

Name: \_\_\_\_\_

**Problem One (20 Points)**

Consider a random-access memory that has a word format  $X_4 X_3 X_2 X_1 X_0$  of size 5 bits. We can use Hamming code to correct any single bit in this memory.

- a) What is the H (or P) matrix?
- b) Given the four syndromes  $s_i$  computed by your SEC Hamming code for single-bit errors affecting data bit  $x_i$ ,  $0 \leq i \leq 4$ . Also give the error-free syndrome  $s^*$ .
- c) Explain how you would modify the SEC code you have defined above in order to obtain an SEC/DED code.

**Problem Two (20 Points)**

Using the combinatorial model, determine the reliability of a simplex, TMR, and 5MR systems as a function of reliability of a simplex system,  $R(t)$ . You may assume a fault-free voter. Using MathLab, plot the reliability of the three systems versus  $R(t)$  and comment on their relative reliabilities.

**Problem Three (25 Points)**

Using Markov model, determine the discrete solution for the reliability of a 3MR system with  $\lambda$  failure rate and  $\mu$  repair rate. You may assume that the system initially is fault free. Using MathLab plot  $R(t)$  from 0 to 5 hours using

- a.  $\Delta t = 0.01$ ,  $\lambda = .0001$  and  $\mu = .01$
- b.  $\Delta t = 0.01$ ,  $\lambda = .001$  and  $\mu = .01$
- c.  $\Delta t = 0.01$ ,  $\lambda = .0001$  and  $\mu = .001$

Due October 22, 2007