

Name: \_\_\_\_\_

Problem 1 (20 Points)

A cyclic code is to be based on the Generator polynomial  $X^7 + X^5 + X^4 + X + 1$ .

- Generate a codeword for the input data 10101.
- Using logic gates, design an appropriate encoder and decoder the given generator.

Problem 2 (20 Points)

A 4G X 16 memory system is design using 1 G X 4 chips. Assume chip failure modes are single-bit cell (55%), single-row all-0's (20%), single-column all-0's (15%), and whole-chip all-0's (10%). Also, assume 0 and 1 values are equally likely. Compare and comment on relative performance (single-error-detection coverage) and overhead of the following approaches.

- Bit per chip
- Bit per multiple chips
- Duplication
- Single precision checksum (one sum for the entire memory).

Problem 3 (10 Points)

Design a totally self-checking checker with 8 inputs.

Problem 4 (20 Points)

Consider a random-access memory that has an 8-bit data.

- Determine the H matrix such that the error code computed by your Single Error Correcting Hamming code specifies the bit position of the error.
- Design a circuit for such an encoder using basic gates.
- How you would modify the SEC code you have defined above in order to obtain an SEC/DED code.

Problem 5 (20 Points)

- Using full adders and basic gates, design a 3N code encoder, where N is a 3-bit binary number.
- Design a circuit to detect an error in the above 3N code.

Problem 6 (20 Points)

Consider a low-cost residue code based on module 7.

- Show how do you obtain residue-7 check bits of  $X_7 X_6 X_5 X_4 X_3 X_2 X_1 X_0$  using recursive addition technique?
- What is the theoretical base for this easy encoding process?

Problem 7 (15 Points)

Convert 0 to 14 to RNS using modules [3,5,7]. Within this range demonstrate if the code is single error detecting. Repeat the same for single error correcting.

Due: March 12, 2010