

## EGC220 Digital Logic Fundamentals

### Test 1

**For full credit, you need to show your work.**  
**Closed Book and Notes**

First Name: Key Last Name: \_\_\_\_\_

- Your submission must be in a single PDF file
- Make sure you submit before the deadline of 3:15 PM. I will not accept late submission by email.
- You must adhere to the honor code. Any evidence of misconduct will be dealt with strictly per syllabus.

5 PT.

1) Convert  $(30.25)_{10}$  to base 2 and 16.

$$\begin{array}{cccccccc}
 & 16 & 8 & 4 & 2 & 1 & .5 & .25 \\
 \phi & \phi & \phi & 1 & 1 & 1 & 1 & 0 \\
 \hline
 & & & & & & 0 & 1 & 0 & 0
 \end{array}$$

1
E
4

$$\boxed{11110.01}$$

$$\boxed{1E.4}$$

15 PT.

2) Perform the following operations in the indicated base.

a.

$$\begin{array}{r}
 1 \\
 (2.3)_6 \\
 + (15.2)_6 \\
 \hline
 (21.5)_6
 \end{array}$$

$$\boxed{(21.5)_6}$$

b.

$$\begin{array}{r}
 +6 \\
 23 + 6 \\
 (34.3)_6 \\
 - (25.5)_6 \\
 \hline
 (4.4)_6
 \end{array}$$

$$\boxed{(4.4)_6}$$

c.

$$\begin{array}{r}
 (4.3)_6 \\
 \times (13.2)_6 \\
 \hline
 130 \\
 213 \\
 43 \\
 \hline
 110.00
 \end{array}$$

$6 \div 6 = 1 \quad R=0$   
 $9 \div 6 = 1 \quad R=3$   
 $13 \div 6 = 2 \quad R=1$   
 $7 \div 6 = 1 \quad R=1$

$$\boxed{(110)_6}$$

5 PT.

3) Perform  $(57)_{10} - (74)_{10}$  operations in binary, assuming signed 2's complement notation.

S	64	32	16	8	4	2	1	
0	0	1	1	1	0	0	1	57
0	1	0	0	1	0	1	0	74
1	0	1	1	0	1	1	0	-74

$$\begin{array}{r}
 00111001 \\
 10110110 \\
 \hline
 11101111 \checkmark \\
 - 00010001 \\
 \hline
 \boxed{11101111} = -17 \checkmark
 \end{array}$$

10 PT.

4) What do the following binary numbers represent in

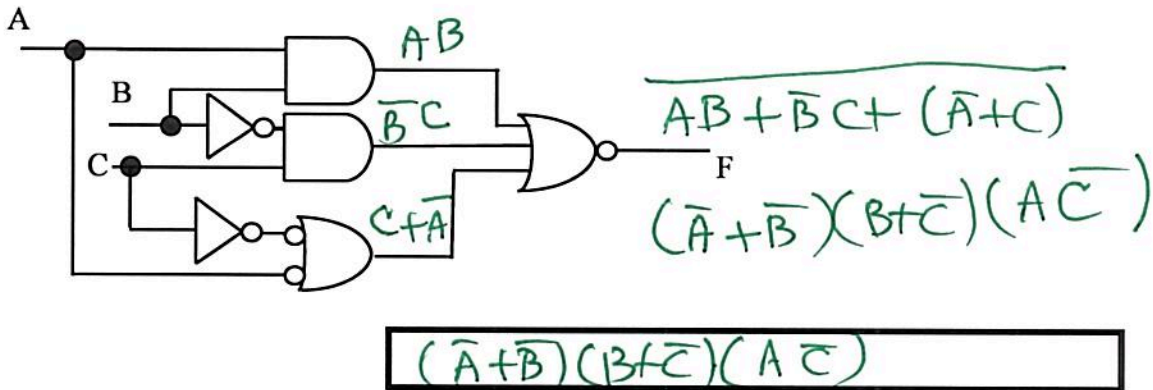
- Unsigned domain
- Signed magnitude
- Signed 2's complement

	Unsigned	Signed magnitude	Signed 2's complement
00111101	61	+61	+61
11010110	214	-86	-42

32 16 8 4 2 1  
 64 128  
 32 16 8 4 2 1  
 32 16 8 4 2 1  
 - 00101010

10 PT.

5) Find the Boolean equation for the following circuit. You do not need to simplify the function. However, there should not be a bar over more than one term.



10 PT.

6) By means of truth table prove or disprove that  $A + \overline{B}C = (A + \overline{B})(A + \overline{C})$

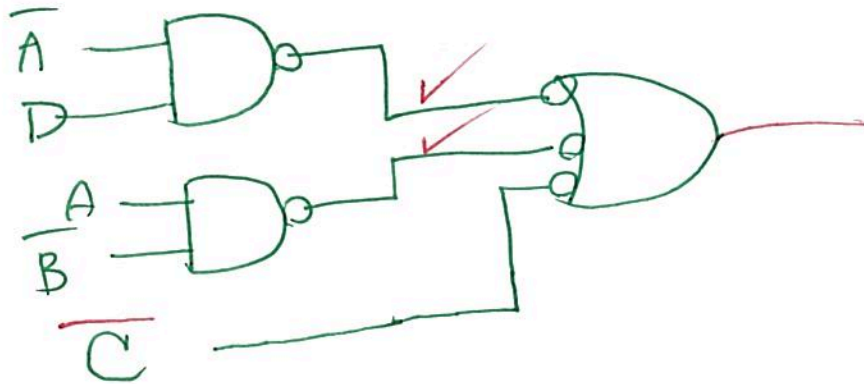
not the same

A	B	C	$\overline{B}C$	$A + \overline{B}C$	$A + \overline{B}$	$A + \overline{C}$	$(A + \overline{B})(A + \overline{C})$
0	0	0	0	0	1	1	1
0	0	1	1	1	1	0	0
0	1	0	0	0	0	1	0
0	1	1	0	0	1	0	0
1	0	0	0	1	1	1	1
1	0	1	1	1	1	1	1
1	1	0	0	1	1	1	1
1	1	1	0	1	1	1	1

10 PT.

7) Implement the following function using all NAND gates.

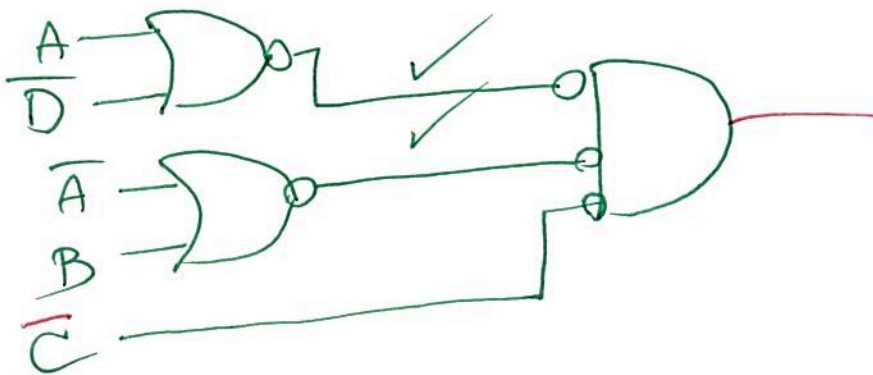
$$F = C + \bar{A}D + A\bar{B}$$



10 PT.

8) Implement the following function using all NOR gates

$$F = C(A + \bar{D})(\bar{A} + B)$$



10 PT.

9) For the following function  $F(A, B, C) = \bar{A}\bar{B} + BC + \bar{A}B\bar{C}$

- Make a truth table
- Using Boolean algebra simplify the function.

A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

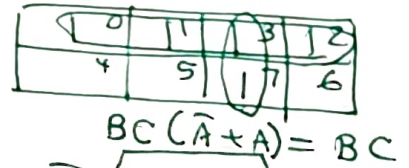
$$F = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + ABC$$

$$\underbrace{\bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C}_{\bar{A}\bar{B}(\bar{C}+C)} + \underbrace{\bar{A}B\bar{C} + \bar{A}BC}_{\bar{A}B(\bar{C}+C)} + ABC$$

$$\bar{A}\bar{B} + \bar{A}B + BC$$

$$\bar{A}(\bar{B}+B) + BC$$

$$\bar{A} + BC$$



15 PT.

9) For Boolean expression  $F(A, B, C, D) = \prod M(7, 8, 12, 13, 15) + d(0, 2, 5, 10, 14)$ , determine

- Sum of Min terms.
- Minimum sum of products.
- Minimum products of sums.

a.  $F = \sum m(1, 3, 4, 6, 9, 11) + d(0, 2, 5, 10, 14)$

b.  $F = \bar{A}\bar{D} + \bar{B}D$

c.  $\bar{F} = BD + A\bar{D}$

$F = (\bar{B} + \bar{D})(\bar{A} + D)$

