First Name:_____ Last Name: _____

Problem 1 (20 Points)

A 8G X 32 memory system is design using 1 G X 8 chips. Assume chip failure modes are single-bit cell (45%), single-row all-0's (30%), single-column all-0's (15%), and whole-chip all-0's (10%). Also, assume 0 and 1 values are equally likely. Compare and comment on relative performance (single-error-detection coverage) and overhead of the following approaches.

- a. Bit per chip
- b. Bit per multiple chips
- c. Duplication
- d. Single precision checksum (one sum for the entire memory).

Problem 2 (30 Points)

Consider a random-access memory that has a 6-bit data.

- a. Determine the H matrix such that the error code computed by your Single Error Correcting Hamming code specifies the bit position of the error.
- b. Show a block diagram of your data bus, memory, and various stages of parity generation and error correction mechanism.
- c. Design the detailed design of parity generation, syndrome generation and error correction circuitry using basic gates.
- d. How you would modify the SEC code you have defined above in order to obtain an SEC/DED code.

Problem 3 (20 Points)

A cyclic code is to be based on the Generator polynomial $X^6 + X^5 + X^2 + 1$.

- a. Generate a codeword for the input data 10111.
- b. Using logic gates, design an appropriate encoder and decoder the given generator.

Problem 4 (20 Points)

- a. Using full adders and basic gates, design a 5N code encoder, where N is a 4-bit binary number.
- b. Based on the code distance, determine if the code has error detecting and/or error correcting capability.

Problem 5 (20 Points)

Consider a low-cost residue code based on module 7.

- a. Show how do you obtain residue-7 check bits of X₇ X₆ X₅ X₄ X₃ X₂ X₁ X₀ using recursive addition technique?
- b. What is the theoretical base for this easy encoding process?

Problem 6 (20 Points)

Convert 0 to 14 to RNS using modules [3,4,5,7].

- a. For the given range, does the code has the capacity for error detection? If yes, how many bits?
- b. For this given range, does the code has the capacity for error correction? If yes, how many bits?

Problem 7 (15 Points)

Design a totally self-checking checker with 8 inputs. After showing the internal circuitry of one module, you may use block form to implement the design of an 8 input unit.

Due: Friday 2/26/ 2016