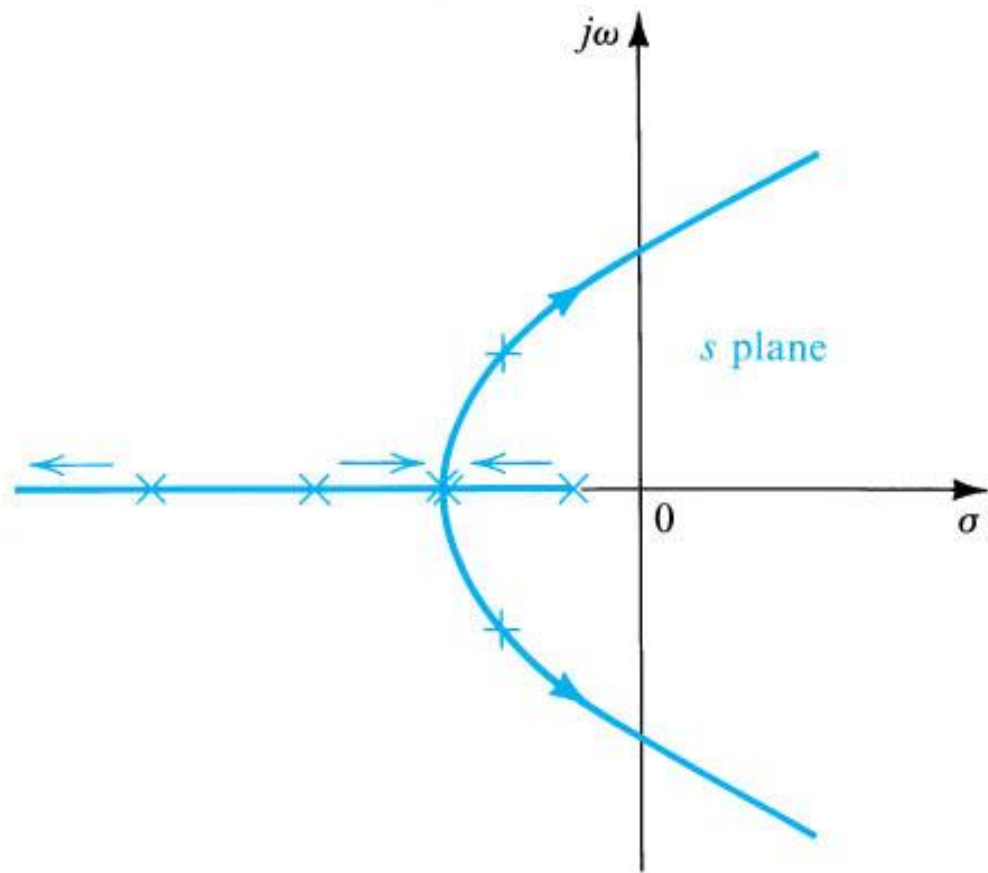
**Figure 8.32** Definition of  $\omega_0$  and  $Q$  of a pair of complex-conjugate poles.



**Figure 8.33** Normalized gain of a two-pole feedback amplifier for various values of  $Q$ . Note that  $Q$  is determined by the loop gain according to Eq. (8.65).



**Figure 8.34** Circuits and plot for Example 8.5.



**Figure 8.35** Root-locus diagram for an amplifier with three poles. The arrows indicate the pole movement as  $A_0\beta$  is increased.

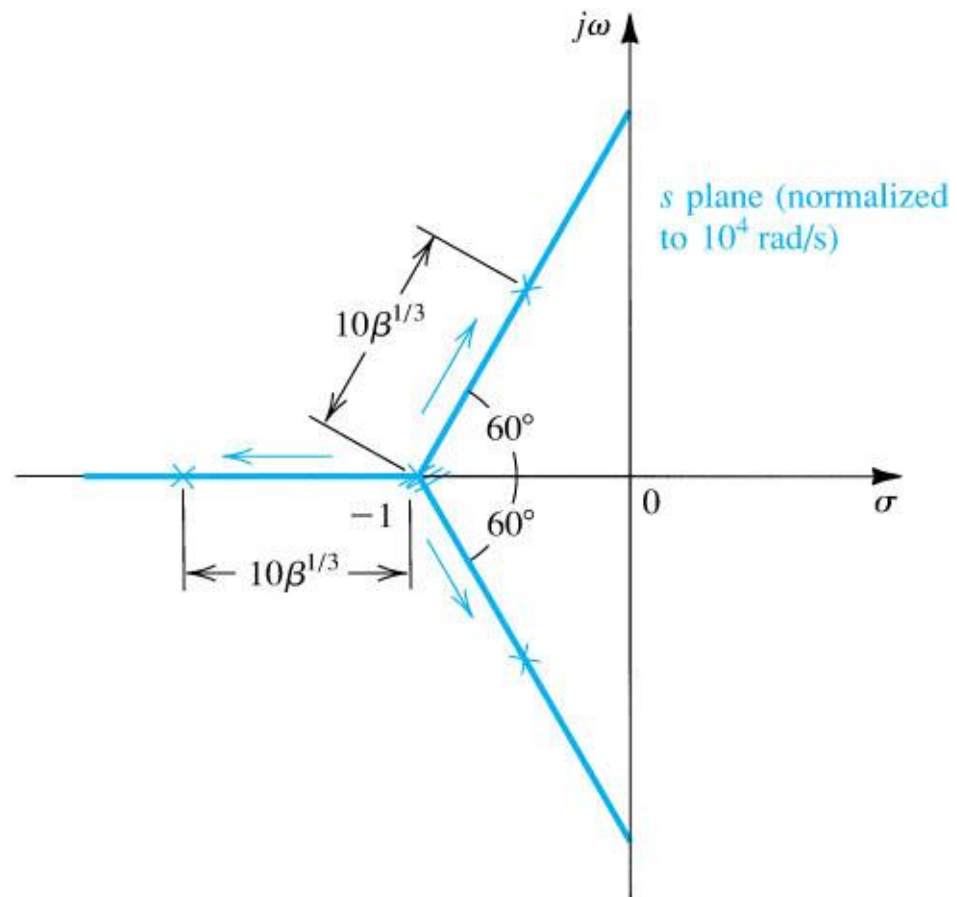
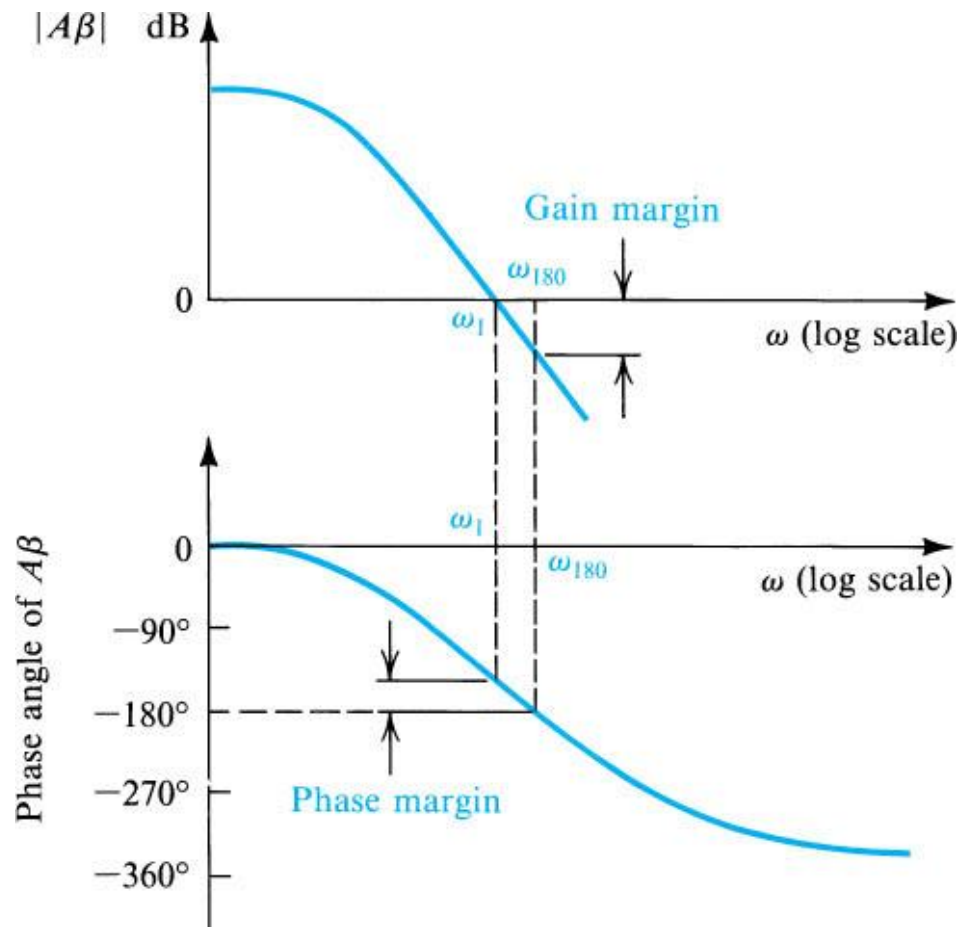
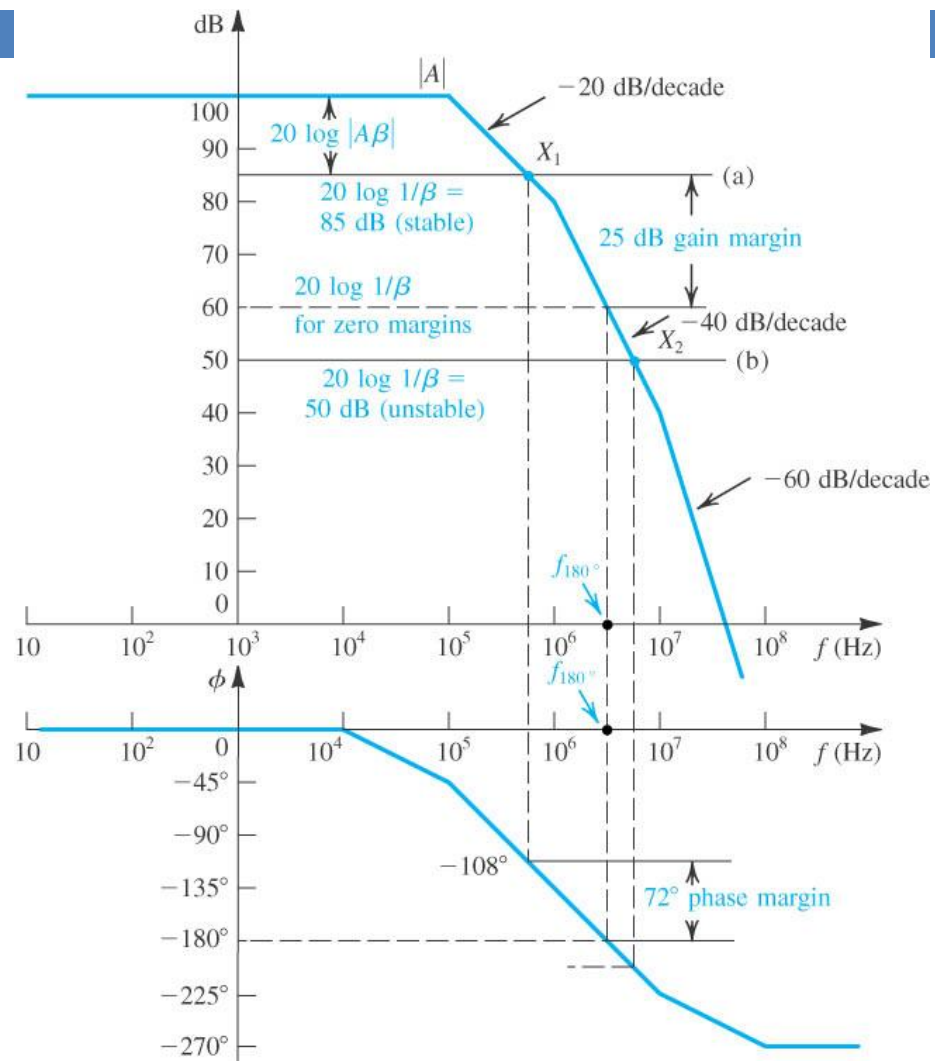


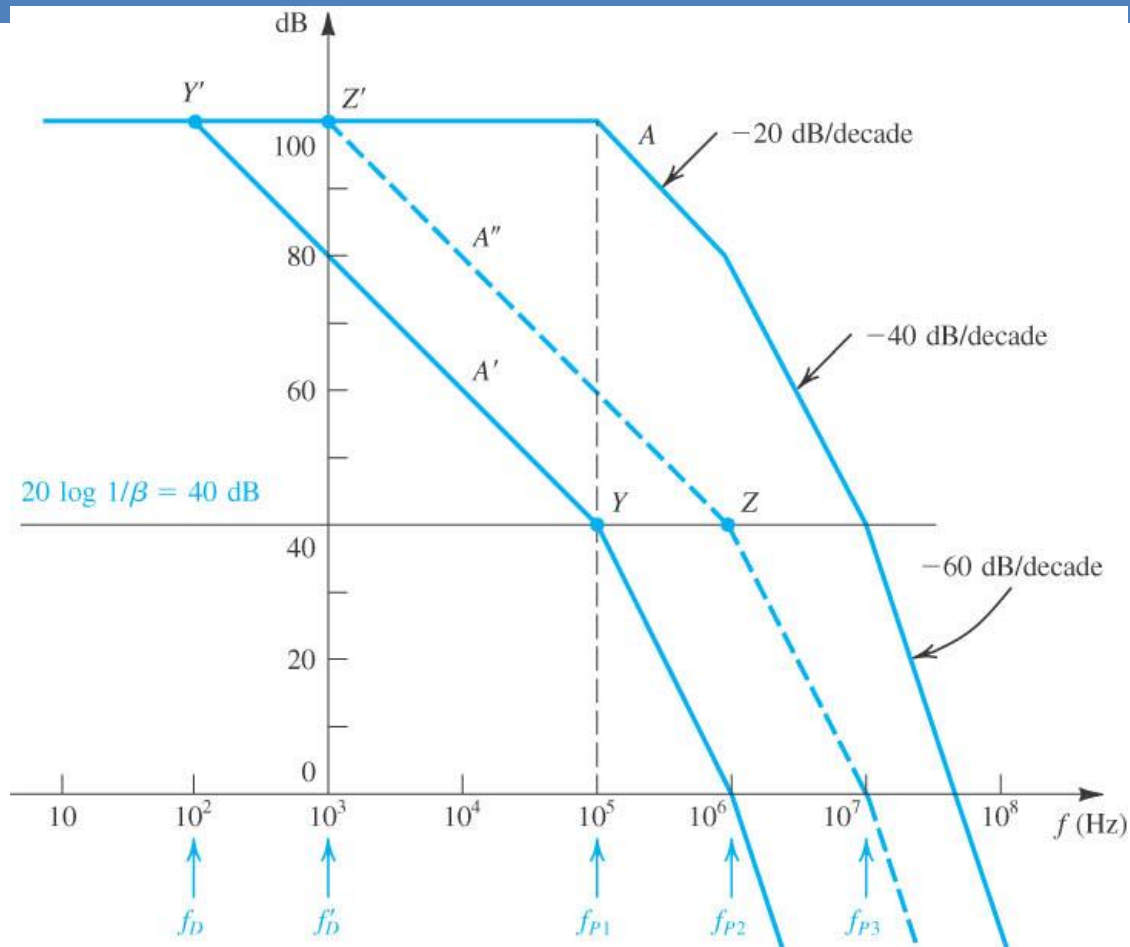
Figure E8.13



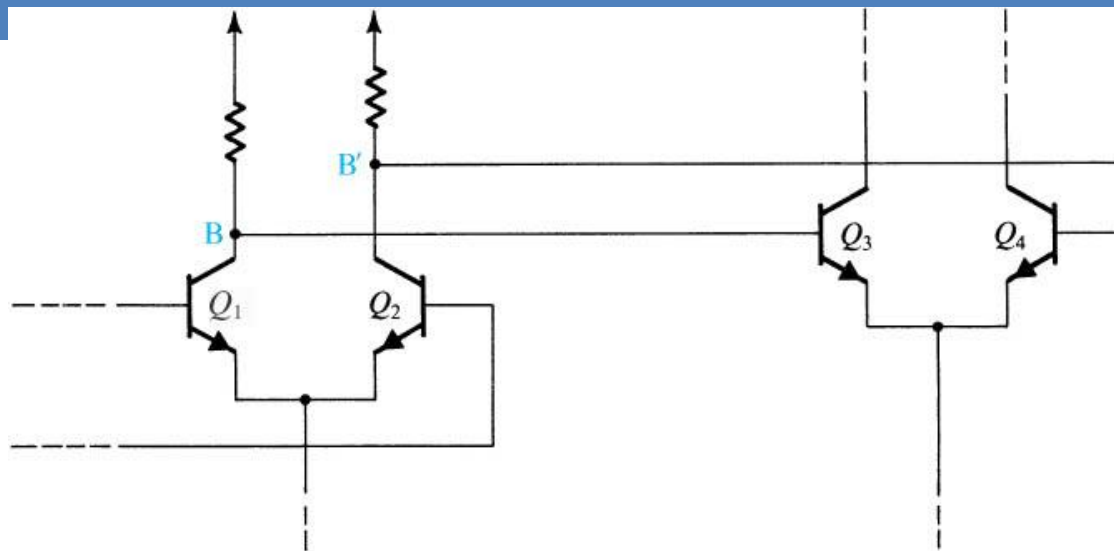
**Figure 8.36** Bode plot for the loop gain  $A\beta$  illustrating the definitions of the gain and phase margins.



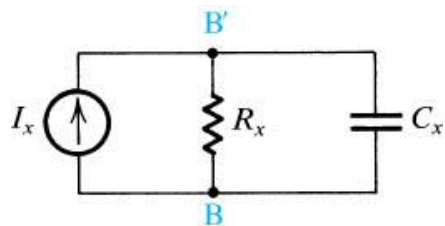
**Figure 8.37** Stability analysis using Bode plot of  $|A|$ .



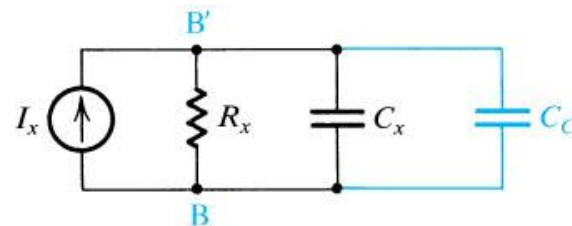
**Figure 8.38** Frequency compensation for  $\beta = 10^{-2}$ . The response labeled  $A'$  is obtained by introducing an additional pole at  $f_D$ . The  $A''$  response is obtained by moving the original low-frequency pole to  $f'_D$ .



(a)

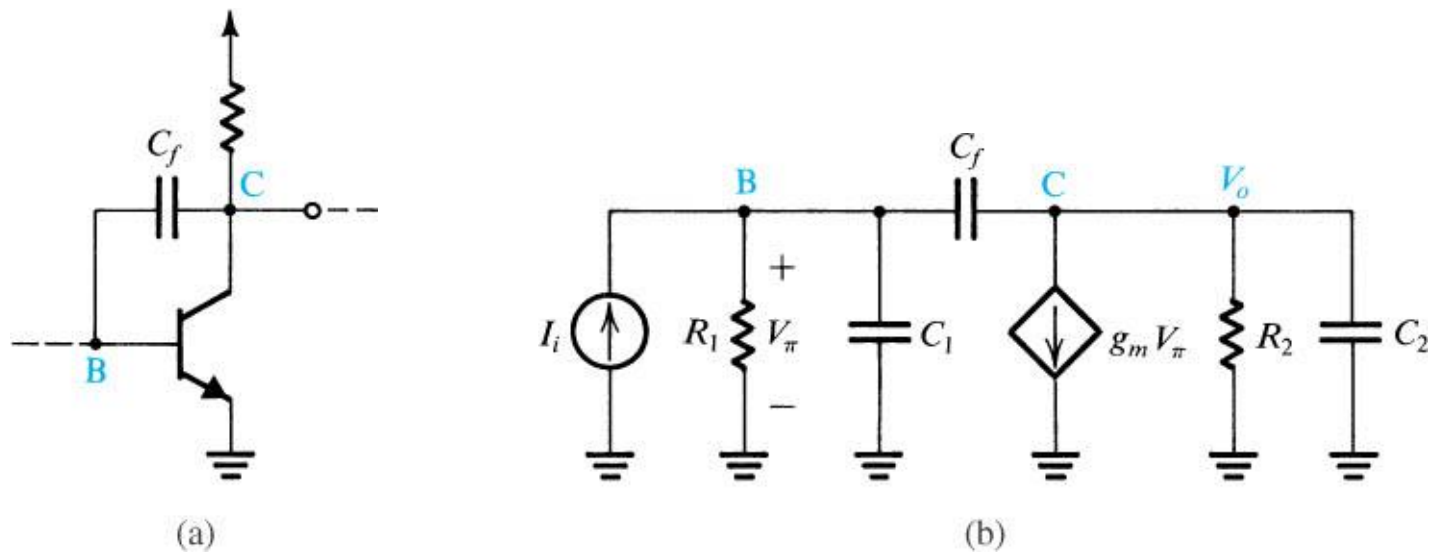


(b)

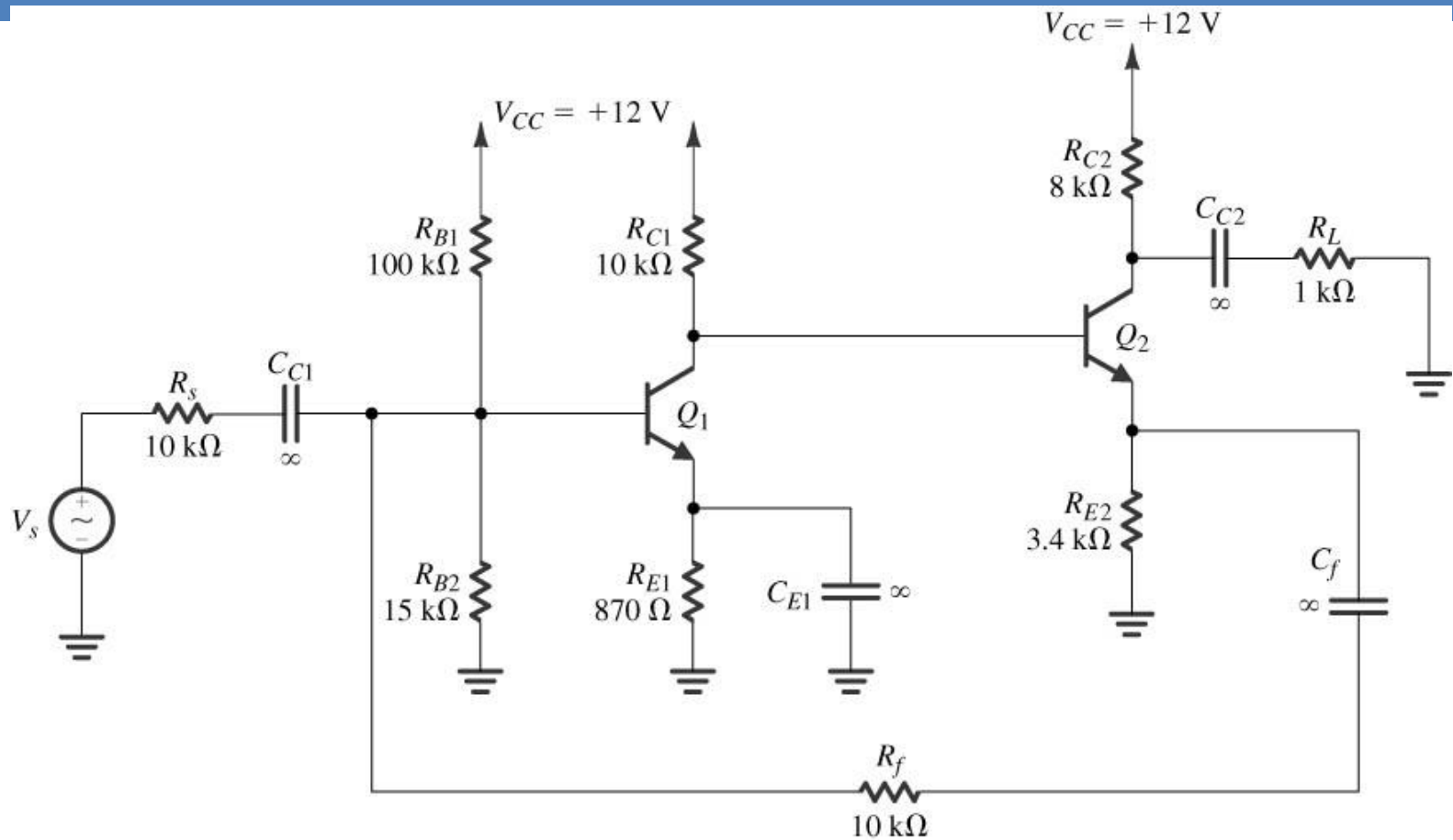


(c)

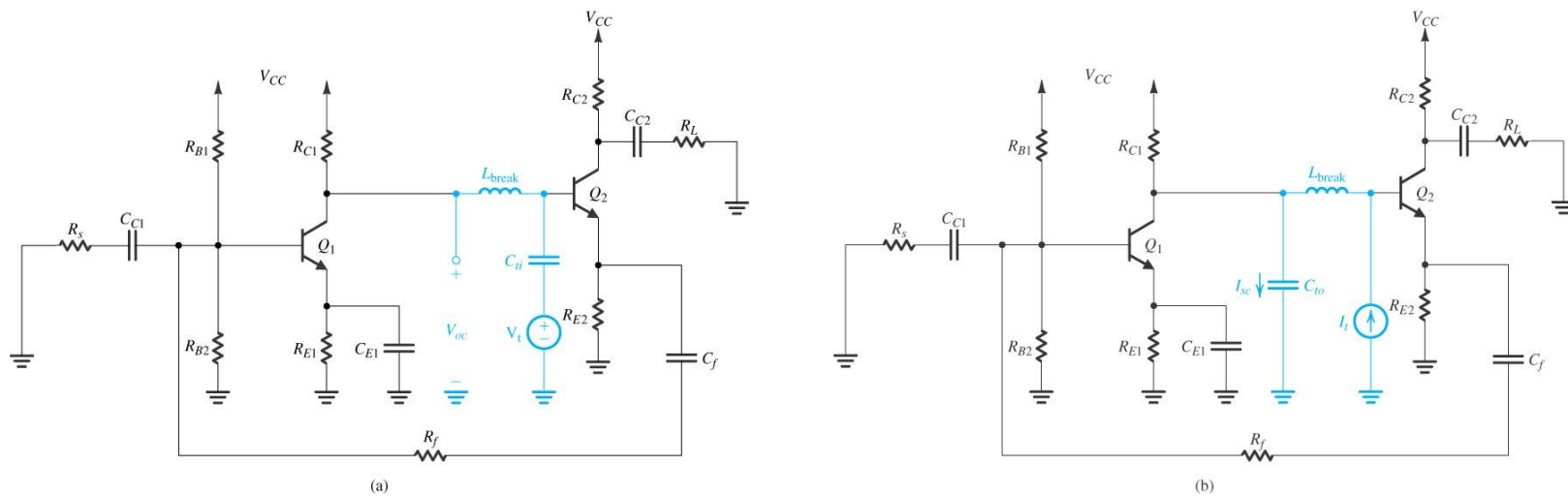
**Figure 8.39** (a) Two cascaded gain stages of a multistage amplifier. (b) Equivalent circuit for the interface between the two stages in (a). (c) Same circuit as in (b) but with a compensating capacitor  $C_C$  added. Note that the analysis here applies equally well to MOS amplifiers.



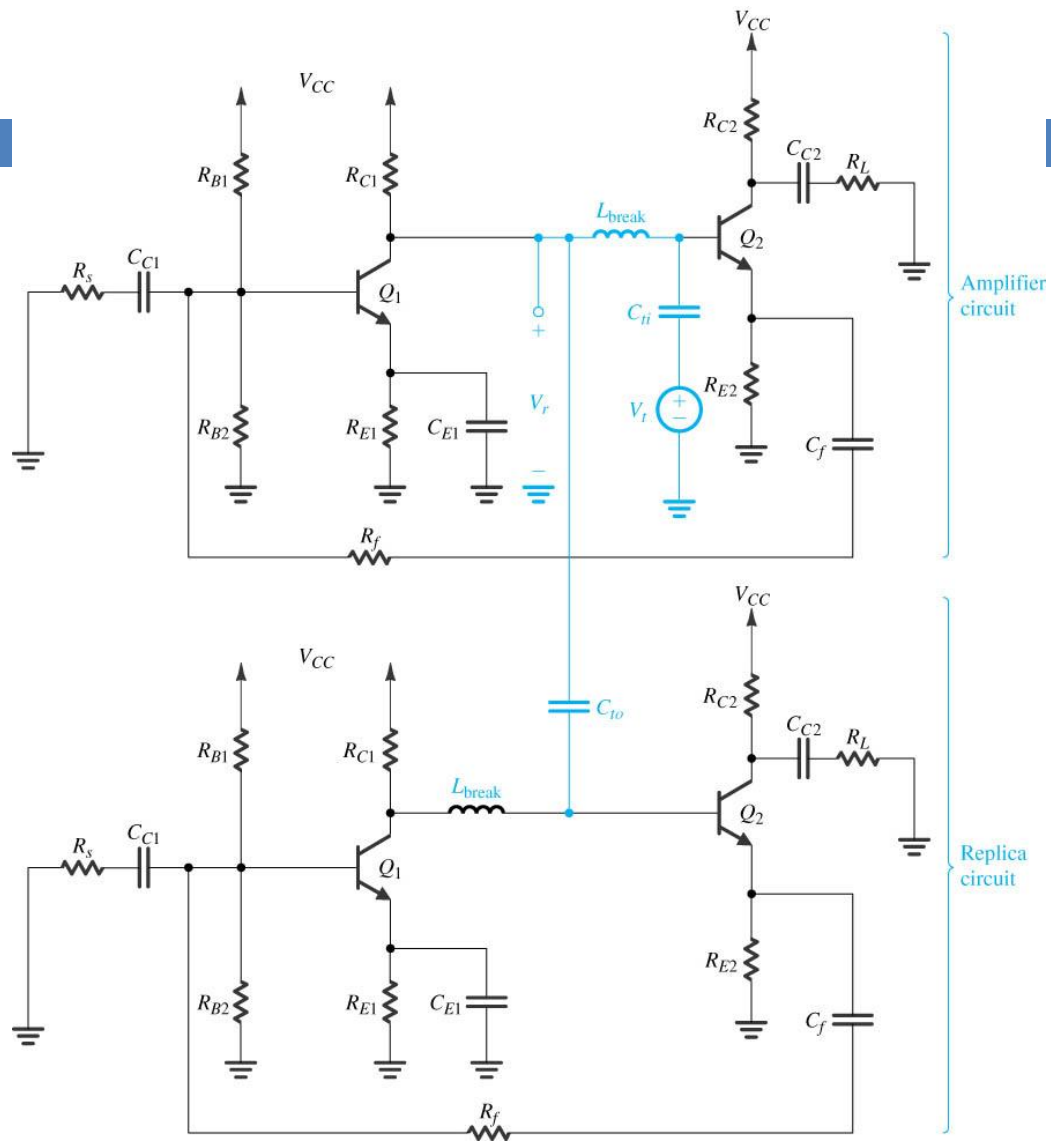
**Figure 8.40** (a) A gain stage in a multistage amplifier with a compensating capacitor connected in the feedback path and (b) an equivalent circuit. Note that although a BJT is shown, the analysis applies equally well to the MOSFET case.



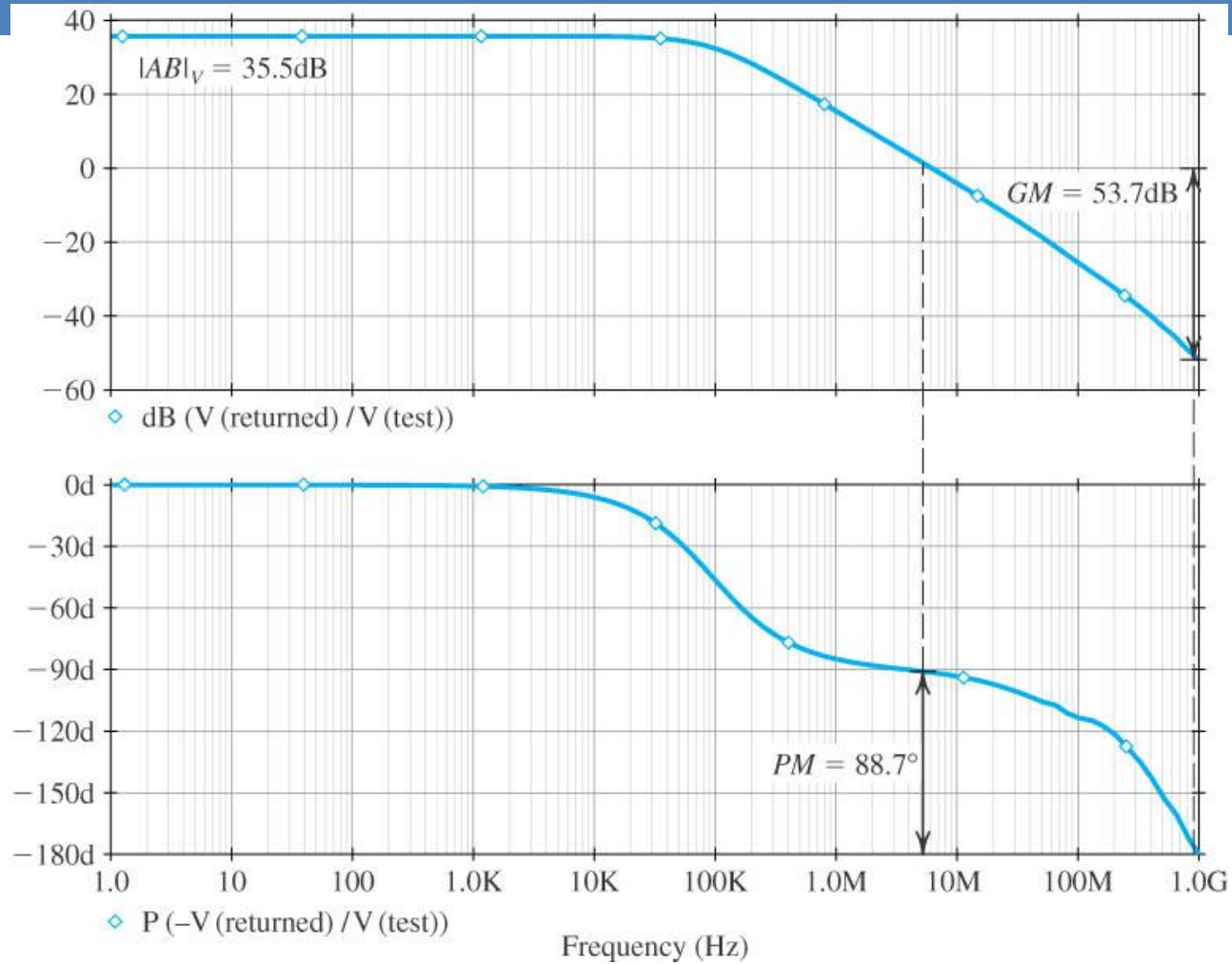
**Figure 8.41** Circuit of the shunt-series feedback amplifier in Example 8.4.



**Figure 8.42** Circuits for simulating (a) the open-circuit voltage transfer function  $T_{oc}$  and (b) the short-circuit current transfer function  $T_{sc}$  of the feedback amplifier in Fig. 8.41 for the purpose of computing its loop gain.



**Figure 8.43** Circuit for simulating the loop gain of the feedback amplifier circuit in Fig. 8.41 using the replica-circuit method.



**Figure 8.44** (a) Magnitude and (b) phase of the loop gain  $A\beta$  of the feedback amplifier circuit in Fig. 8.41.

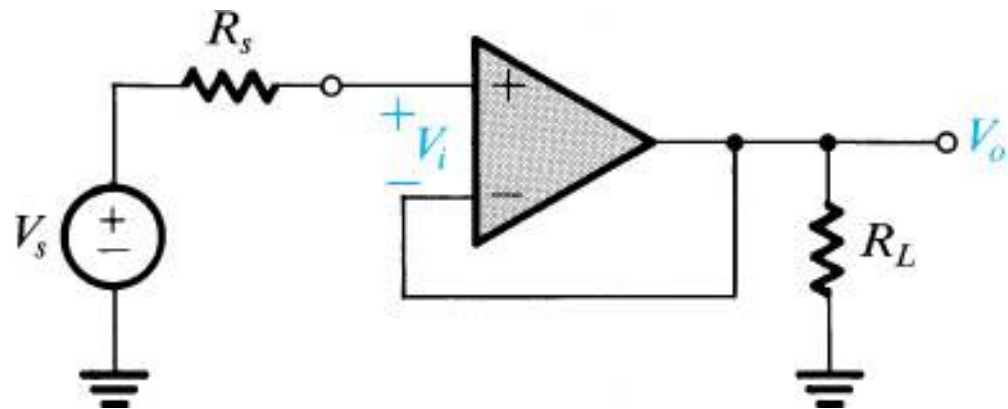


Figure P8.4

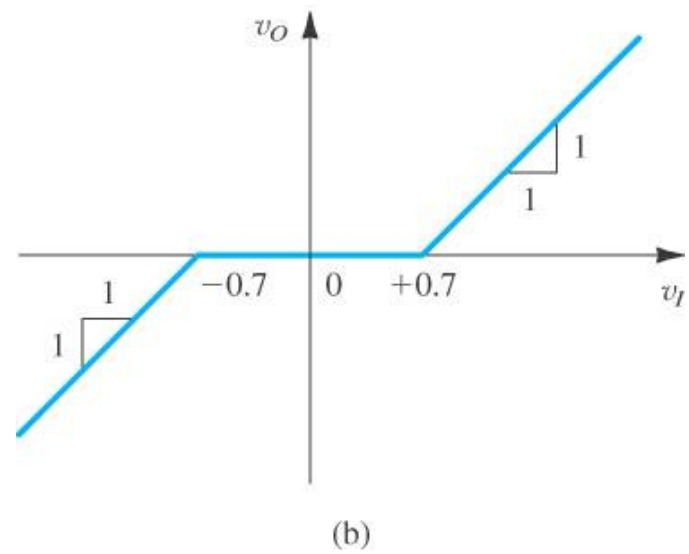
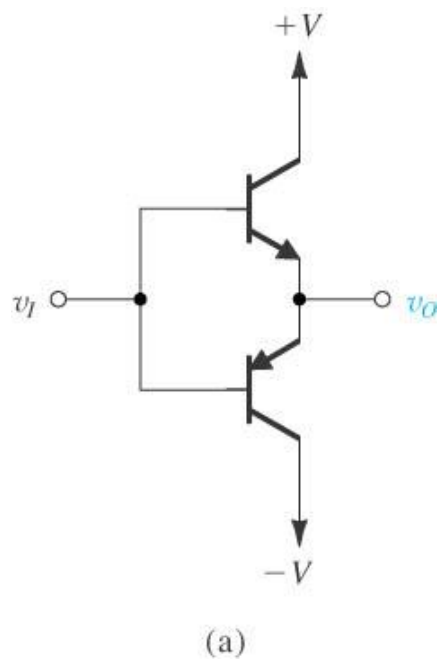


Figure P8.19

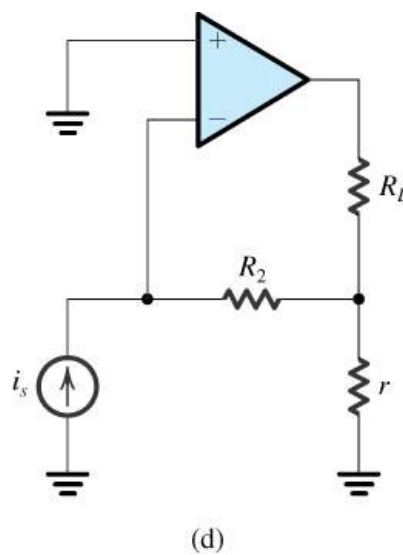
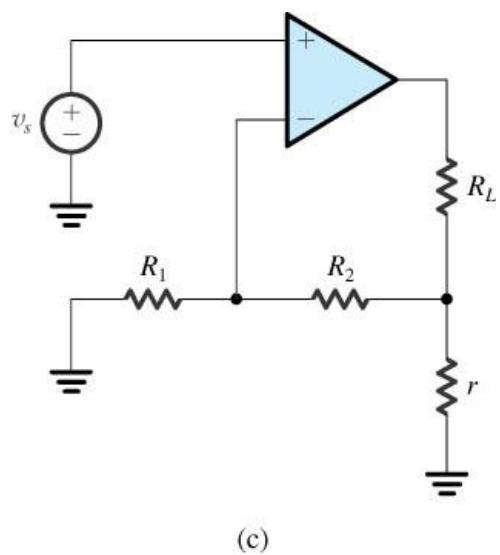
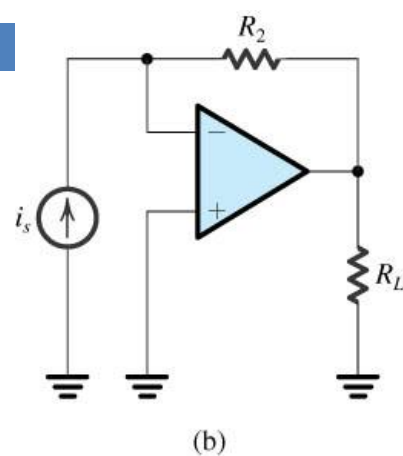
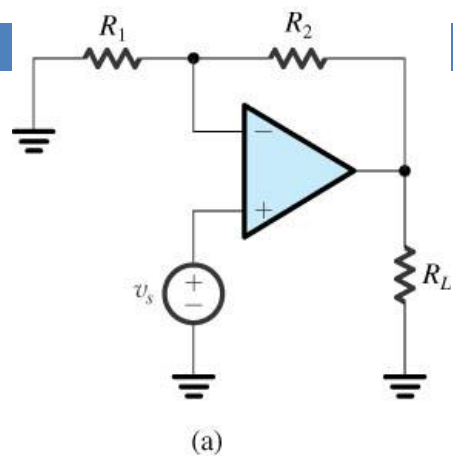


Figure P8.26

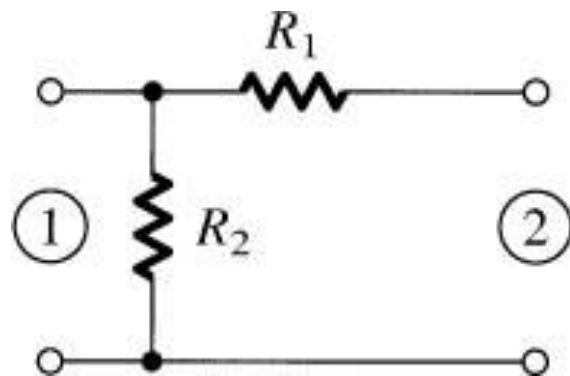


Figure P8.30

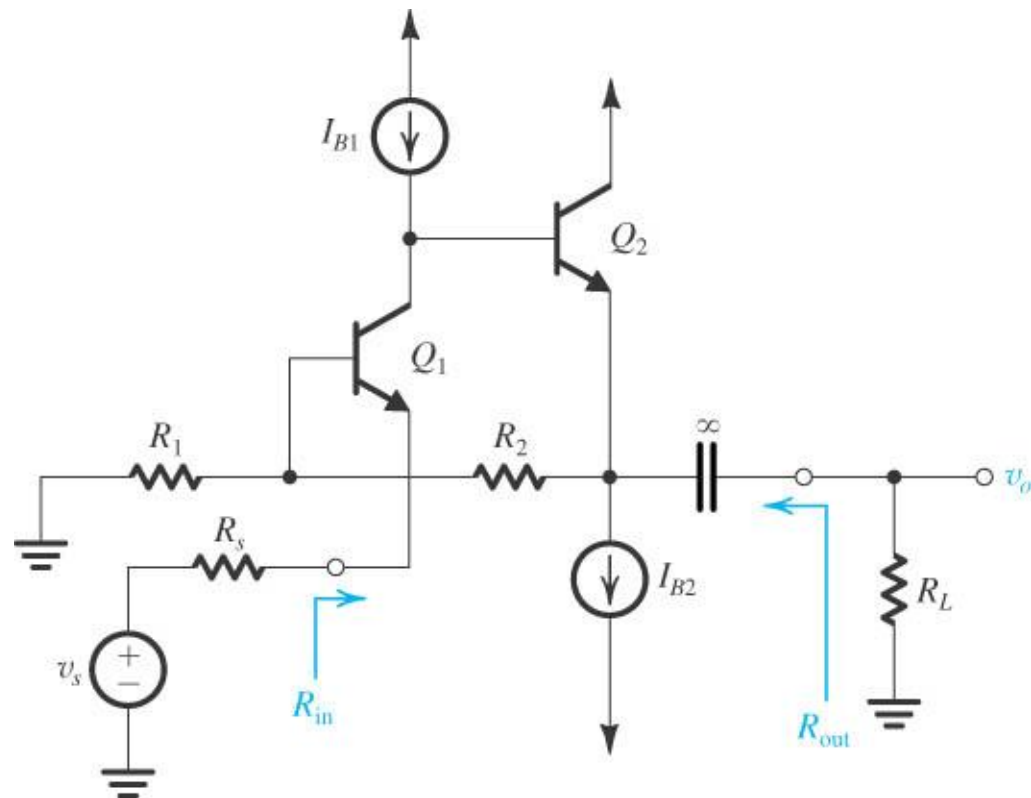


Figure P8.32

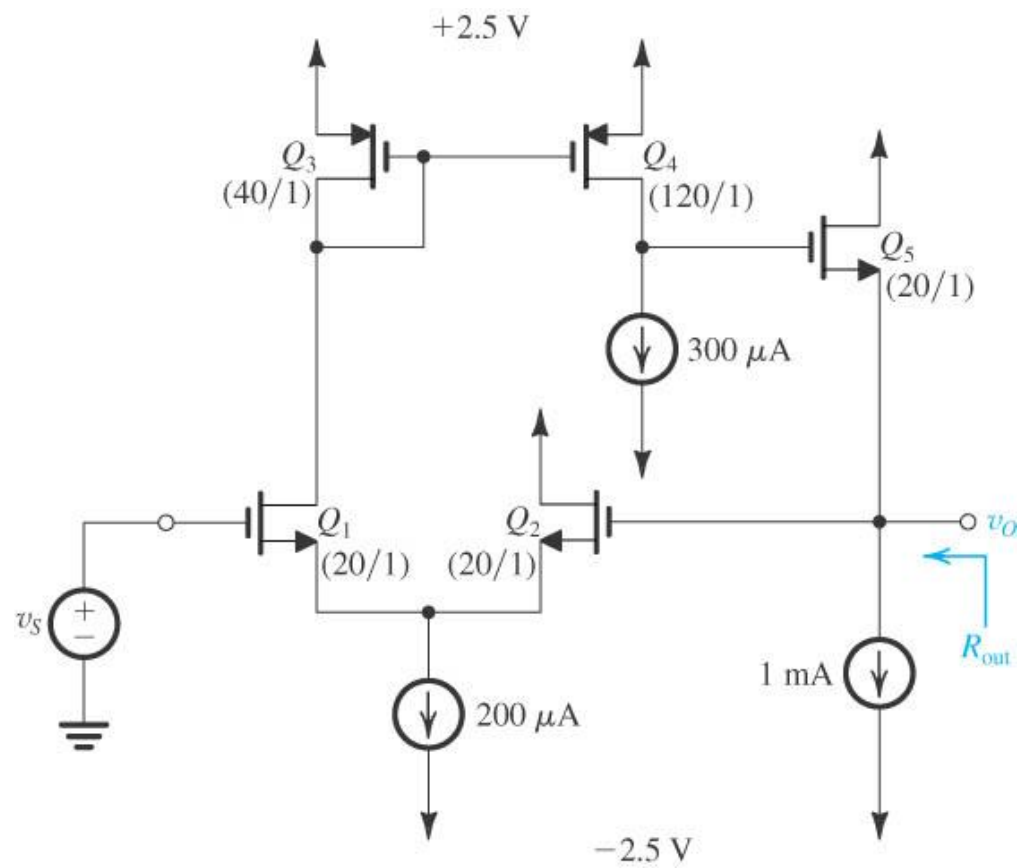


Figure P8.33

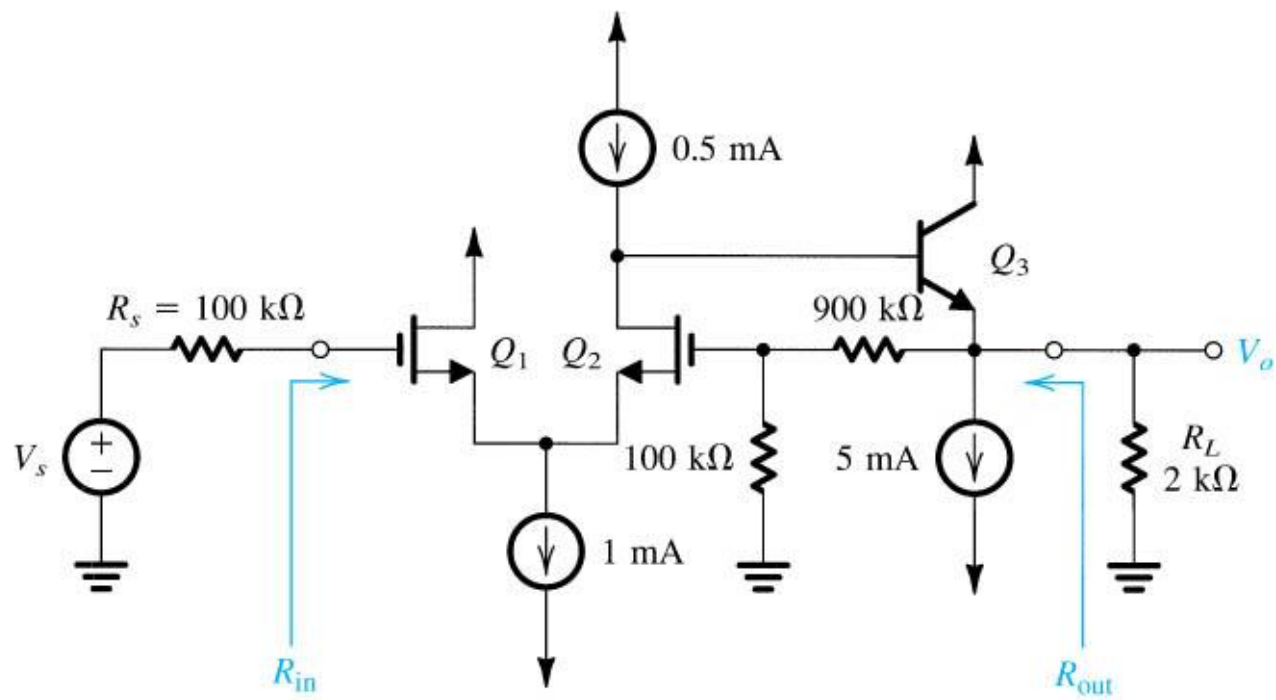


Figure P8.34

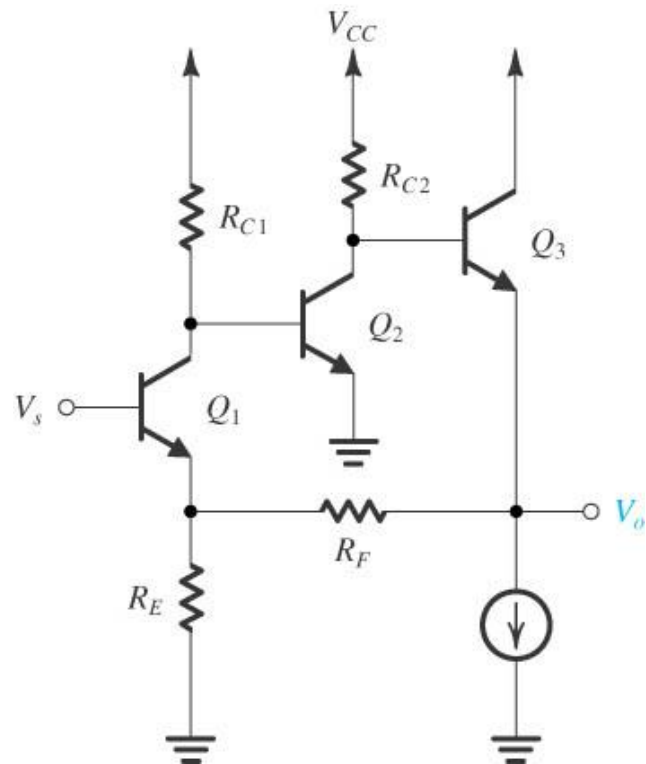


Figure P8.35

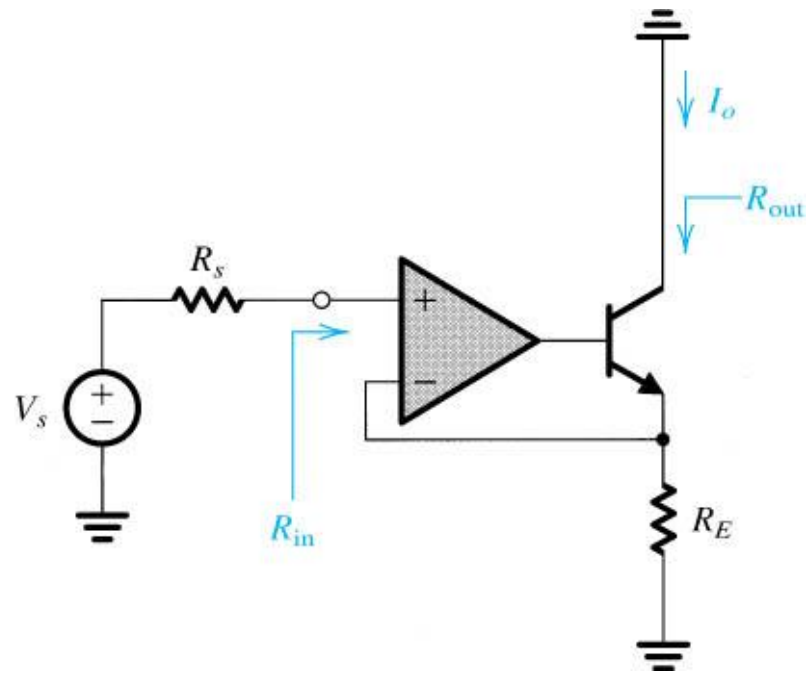


Figure P8.38

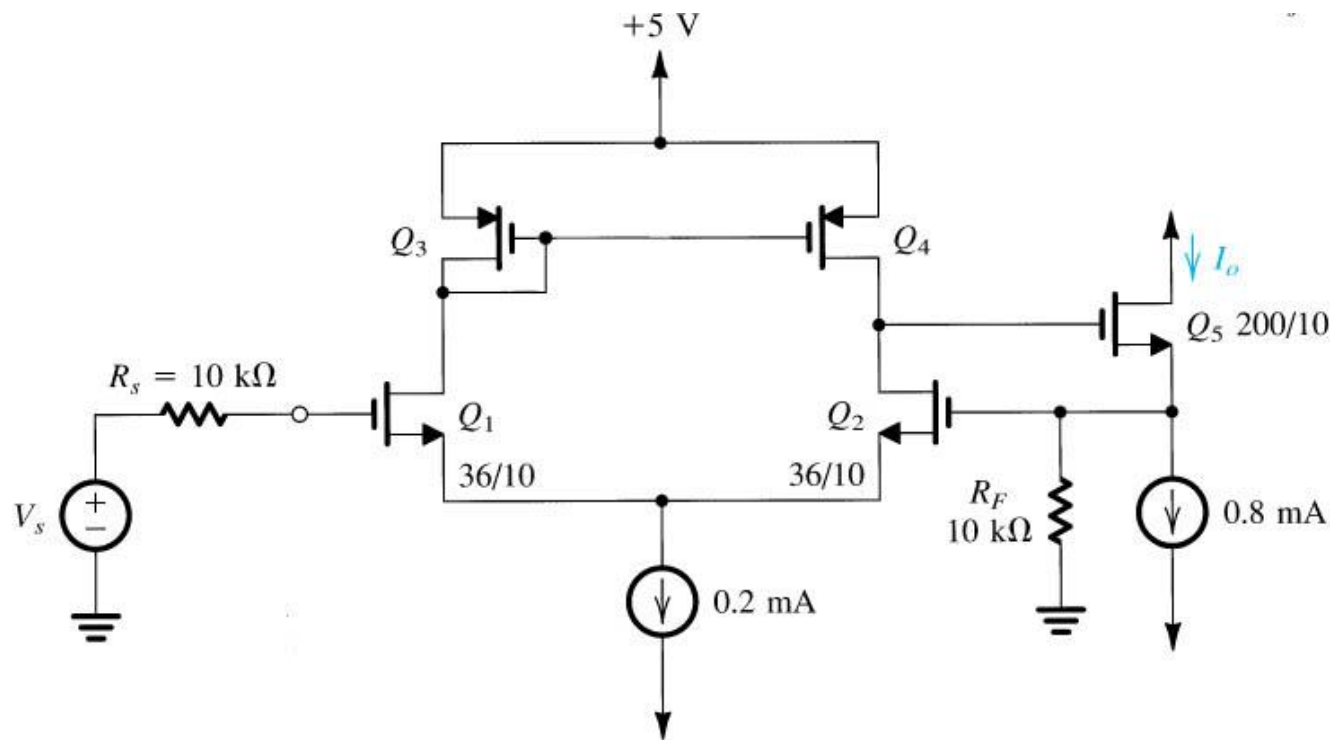


Figure P8.39

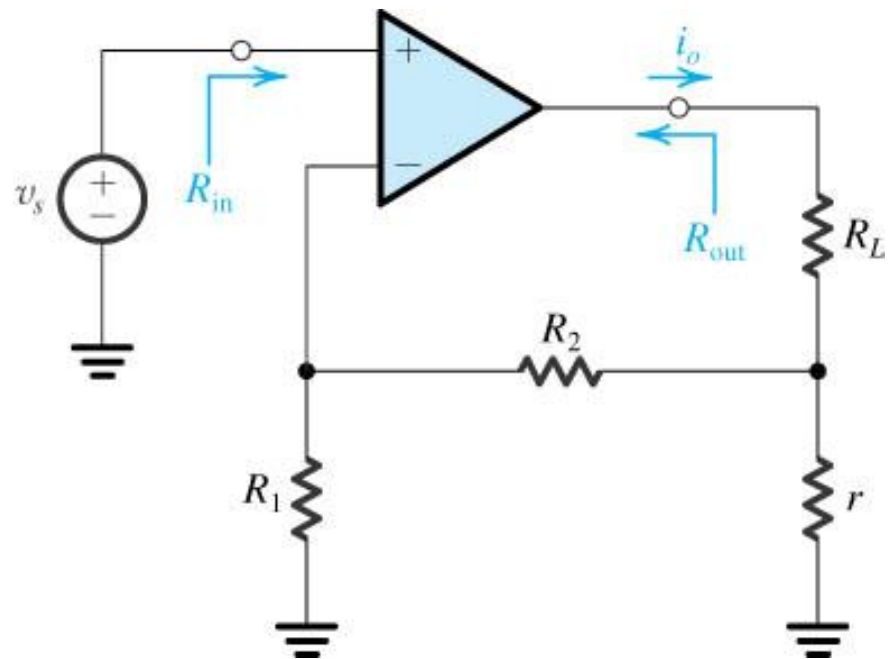


Figure P8.40

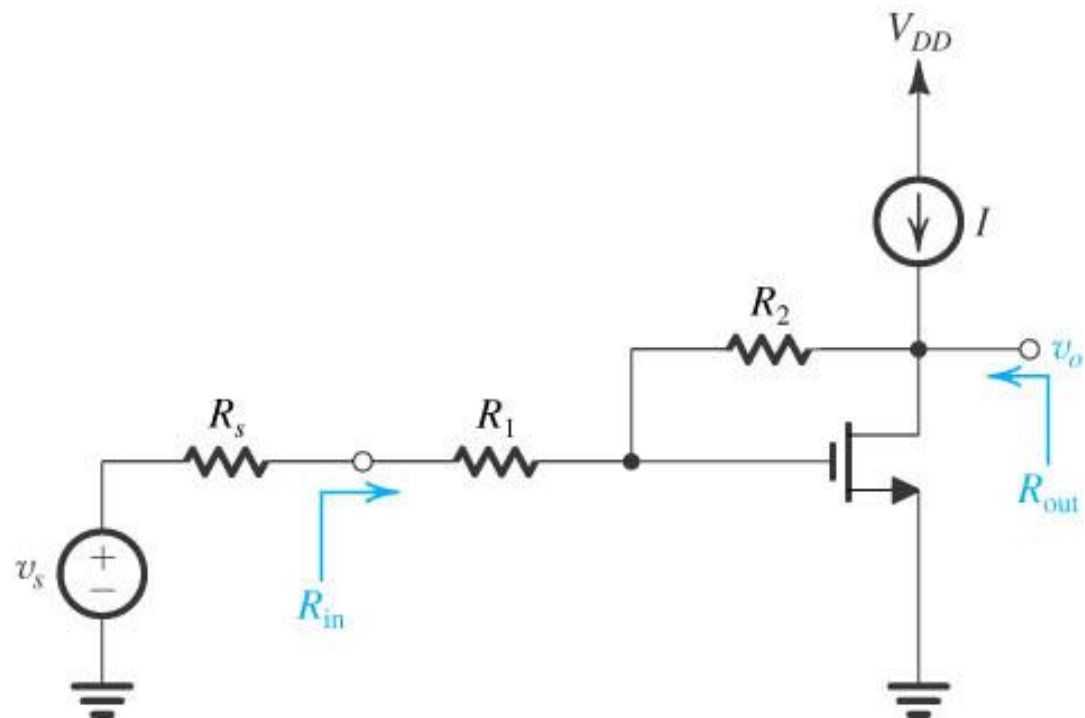


Figure P8.42

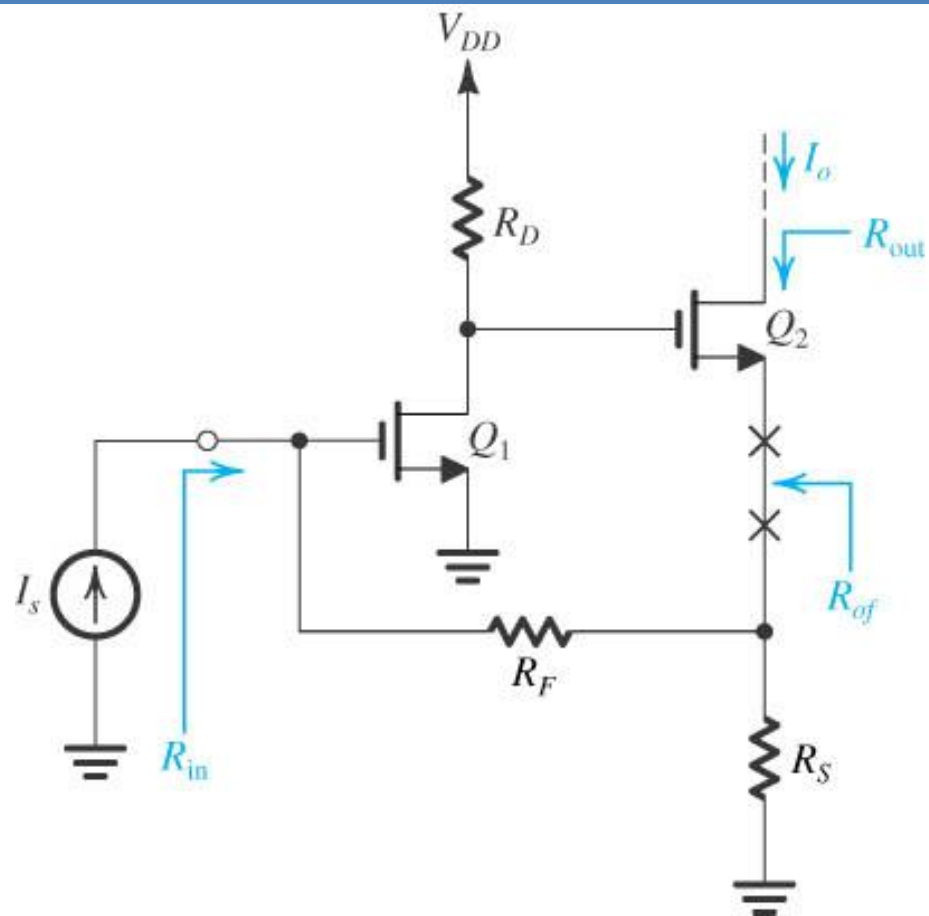


Figure P8.44

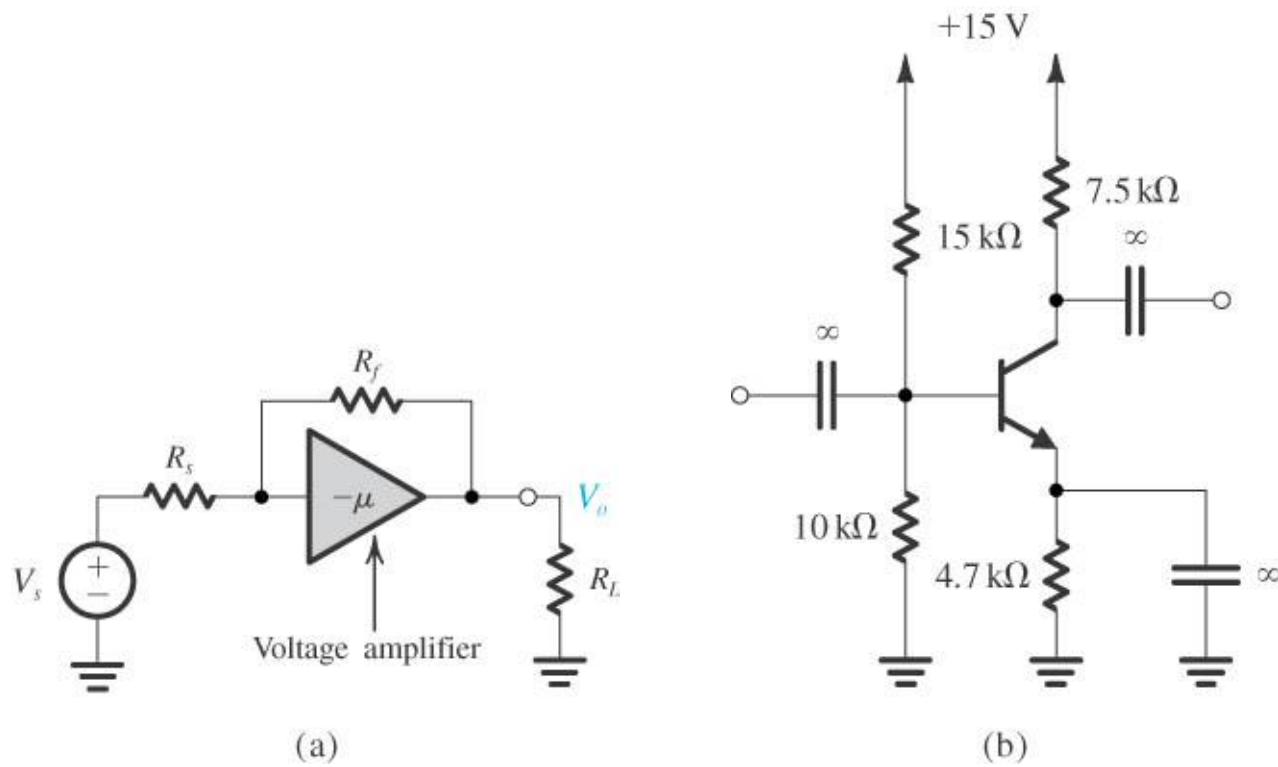


Figure P8.46

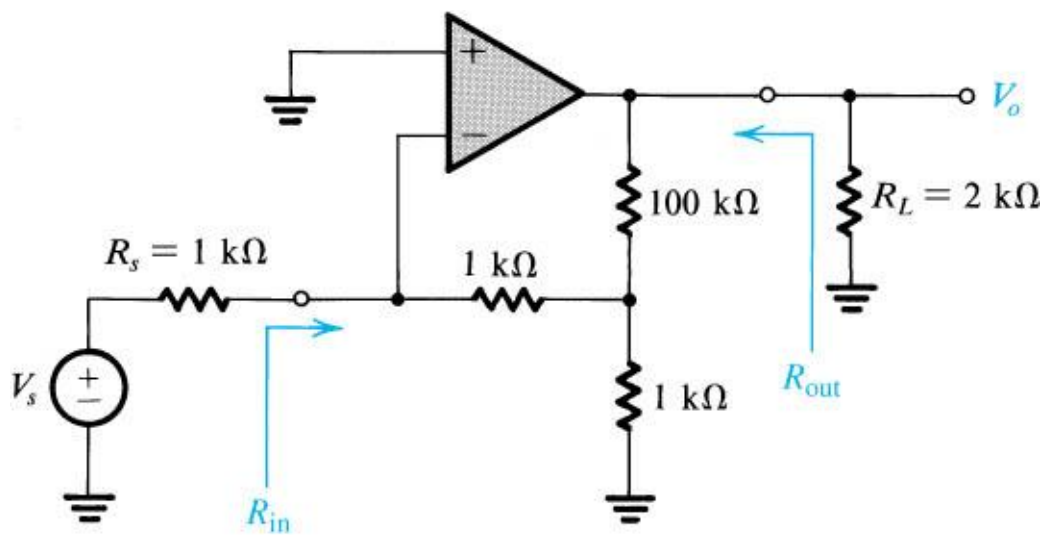


Figure P8.48

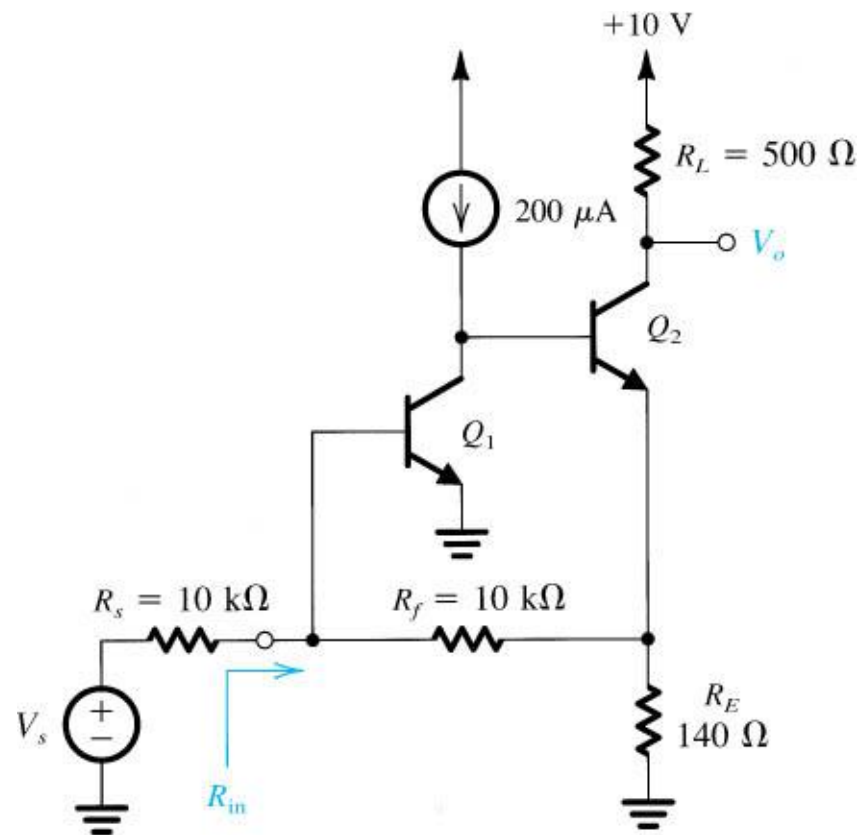


Figure P8.51

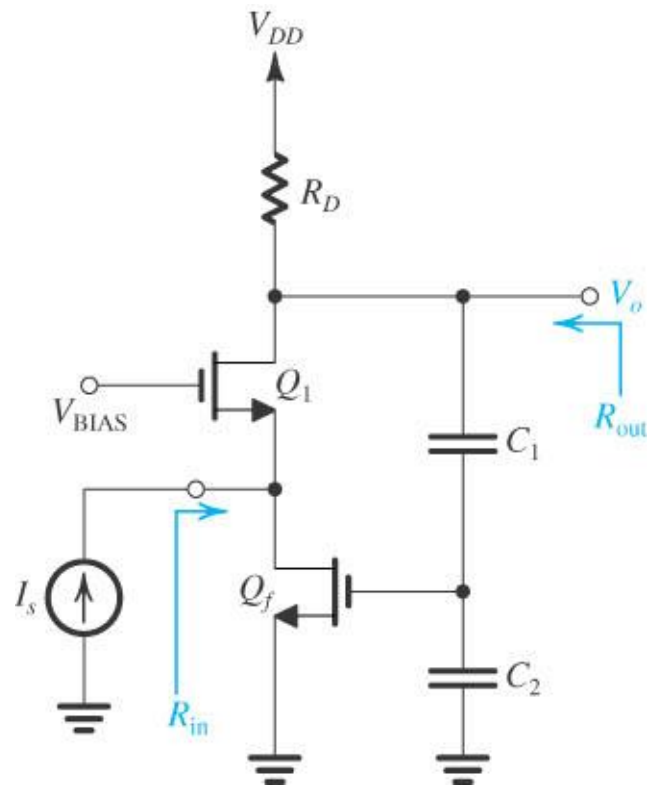


Figure P8.52

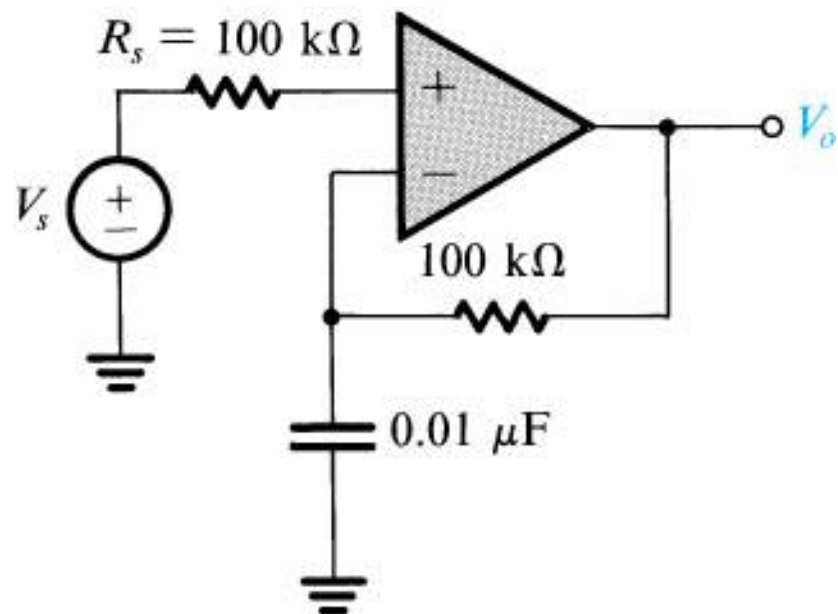


Figure P8.81