First Name: $\qquad$ Last Name: $\qquad$

1. Prove by means of truth table that $(\mathrm{AB})^{\prime}=\mathrm{A}^{\prime}+\mathrm{B}^{\prime}$
2. Circle T (true) or F (false) for each of these Boolean equations.
(a). $\quad T \quad F \quad A+1=A$
(b). $\quad T \quad F \quad A+B C=(A+B)(B+C)$
(c). $T \quad F \quad \bar{A} \oplus \bar{B}=A \oplus B$
(d). $\quad T \quad F \quad A(B C)=(A B) C$
(e). $T$ F $A+B+C=A \cdot B \cdot C$
3. Demonstrate by means of truth tables the validity of the following identities
a. DeMorgan's law for three variables: $(\mathrm{X}+\mathrm{Y}+\mathrm{Z})^{\prime}=\mathrm{X}^{\prime} \mathrm{Y}^{\prime} \mathrm{Z}^{\prime}$ and (XYZ) ${ }^{\prime}=\mathrm{X}^{\prime}+\mathrm{Y}^{\prime}+\mathrm{Z}$ '
b. $(\mathrm{X}+\mathrm{Y}) \mathrm{X}=\mathrm{X}$
4. Using AND and OR gates, draw the logic diagrams for the following Boolean expressions without expanding or simplifying them.
a. $Y=\left(A^{\prime}+B^{\prime}\right) C+B(A+C)$
b. $\mathrm{W}=\left(\mathrm{A}+\mathrm{B}^{\prime}\right)\left(\mathrm{C}+\mathrm{D}^{\prime}\right)$
5. Write the Boolean expression equivalent to the followinglogic circuit. Donot simplify! Hint: Each bubble has the same effect as an invertor.

6. Write a truth table for

$$
F(A, B, C)=(\overline{A+B)}(B+\bar{C})
$$

7. Find the dual of
a. $\mathrm{F}=\mathrm{A}^{\prime} \mathrm{B}+\mathrm{B}^{\prime} \mathrm{C}^{\prime}+\mathrm{D}^{\prime}$
b. $\quad F(A, B, C)=(\overline{A+B})(B+\bar{C})$
8. Find the complement of
a. $\mathrm{F}=\mathrm{A}^{\prime} \mathrm{B}+\mathrm{B}^{\prime} \mathrm{C}^{\prime}+\mathrm{D}^{\prime}$
b. $\quad F(A, B, C)=(\overline{A+B})(B+\bar{C})$
