

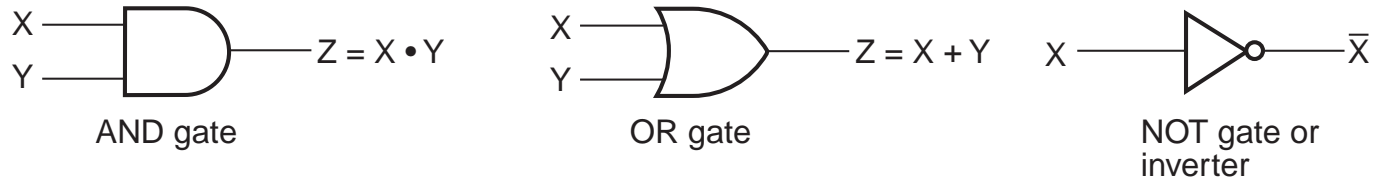
## 2-1 Table 2-1 Truth Tables for the Three Basic Logic Operations

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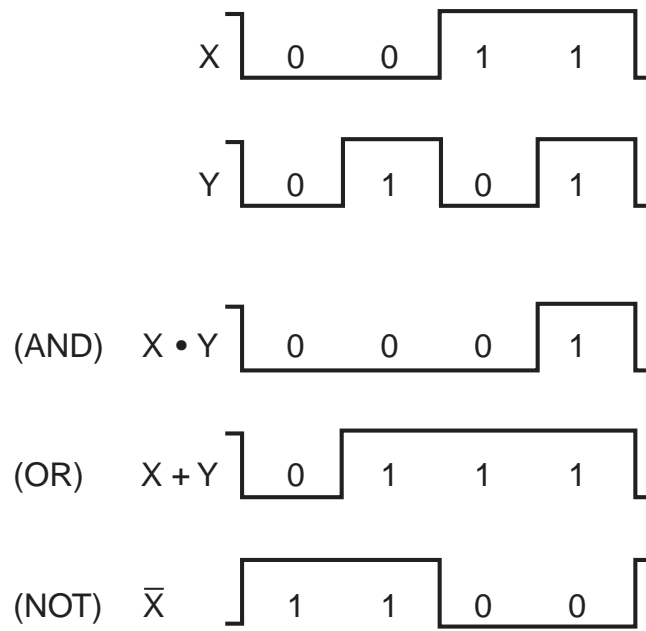
AND			OR			NOT	
X	Y	Z	X	Y	Z	X	Z
0	0	0	0	0	0	0	1
0	1	0	0	1	1	1	0
1	0	0	1	0	1		
1	1	1	1	1	1		

---

Figure 2-1 Digital Logic Gates

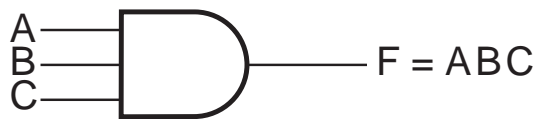


(a) Graphic symbols

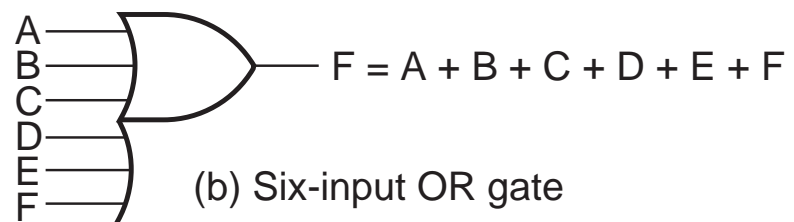


(b) Timing diagram

Figure 2-2 Gates with More than Two Inputs



(a) Three-input AND gate



(b) Six-input OR gate

Table 2-2 Truth Table for the Function  $F = X + Y'Z$ 

X	Y	Z	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

2-5

Figure 2-3 Logic Circuit Diagram for  $F = X + Y'Z$

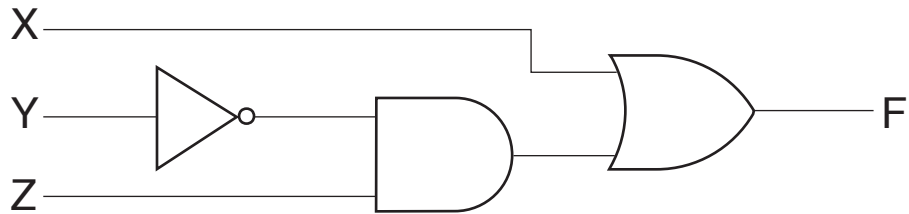


Table 2-3 Basic Identities of Boolean Algebra

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1.	$X + 0 = X$	2.	$X \cdot 1 = X$	
3.	$X + 1 = 1$	4.	$X \cdot 0 = 0$	
5.	$X + X = X$	6.	$X \cdot X = X$	
7.	$X + \bar{X} = 1$	8.	$X \cdot \bar{X} = 0$	
9.	$\overline{\bar{X}} = X$			
10.	$X + Y = Y + X$	11.	$XY = YX$	Commutative
12.	$X + (Y + Z) = (X + Y) + Z$	13.	$X(YZ) = (XY)Z$	Associative
14.	$X(Y + Z) = XY + XZ$	15.	$X + YZ = (X + Y)(X + Z)$	Distributive
16.	$\overline{X + Y} = \bar{X} \cdot \bar{Y}$	17.	$\overline{X \cdot Y} = \bar{X} + \bar{Y}$	DeMorgan's

---

Table 2-4 Truth Tables to Verify DeMorgan's Theorem

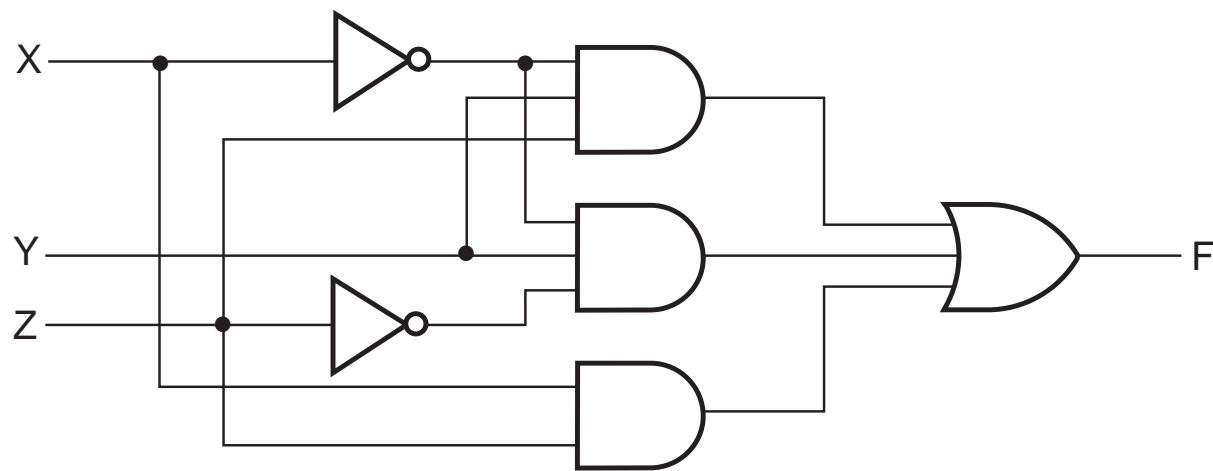
A)	X	Y	$\overline{X+Y}$	B	X	Y	$\overline{X}$	$\overline{Y}$	$\overline{X} \cdot \overline{Y}$
	0	0	1		0	0	1	1	1
	0	1	0		0	1	1	0	0
	1	0	0		1	0	0	1	0
	1	1	0		1	1	0	0	0

Table 2-5 Truth Table for Boolean Function

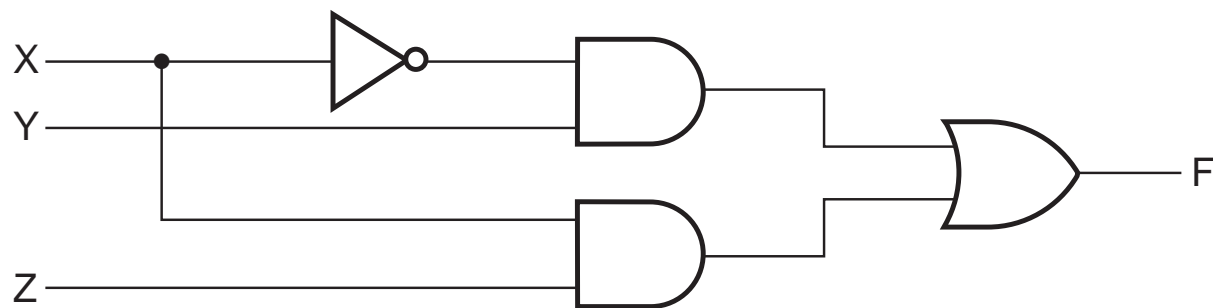
X	Y	Z	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1



Figure 2-4 Implementation of Boolean Function with Gates



(a)  $F = \bar{X}YZ + \bar{X}Y\bar{Z} + XZ$



(b)  $F = \bar{X}Y + XZ$



Table 2-7 Maxterms for Three Variables

X	Y	Z	Sum Term	Symbol	M <sub>0</sub>	M <sub>1</sub>	M <sub>2</sub>	M <sub>3</sub>	M <sub>4</sub>	M <sub>5</sub>	M <sub>6</sub>	M <sub>7</sub>
0	0	0	$X + Y + Z$	M <sub>0</sub>	0	1	1	1	1	1	1	1
0	0	1	$X + Y + \bar{Z}$	M <sub>1</sub>	1	0	1	1	1	1	1	1
0	1	0	$X + \bar{Y} + Z$	M <sub>2</sub>	1	1	0	1	1	1	1	1
0	1	1	$X + \bar{Y} + \bar{Z}$	M <sub>3</sub>	1	1	1	0	1	1	1	1
1	0	0	$\bar{X} + Y + Z$	M <sub>4</sub>	1	1	1	1	0	1	1	1
1	0	1	$\bar{X} + Y + \bar{Z}$	M <sub>5</sub>	1	1	1	1	1	0	1	1
1	1	0	$\bar{X} + \bar{Y} + Z$	M <sub>6</sub>	1	1	1	1	1	1	0	1
1	1	1	$\bar{X} + \bar{Y} + \bar{Z}$	M <sub>7</sub>	1	1	1	1	1	1	1	0

Table 2-8 Boolean Function of Three Variables

(a)	X	Y	Z	F	$\bar{F}$	(b)	X	Y	Z	E
	0	0	0	1	0		0	0	0	1
	0	0	1	0	1		0	0	1	1
	0	1	0	1	0		0	1	0	1
	0	1	1	0	1		0	1	1	0
	1	0	0	0	1		1	0	0	1
	1	0	1	1	0		1	0	1	1
	1	1	0	0	1		1	1	0	0
	1	1	1	1	0		1	1	1	0

Figure 2-8 Two-Variable Map

$m_0$	$m_1$
$m_2$	$m_3$

(a)

		0	1
Y X			
0	$\bar{X}\bar{Y}$	$\bar{X}Y$	
1	$X\bar{Y}$	$XY$	

(b)

Figure 2-9 Representation of Functions in the Map

		Y		
	X		0	1
	0			
	1			1

(a)  $XY$ 

		Y		
	X		0	1
	0			1
	1		1	1

(b)  $X + Y$

Figure 2-10 Three-Variable Map

$m_0$	$m_1$	$m_3$	$m_2$
$m_4$	$m_5$	$m_7$	$m_6$

(a)

		YZ		
		00	01	Y 11 10
X	0	$\bar{X}\bar{Y}\bar{Z}$	$\bar{X}\bar{Y}Z$	$\bar{X}YZ$
	1	$X\bar{Y}\bar{Z}$	$X\bar{Y}Z$	$XYZ$
		Z		

(b)

Figure 2-11 Map for Example 2-3

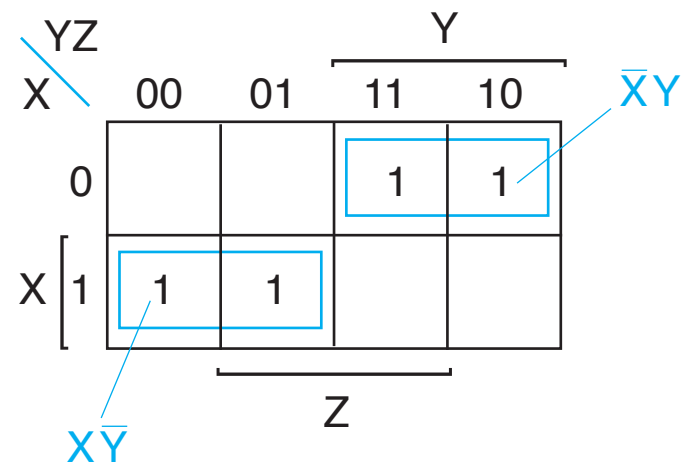




Figure 2-12 Three-Variable Map: Flat and on a Cylinder to Show Adjacent Squares

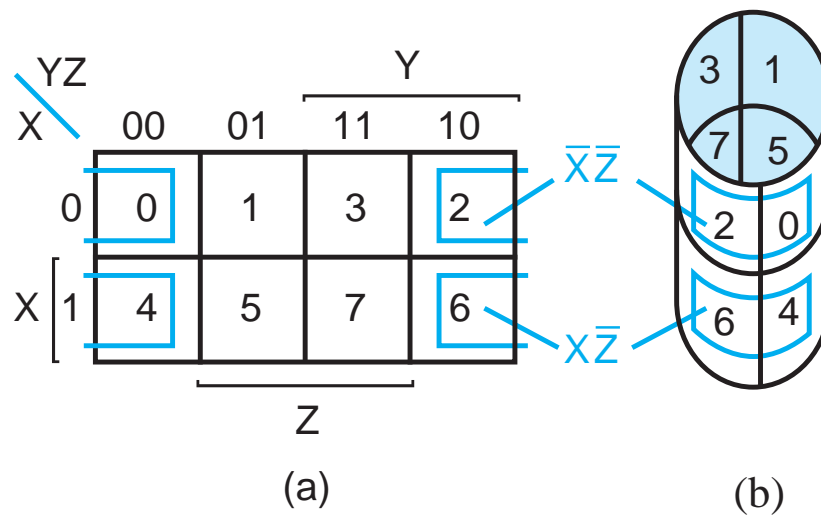


Figure 2-13 Product Terms Using Four Minterms

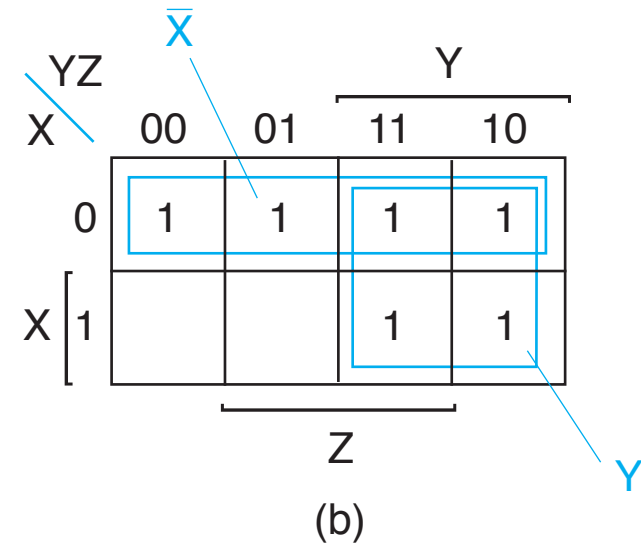
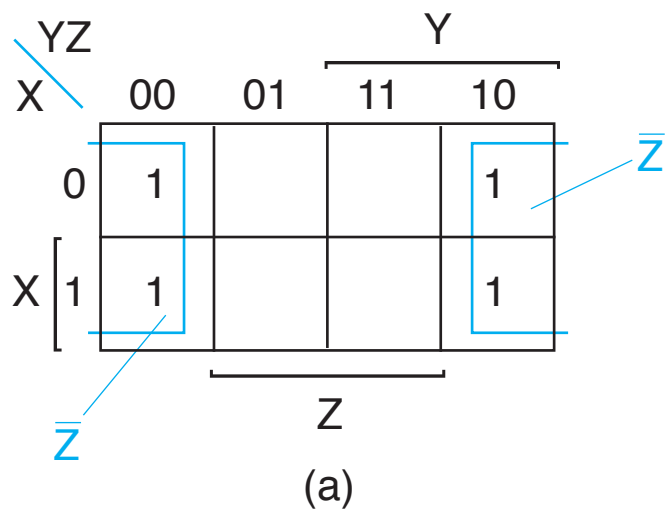
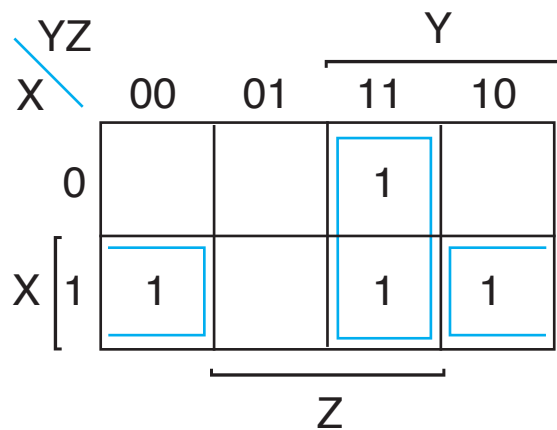
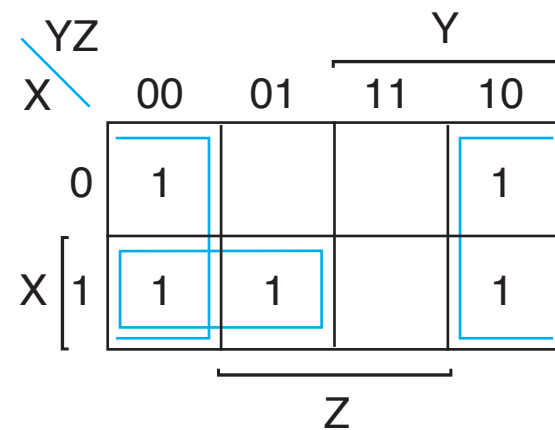


Figure 2-14 Maps for Example 2-4



$$(a) F_1(X, Y, Z) = m(3, 4, 6, 7) \\ = YZ + X\bar{Z}$$



$$(b) F_2(X, Y, Z) = m(0, 2, 4, 5, 6) \\ = \bar{Z} + XY$$

Figure 2-15  $F(X, Y, Z) = \text{SUM } m(1, 3, 4, 5, 6)$ 

		YZ			
		00	01	11	10
X	0		1	1	
	1	1	1		1

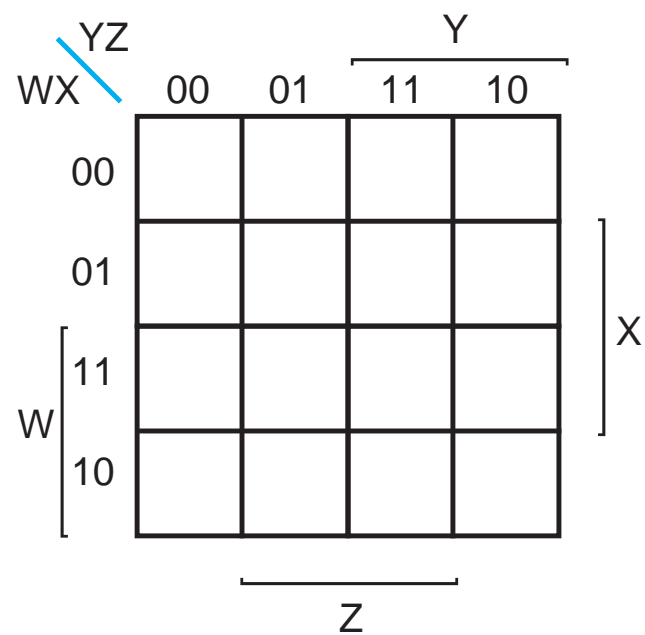
Figure 2-16  $F(X, Y, Z) = \text{SUM } m(1, 2, 3, 5, 7)$ 

YZ		Y			
		00	01	11	10
X	0		1	1	1
	1		1	1	

Figure 2-17 Four-Variable Map

$m_0$	$m_1$	$m_3$	$m_2$
$m_4$	$m_5$	$m_7$	$m_6$
$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
$m_8$	$m_9$	$m_{11}$	$m_{10}$

(a)



(b)

Figure 2-18 Four-Variable Map: Flat and on a Torus to Show Adjacencies

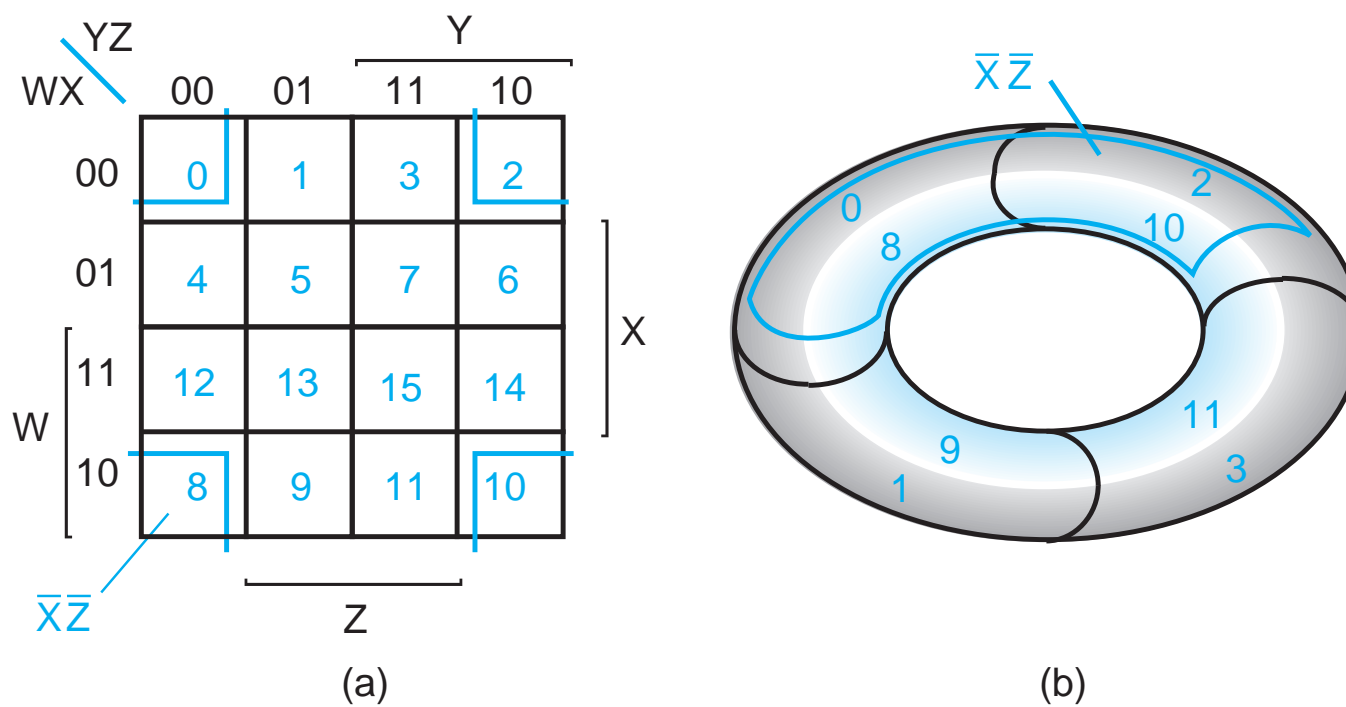


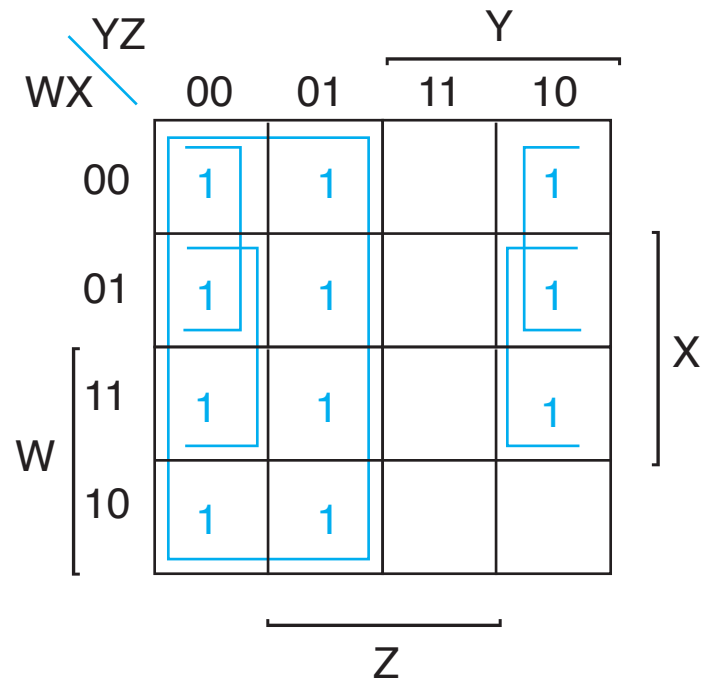
Figure 2-19 Map for Example 2-5:  $F = Y' + W'Z' + XZ'$ 



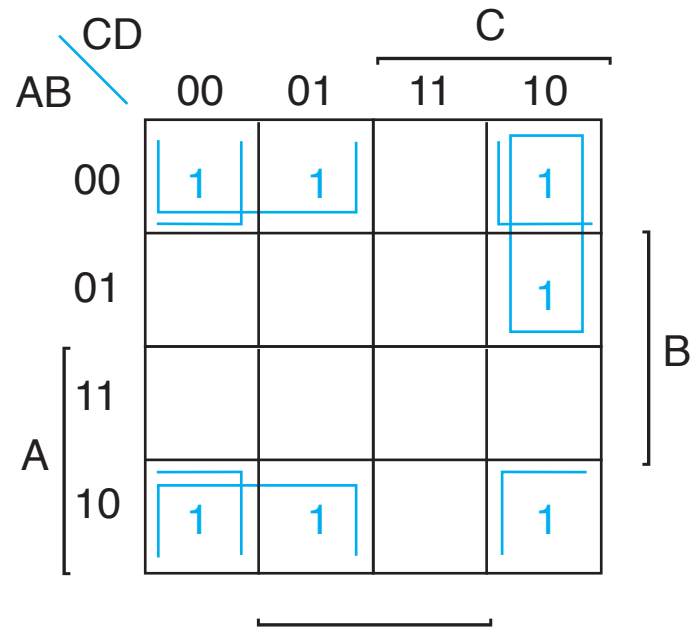
Figure 2-20 Map for Example 2-6:  $F = B'D' + B'C + A'CD'$ 

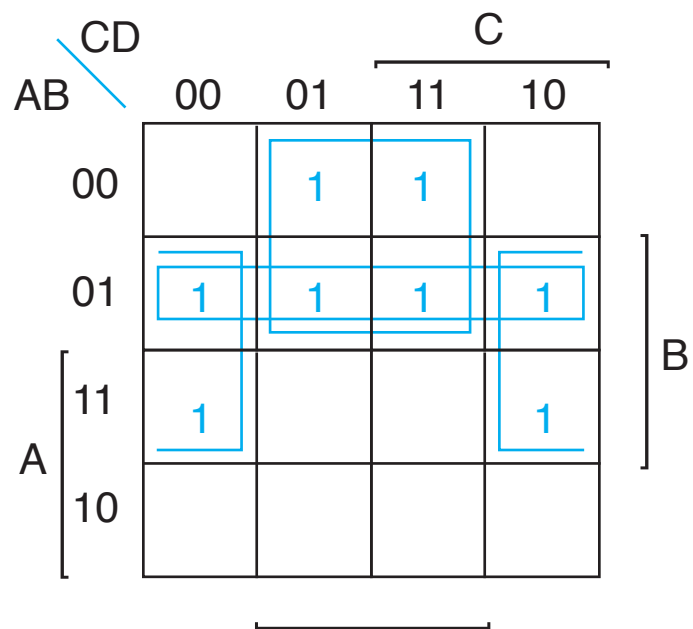
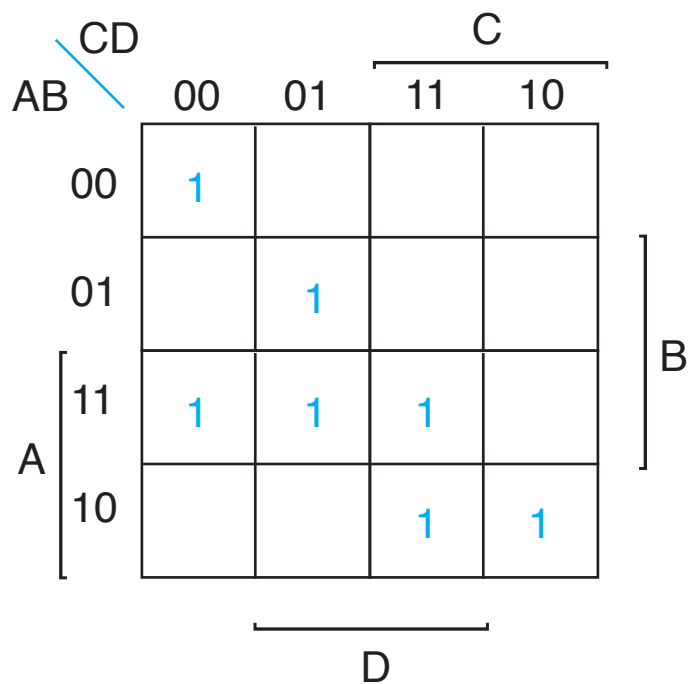
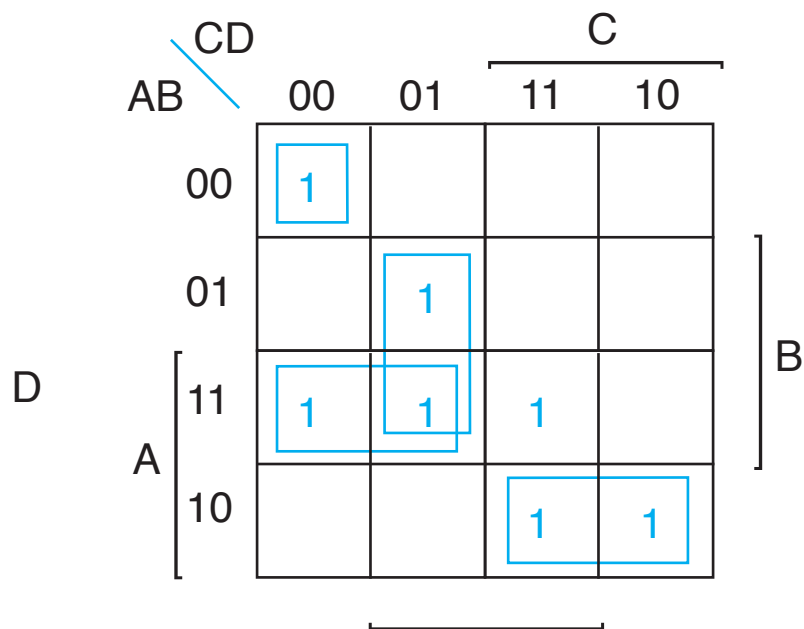
Figure 2-21 Prime Implicants for Example 2-7:  $A'D$ ,  $BD'$ , and  $A'B$ 

Figure 2-22 Simplification with Prime Implicants in Example 2-8



(a) Plotting the minterms



(b) Essential prime implicants

Figure 2-23 Map for Example 2-9

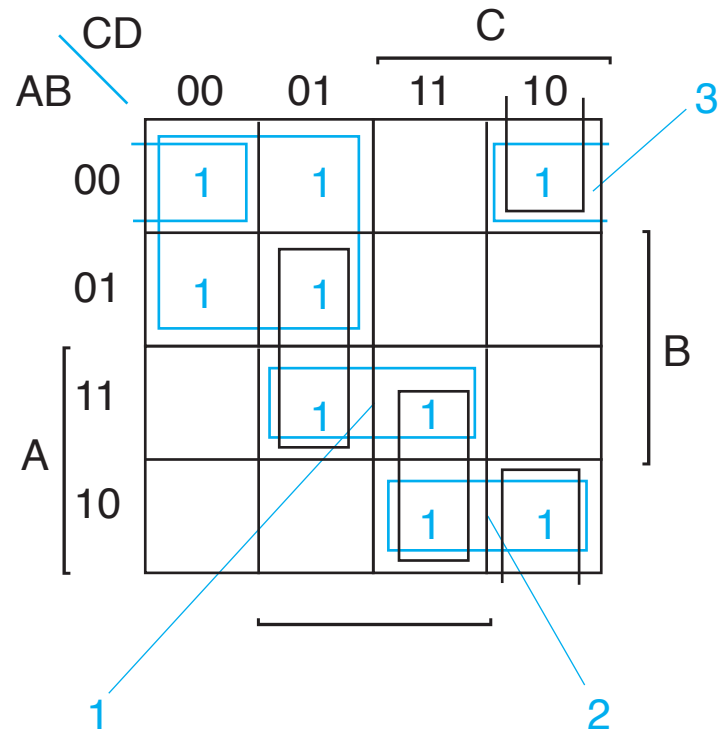


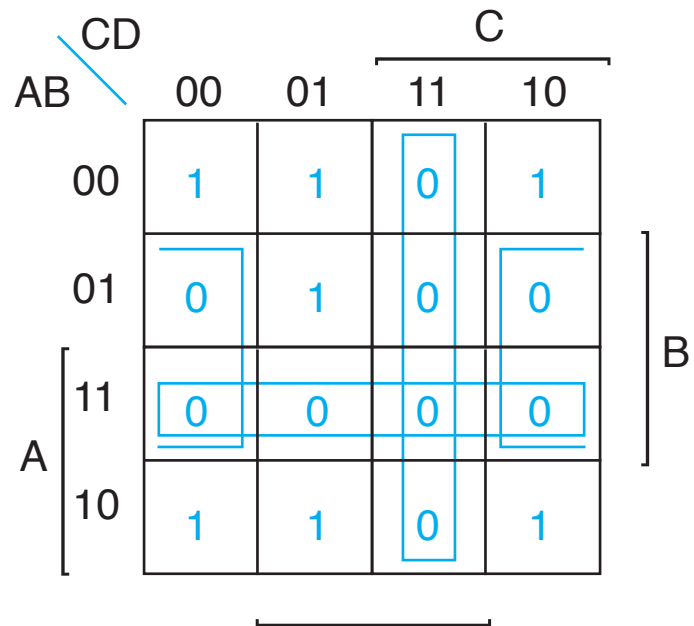
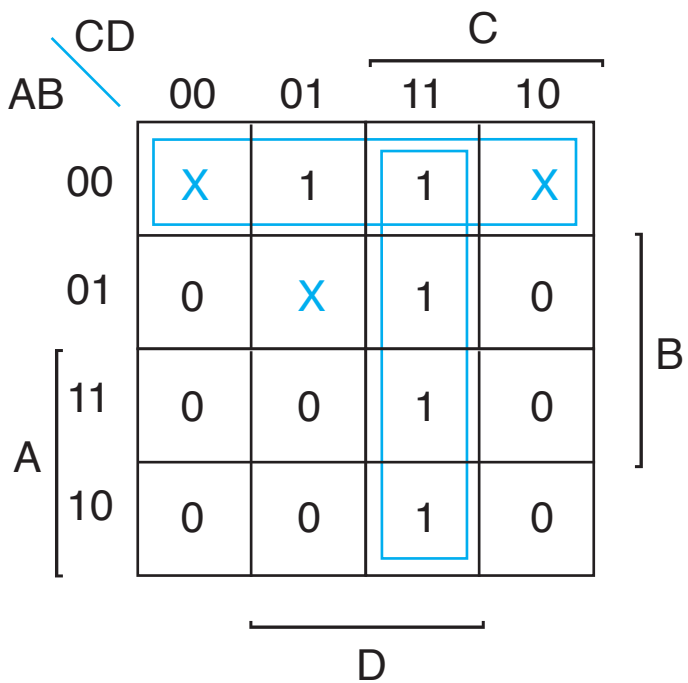
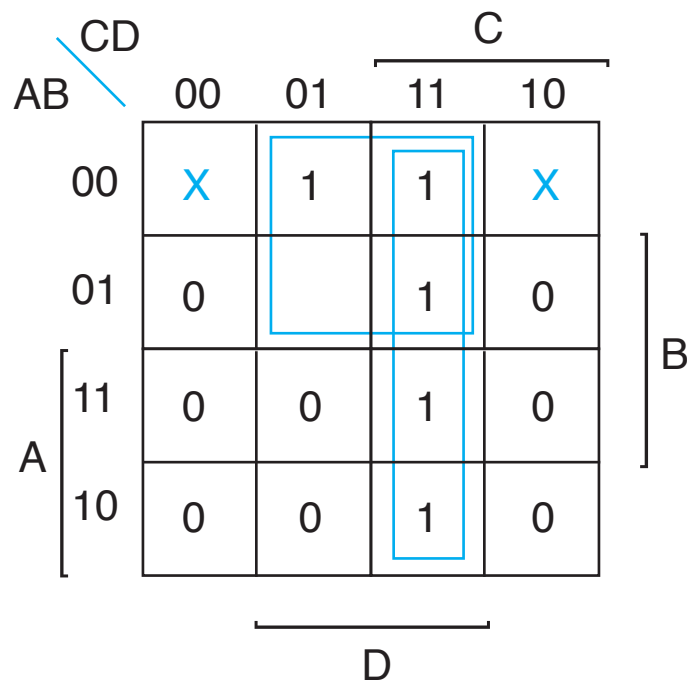
Figure 2-24 Map for Example 2-10:  $F = (A' + B')(C' + D')(B' + D)$ 

Figure 2-25 Example with Don't Care Conditions



(a)  $F = CD + \bar{A}\bar{B}$

X



(b)  $F = CD + \bar{A}D$

## Graphics Symbols


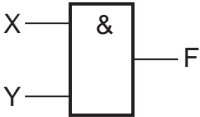
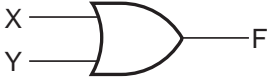
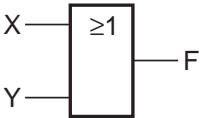
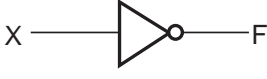
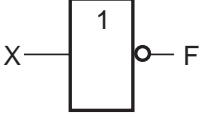

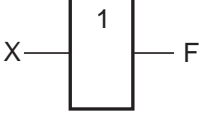

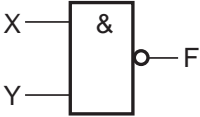

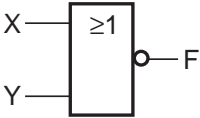

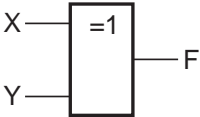

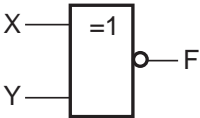
Name	Distinctive shape	Rectangular shape	Algebraic equation	Truth table															
AND			$F = XY$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	X	Y	F	0	0	0	0	1	0	1	0	0	1	1	1
X	Y	F																	
0	0	0																	
0	1	0																	
1	0	0																	
1	1	1																	
OR			$F = X + Y$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	X	Y	F	0	0	0	0	1	1	1	0	1	1	1	1
X	Y	F																	
0	0	0																	
0	1	1																	
1	0	1																	
1	1	1																	
NOT (inverter)			$F = \bar{X}$	<table border="1"> <thead> <tr><th>X</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </tbody> </table>	X	F	0	1	1	0									
X	F																		
0	1																		
1	0																		
Buffer			$F = X$	<table border="1"> <thead> <tr><th>X</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td></tr> </tbody> </table>	X	F	0	0	1	1									
X	F																		
0	0																		
1	1																		
NAND			$F = \overline{X \cdot Y}$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	X	Y	F	0	0	1	0	1	1	1	0	1	1	1	0
X	Y	F																	
0	0	1																	
0	1	1																	
1	0	1																	
1	1	0																	
NOR			$F = \overline{X + Y}$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	X	Y	F	0	0	1	0	1	0	1	0	0	1	1	0
X	Y	F																	
0	0	1																	
0	1	0																	
1	0	0																	
1	1	0																	
Exclusive-OR (XOR)			$F = X\bar{Y} + \bar{X}Y$ $= X \oplus Y$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	X	Y	F	0	0	0	0	1	1	1	0	1	1	1	0
X	Y	F																	
0	0	0																	
0	1	1																	
1	0	1																	
1	1	0																	
Exclusive-NOR (XNOR)			$F = XY + \bar{X}\bar{Y}$ $= \overline{X \oplus Y}$	<table border="1"> <thead> <tr><th>X</th><th>Y</th><th>F</th></tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	X	Y	F	0	0	1	0	1	0	1	0	0	1	1	1
X	Y	F																	
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0	1	0																	
1	0	0																	
1	1	1																	

Figure 2-28 Alternative Graphics Symbols for NAND and NOT Gates

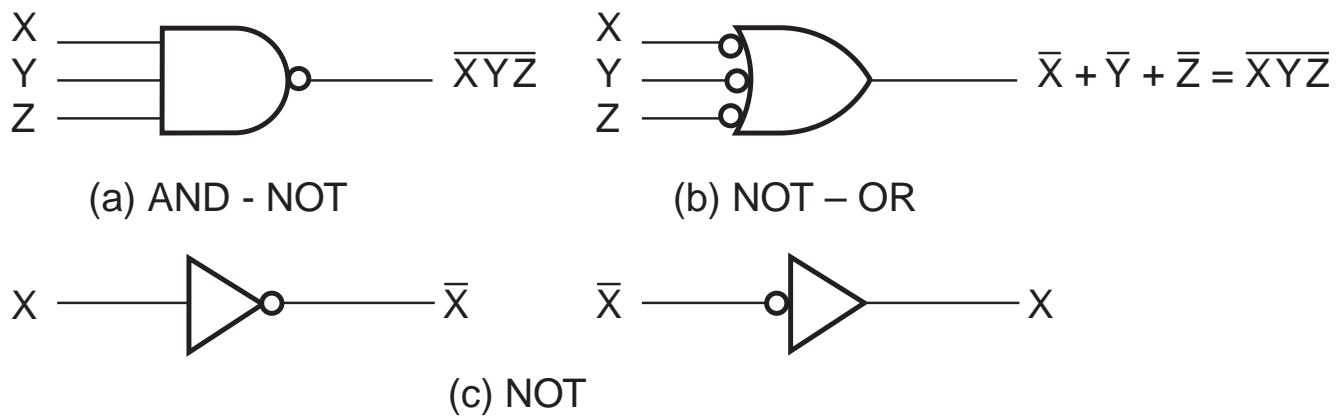
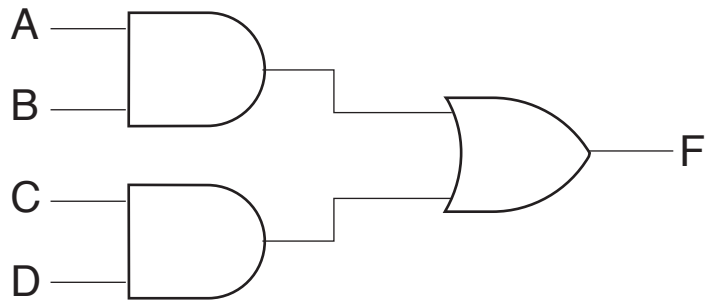
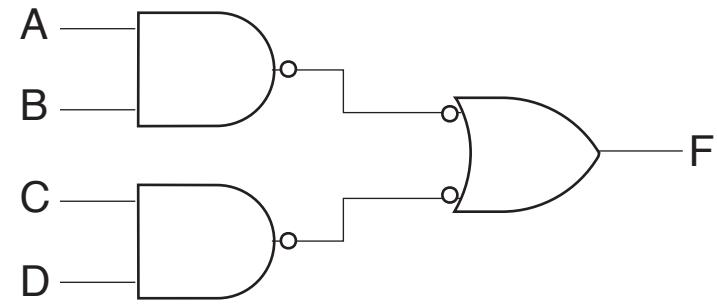


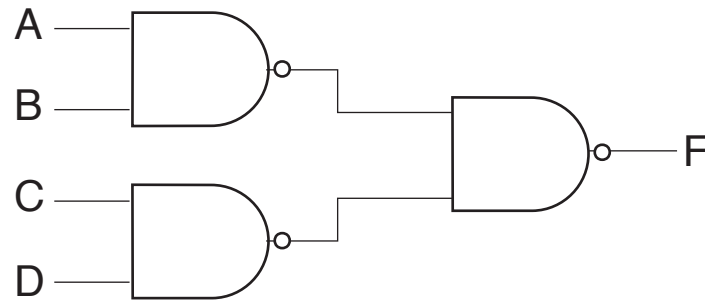


Figure 2-29 Three Ways to Implement  $F = AB + CD$ 

(a)



(b)



(c)

Figure 2-5 Sum-of-Products Implementation

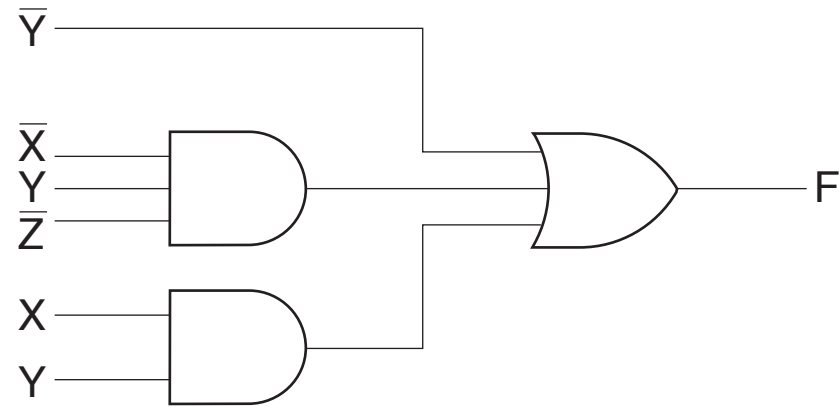


Figure 2-6 Three-Level and Two-Level Implementation

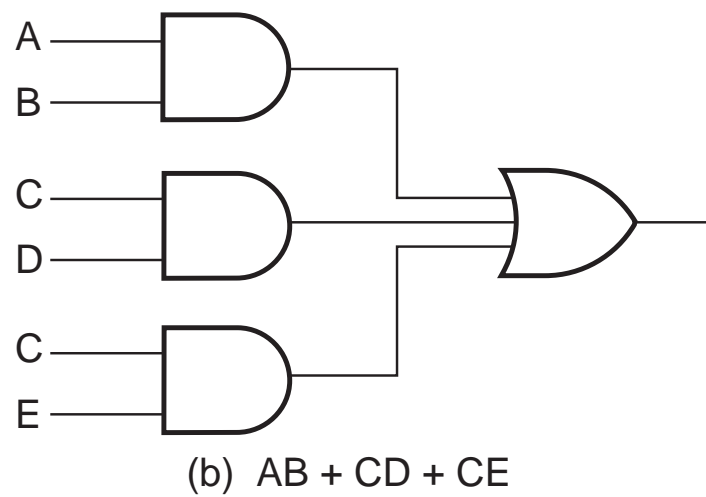
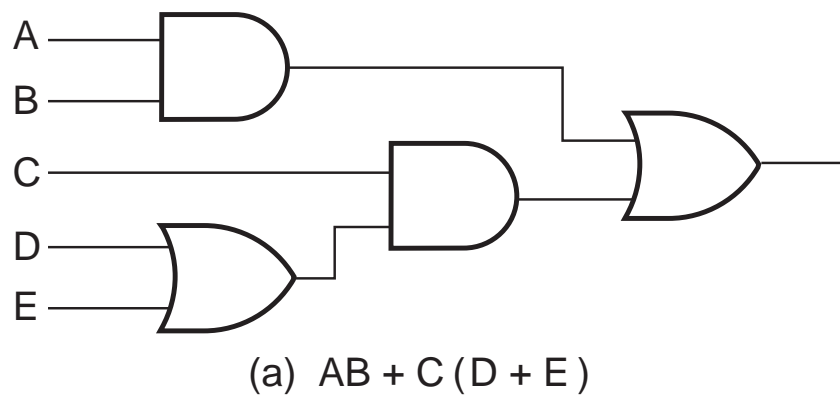


Figure 2-7 Product-of-Sums Implementation

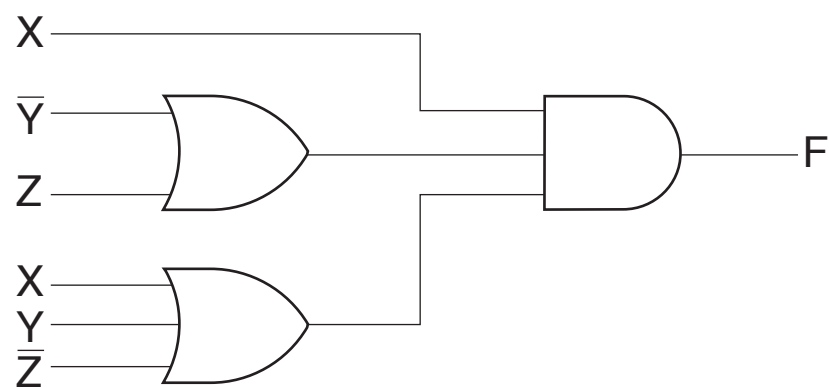
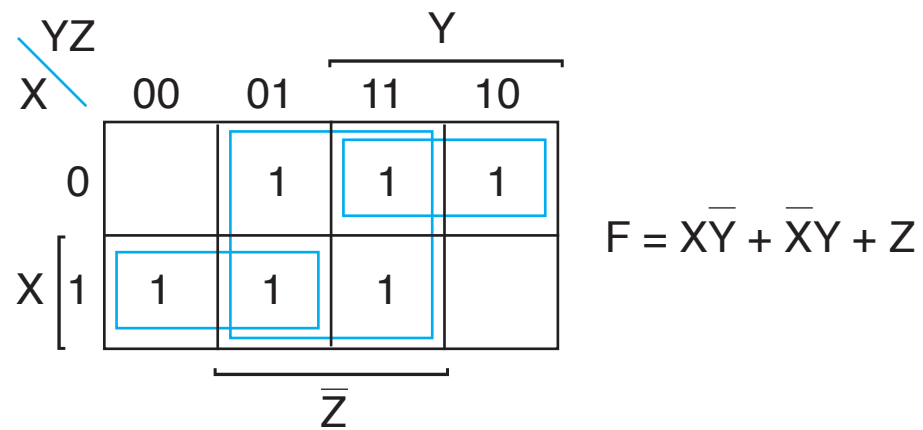
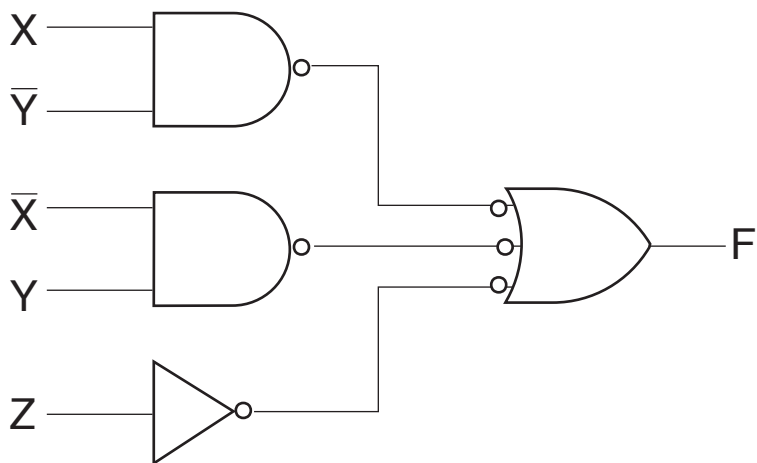


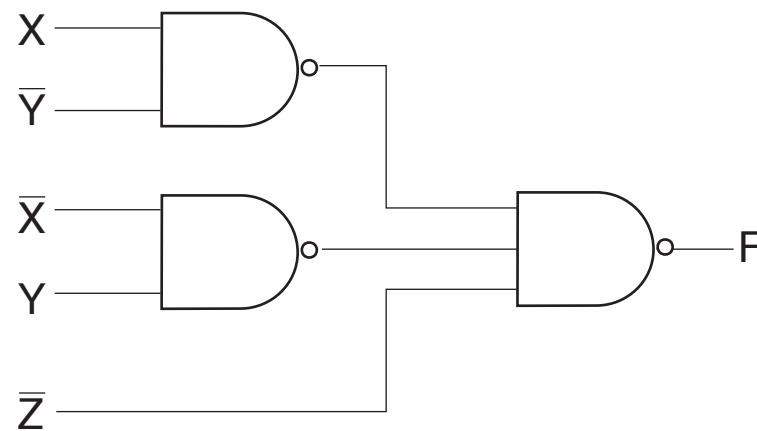
Figure 2-30 Solution to Example 2-12



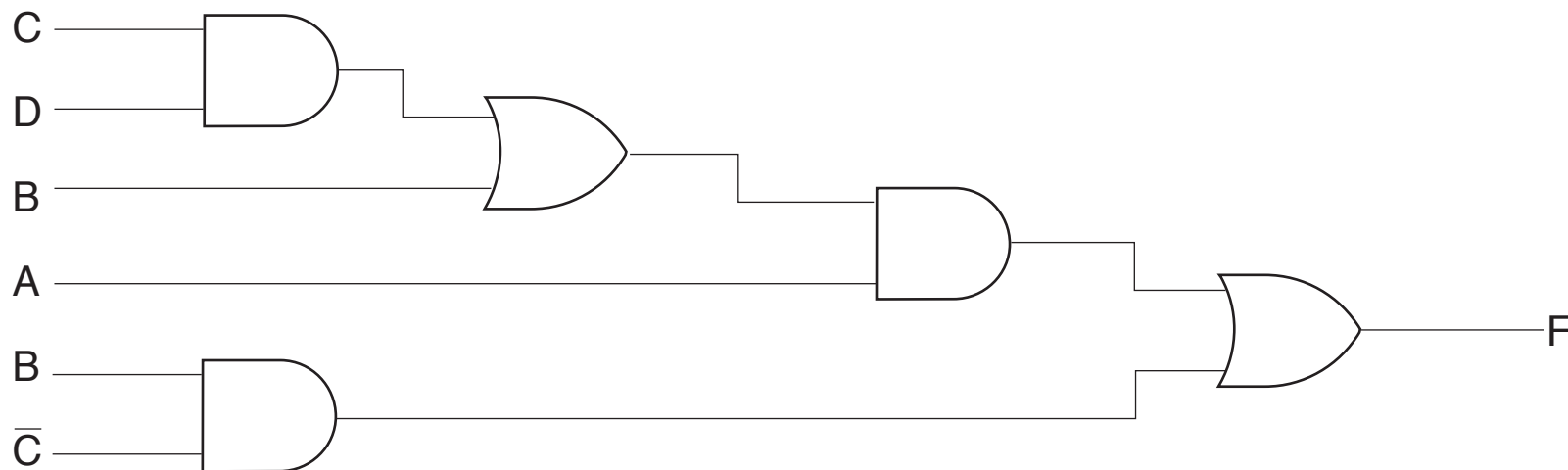
(a)



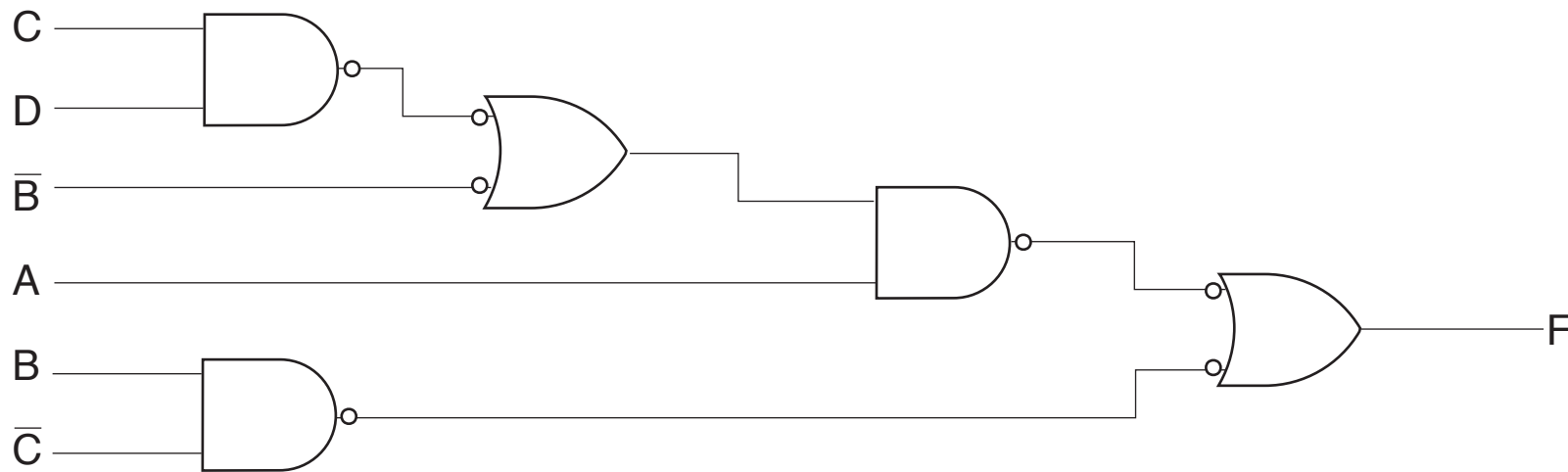
(b)



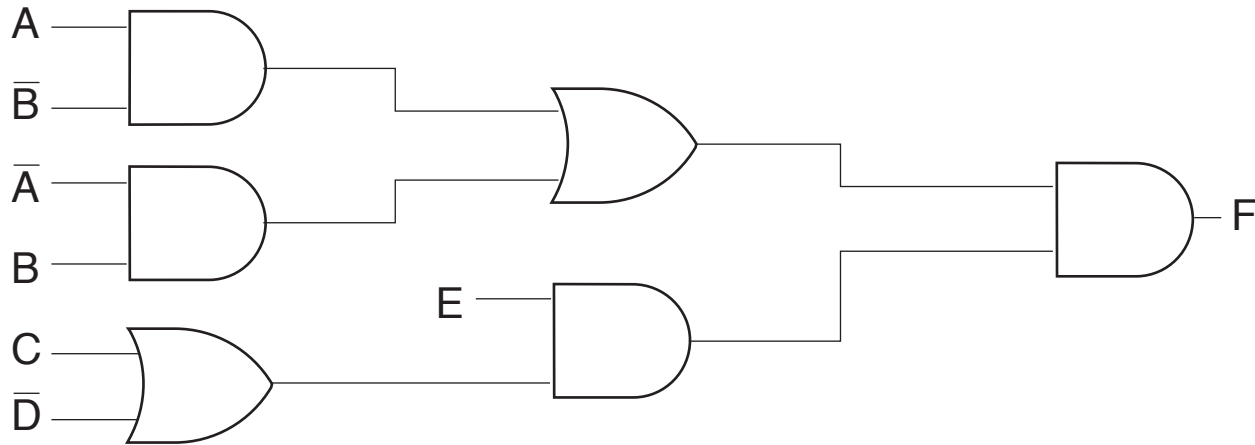
(c)

Figure 2-31 Implementing  $F = A(CD + B) + BC'$ 

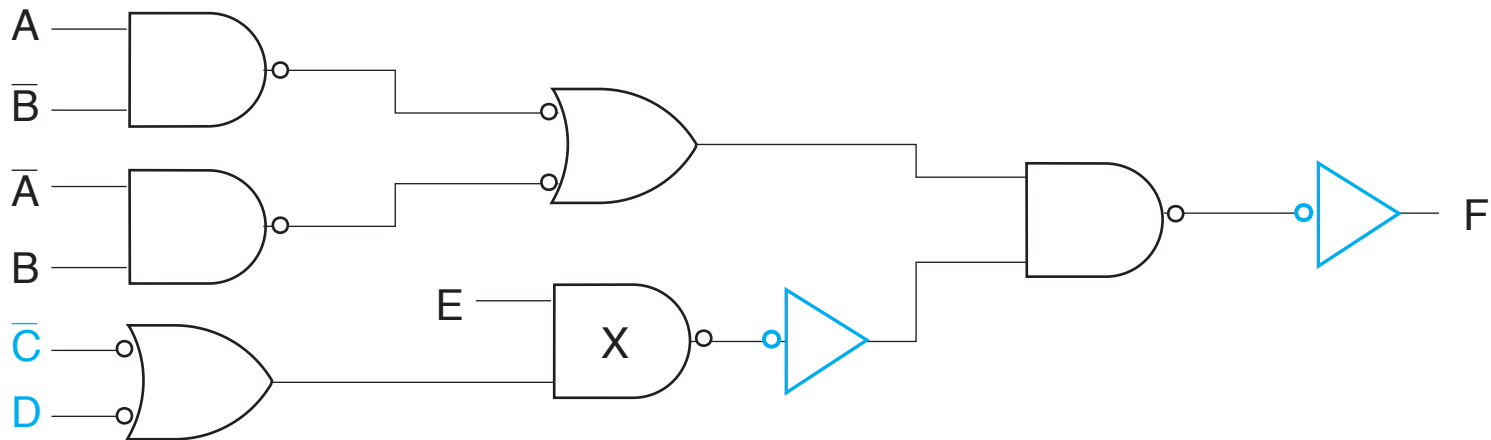
(a) AND – OR gates



(b) NAND gates

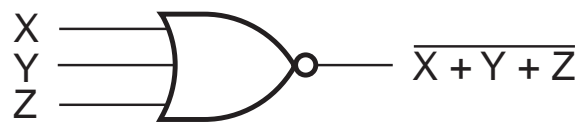
Figure 2-32 Implementing  $F = (AB' + A'B) E (C + D')$ 

(a) AND – OR gates

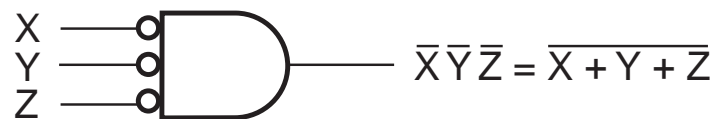


(b) NAND gates

Figure 2-34 Two Graphic Symbols for NOR Gate



(a) OR – NOT



(b) NOT – AND



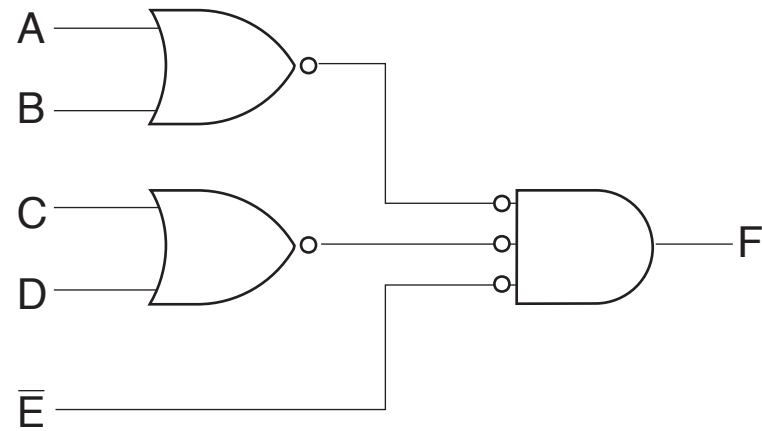
Figure 2-35 Implementing  $F = (A + B)(C + D)E$  with NOR Gates

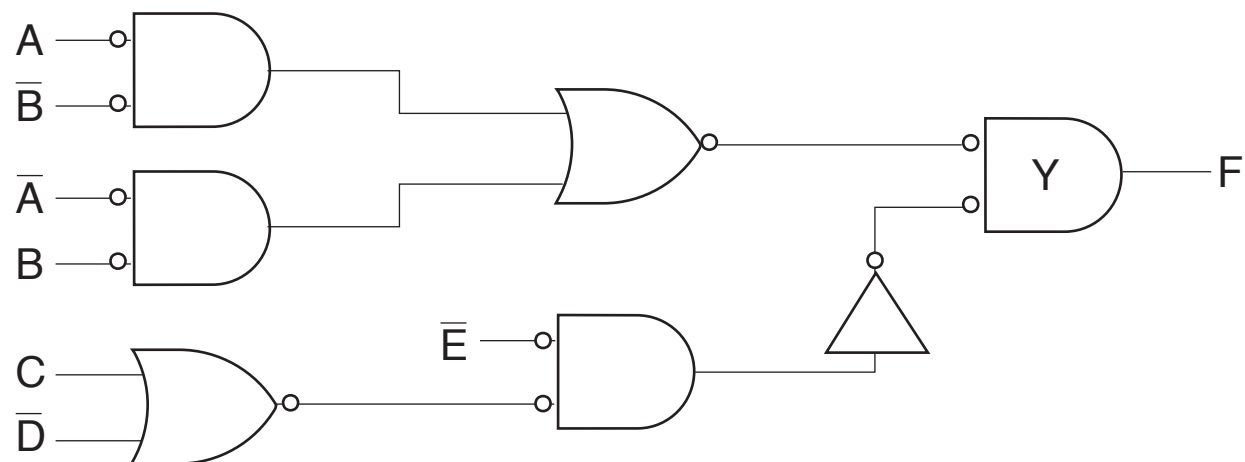
Figure 2-36 Implementing  $F = (AB' + A'B) E (C + D')$  with NOR Gates

Figure 2-37 Exclusive-OR Constructed with NAND Gates

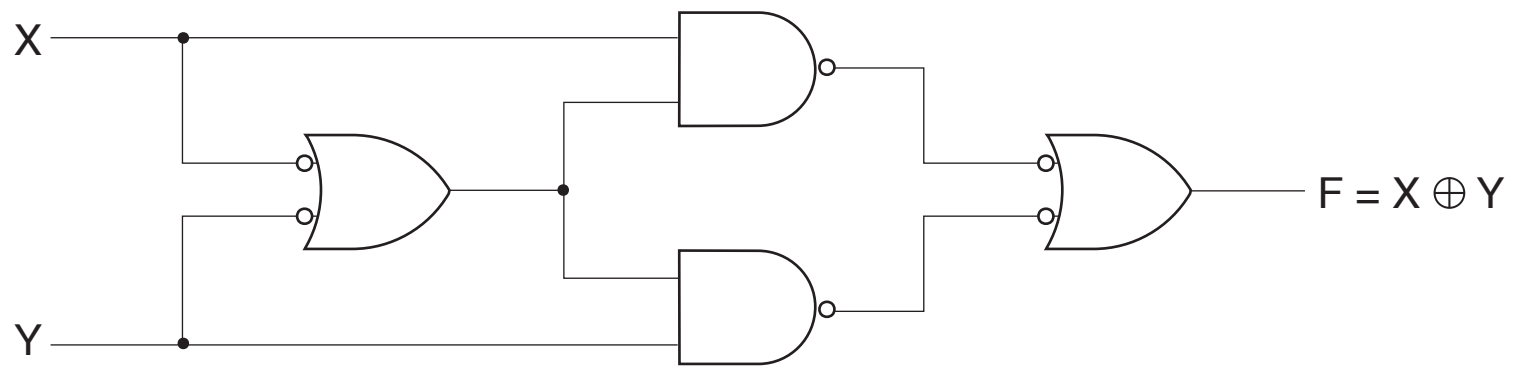


Figure 2-39 Multiple-Input Odd Functions

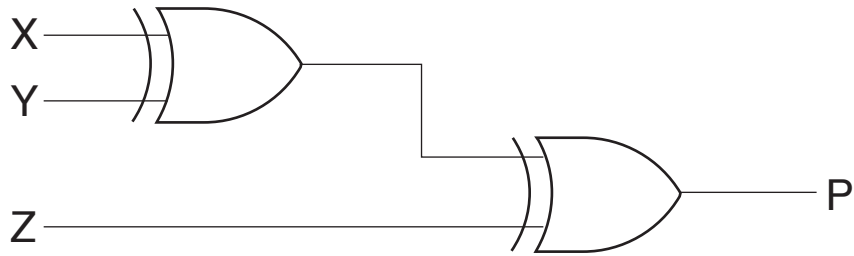
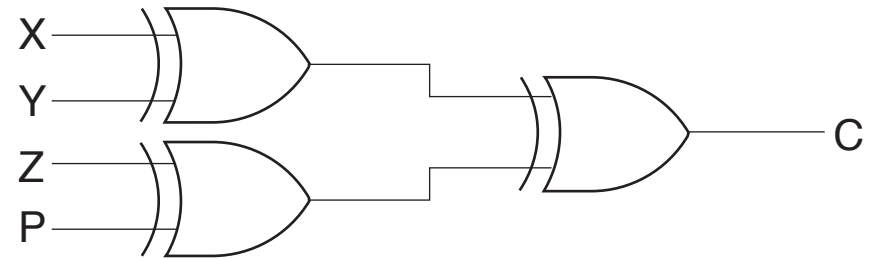
(a)  $P = X \oplus Y \oplus Z$ (b)  $C = X \oplus Y \oplus Z \oplus P$

Figure 2-40 Propagation Delay for an Inverter

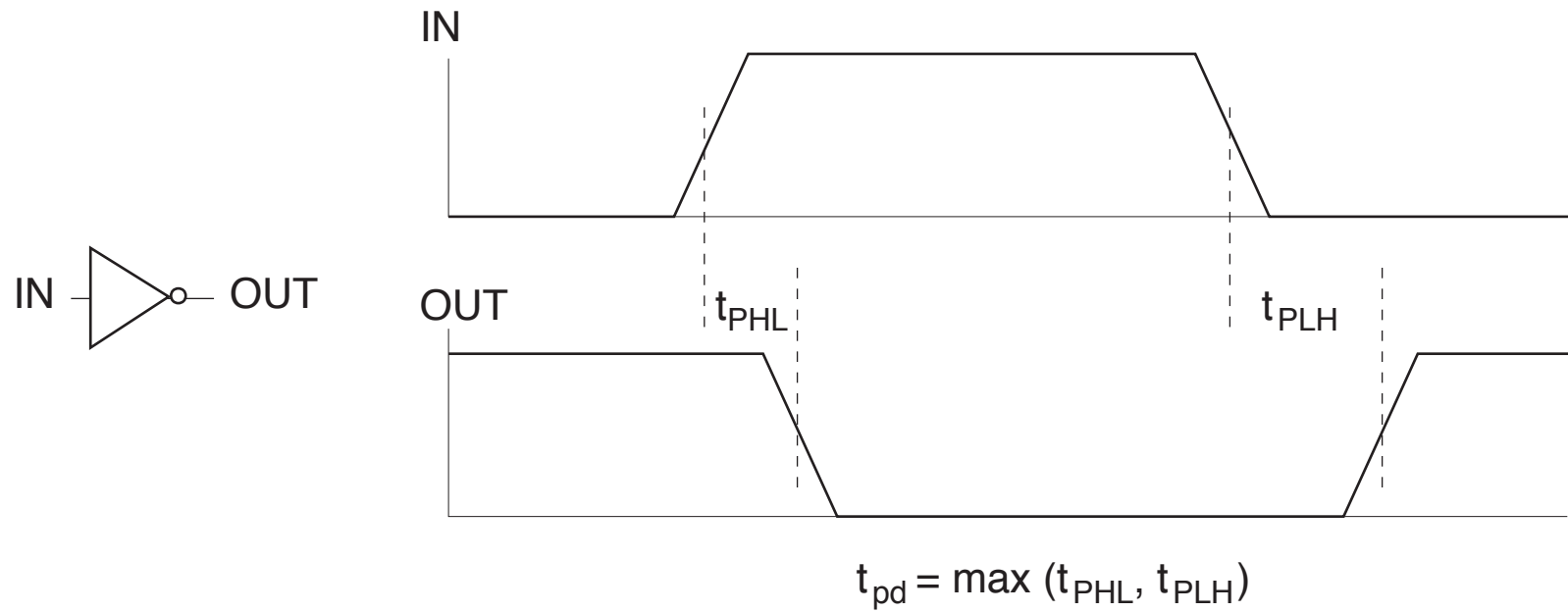


Figure 2-42 Signal Assignment and Logic Polarity

Signal value	Logic value	Signal value	Logic value
H	1	H	0
L	0	L	1

(a) Positive logic

(b) Negative logic